

Mathematica 11.3 Integration Test Results

Test results for the 314 problems in "3.2.1 (f+g x)^m (A+B log(e ((a+b x) over (c+d x))^n))^p.m"

Problem 10: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^4 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 396 leaves, 8 steps):

$$\begin{aligned} & - \frac{B (b c - a d) g^4 n (a + b x)^4 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{10 b d} + \frac{g^4 (a + b x)^5 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{5 b} + \\ & \frac{B (b c - a d)^2 g^4 n (a + b x)^3 \left(4 A + B n + 4 B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{30 b d^2} - \\ & \frac{B (b c - a d)^3 g^4 n (a + b x)^2 \left(12 A + 7 B n + 12 B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{60 b d^3} + \\ & \frac{B (b c - a d)^4 g^4 n (a + b x) \left(12 A + 13 B n + 12 B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{30 b d^4} + \\ & \frac{B (b c - a d)^5 g^4 n \left(12 A + 25 B n + 12 B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right) \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right]}{30 b d^5} + \\ & \frac{2 B^2 (b c - a d)^5 g^4 n^2 \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{5 b d^5} \end{aligned}$$

Result (type 4, 3194 leaves):

$$\begin{aligned} & g^4 \left(- \frac{8 a^5 B^2 n^2}{5 b} + \frac{2 b^4 B^2 c^5 n^2}{5 d^5} - \frac{12 a b^3 B^2 c^4 n^2}{5 d^4} + \frac{6 a^2 b^2 B^2 c^3 n^2}{d^3} - \frac{8 a^3 b B^2 c^2 n^2}{d^2} + \frac{28 a^4 B^2 c n^2}{5 d} + \right. \\ & a^4 A^2 x + \frac{8}{5} a^4 A B n x + \frac{2 A b^4 B c^4 n x}{5 d^4} - \frac{2 a A b^3 B c^3 n x}{d^3} + \frac{4 a^2 A b^2 B c^2 n x}{d^2} - \frac{4 a^3 A b B c n x}{d} + \\ & \frac{23}{30} a^4 B^2 n^2 x + \frac{13 b^4 B^2 c^4 n^2 x}{30 d^4} - \frac{59 a b^3 B^2 c^3 n^2 x}{30 d^3} + \frac{17 a^2 b^2 B^2 c^2 n^2 x}{5 d^2} - \frac{79 a^3 b B^2 c n^2 x}{30 d} + \\ & 2 a^3 A^2 b x^2 + \frac{6}{5} a^3 A b B n x^2 - \frac{A b^4 B c^3 n x^2}{5 d^3} + \frac{a A b^3 B c^2 n x^2}{d^2} - \frac{2 a^2 A b^2 B c n x^2}{d} + \\ & \frac{13}{60} a^3 b B^2 n^2 x^2 - \frac{7 b^4 B^2 c^3 n^2 x^2}{60 d^3} + \frac{9 a b^3 B^2 c^2 n^2 x^2}{20 d^2} - \frac{11 a^2 b^2 B^2 c n^2 x^2}{20 d} + 2 a^2 A^2 b^2 x^3 + \\ & \left. \frac{8}{15} a^2 A b^2 B n x^3 + \frac{2 A b^4 B c^2 n x^3}{15 d^2} - \frac{2 a A b^3 B c n x^3}{3 d} + \frac{1}{30} a^2 b^2 B^2 n^2 x^3 + \frac{b^4 B^2 c^2 n^2 x^3}{30 d^2} - \right) \end{aligned}$$

$$\begin{aligned}
 & \frac{a b^3 B^2 c n^2 x^3}{15 d} + a A^2 b^3 x^4 + \frac{1}{10} a A b^3 B n x^4 - \frac{A b^4 B c n x^4}{10 d} + \frac{1}{5} A^2 b^4 x^5 + \frac{8 a^5 B^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]}{5 b} + \\
 & \frac{2 a b^3 B^2 c^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]}{5 d^4} - \frac{2 a^2 b^2 B^2 c^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]}{d^3} + \frac{4 a^3 b B^2 c^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]}{d^2} - \\
 & \frac{4 a^4 B^2 c n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]}{d} + \frac{a^5 B^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2}{5 b} - \frac{2 b^4 B^2 c^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]}{5 d^5} + \frac{2 a b^3 B^2 c^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]}{d^4} - \\
 & \frac{4 a^2 b^2 B^2 c^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]}{d^3} + \frac{4 a^3 b B^2 c^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]}{d^2} - \frac{8 a^4 B^2 c n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]}{5 d} + \\
 & \frac{b^4 B^2 c^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2}{5 d^5} - \frac{a b^3 B^2 c^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2}{d^4} + \frac{2 a^2 b^2 B^2 c^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2}{d^3} - \\
 & \frac{2 a^3 b B^2 c^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2}{d^2} + \frac{a^4 B^2 c n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2}{d} + \frac{2 a^5 A B n \operatorname{Log}[a + b x]}{5 b} - \\
 & \frac{23 a^5 B^2 n^2 \operatorname{Log}[a + b x]}{30 b} + \frac{a^2 b^2 B^2 c^3 n^2 \operatorname{Log}[a + b x]}{5 d^3} - \frac{13 a^3 b B^2 c^2 n^2 \operatorname{Log}[a + b x]}{15 d^2} + \\
 & \frac{43 a^4 B^2 c n^2 \operatorname{Log}[a + b x]}{30 d} - \frac{2 a^5 B^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x]}{5 b} + \frac{2 a^5 B^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x]}{5 b} - \\
 & \frac{2 a^5 B^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]}{5 b} + 2 a^4 A B x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \frac{8}{5} a^4 B^2 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & \frac{2 b^4 B^2 c^4 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]}{5 d^4} - \frac{2 a b^3 B^2 c^3 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]}{d^3} + \frac{4 a^2 b^2 B^2 c^2 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]}{d^2} - \\
 & \frac{4 a^3 b B^2 c n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]}{d} + 4 a^3 A b B x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \frac{6}{5} a^3 b B^2 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - \\
 & \frac{b^4 B^2 c^3 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]}{5 d^3} + \frac{a b^3 B^2 c^2 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]}{d^2} - \frac{2 a^2 b^2 B^2 c n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]}{d} + \\
 & 4 a^2 A b^2 B x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \frac{8}{15} a^2 b^2 B^2 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & \frac{2 b^4 B^2 c^2 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]}{15 d^2} - \frac{2 a b^3 B^2 c n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]}{3 d} + 2 a A b^3 B x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & \frac{1}{10} a b^3 B^2 n x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - \frac{b^4 B^2 c n x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]}{10 d} + \frac{2}{5} A b^4 B x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & \frac{2 a^5 B^2 n \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]}{5 b} + a^4 B^2 x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 2 a^3 b B^2 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 & 2 a^2 b^2 B^2 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + a b^3 B^2 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \frac{1}{5} b^4 B^2 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 - \\
 & \frac{2 A b^4 B c^5 n \operatorname{Log}[c + d x]}{5 d^5} + \frac{2 a A b^3 B c^4 n \operatorname{Log}[c + d x]}{d^4} - \frac{4 a^2 A b^2 B c^3 n \operatorname{Log}[c + d x]}{d^3} + \\
 & \frac{4 a^3 A b B c^2 n \operatorname{Log}[c + d x]}{d^2} - \frac{2 a^4 A B c n \operatorname{Log}[c + d x]}{d} - \frac{13 b^4 B^2 c^5 n^2 \operatorname{Log}[c + d x]}{30 d^5} +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{53 a b^3 B^2 c^4 n^2 \operatorname{Log}[c+d x]}{30 d^4} - \frac{38 a^2 b^2 B^2 c^3 n^2 \operatorname{Log}[c+d x]}{15 d^3} + \frac{6 a^3 b B^2 c^2 n^2 \operatorname{Log}[c+d x]}{5 d^2} + \\
 & \frac{2 b^4 B^2 c^5 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]}{5 d^5} - \frac{2 a b^3 B^2 c^4 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]}{d^4} + \\
 & \frac{4 a^2 b^2 B^2 c^3 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]}{d^3} - \frac{4 a^3 b B^2 c^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]}{d^2} + \\
 & \frac{2 a^4 B^2 c n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]}{d} - \frac{2 b^4 B^2 c^5 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]}{5 d^5} + \\
 & \frac{2 a b^3 B^2 c^4 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]}{d^4} - \frac{4 a^2 b^2 B^2 c^3 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]}{d^3} + \\
 & \frac{4 a^3 b B^2 c^2 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]}{d^2} - \frac{2 a^4 B^2 c n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]}{d} - \\
 & \frac{2 b^4 B^2 c^5 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x]}{5 d^5} + \frac{2 a b^3 B^2 c^4 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x]}{d^4} - \\
 & \frac{4 a^2 b^2 B^2 c^3 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x]}{d^3} + \frac{4 a^3 b B^2 c^2 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x]}{d^2} - \\
 & \frac{2 a^4 B^2 c n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x]}{d} - \frac{2 b^4 B^2 c^5 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{5 d^5} + \\
 & \frac{2 a b^3 B^2 c^4 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^4} - \frac{4 a^2 b^2 B^2 c^3 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^3} + \\
 & \frac{4 a^3 b B^2 c^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^2} - \frac{2 a^4 B^2 c n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d} - \\
 & \frac{2 B^2 c\left(b^4 c^4-5 a b^3 c^3 d+10 a^2 b^2 c^2 d^2-10 a^3 b c d^3+5 a^4 d^4\right) n^2 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]}{5 d^5} \\
 & \left. \frac{2 a^5 B^2 n^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]}{5 b}\right)
 \end{aligned}$$

Problem 11: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^3 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 335 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{B (b c - a d) g^3 n (a + b x)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{6 b d} + \frac{g^3 (a + b x)^4 \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)^2}{4 b} + \\
 & \frac{B (b c - a d)^2 g^3 n (a + b x)^2 \left(3 A + B n + 3 B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{12 b d^2} - \\
 & \frac{B (b c - a d)^3 g^3 n (a + b x) \left(6 A + 5 B n + 6 B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{12 b d^3} - \\
 & \frac{B (b c - a d)^4 g^3 n \left(6 A + 11 B n + 6 B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right) \operatorname{Log} \left[\frac{b c - a d}{b (c+d x)} \right]}{12 b d^4} - \\
 & \frac{B^2 (b c - a d)^4 g^3 n^2 \operatorname{PolyLog} \left[2, \frac{d (a+b x)}{b (c+d x)} \right]}{2 b d^4}
 \end{aligned}$$

Result (type 4, 2348 leaves):

$$\begin{aligned}
 & \frac{1}{12 b d^4} \\
 & g^3 \left(-6 b^4 B^2 c^4 n^2 + 30 a b^3 B^2 c^3 d n^2 - 60 a^2 b^2 B^2 c^2 d^2 n^2 + 54 a^3 b B^2 c d^3 n^2 - 18 a^4 B^2 d^4 n^2 + 12 a^3 A^2 b d^4 \right. \\
 & \quad x - 6 A b^4 B c^3 d n x + 24 a A b^3 B c^2 d^2 n x - 36 a^2 A b^2 B c d^3 n x + 18 a^3 A b B d^4 n x - 5 b^4 B^2 c^3 d n^2 x + \\
 & \quad 17 a b^3 B^2 c^2 d^2 n^2 x - 19 a^2 b^2 B^2 c d^3 n^2 x + 7 a^3 b B^2 d^4 n^2 x + 18 a^2 A^2 b^2 d^4 x^2 + 3 A b^4 B c^2 d^2 n x^2 - \\
 & \quad 12 a A b^3 B c d^3 n x^2 + 9 a^2 A b^2 B d^4 n x^2 + b^4 B^2 c^2 d^2 n^2 x^2 - 2 a b^3 B^2 c d^3 n^2 x^2 + a^2 b^2 B^2 d^4 n^2 x^2 + \\
 & \quad 12 a A^2 b^3 d^4 x^3 - 2 A b^4 B c d^3 n x^3 + 2 a A b^3 B d^4 n x^3 + 3 A^2 b^4 d^4 x^4 - 6 a b^3 B^2 c^3 d n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \\
 & \quad 24 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] - 36 a^3 b B^2 c d^3 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] + 18 a^4 B^2 d^4 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \\
 & \quad 3 a^4 B^2 d^4 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 6 b^4 B^2 c^4 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] - 24 a b^3 B^2 c^3 d n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] + \\
 & \quad 36 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] - 18 a^3 b B^2 c d^3 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] - 3 b^4 B^2 c^4 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + \\
 & \quad 12 a b^3 B^2 c^3 d n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 18 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 12 a^3 b B^2 c d^3 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + \\
 & \quad 6 a^4 A B d^4 n \operatorname{Log} [a + b x] - 3 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log} [a + b x] + 10 a^3 b B^2 c d^3 n^2 \operatorname{Log} [a + b x] - \\
 & \quad 7 a^4 B^2 d^4 n^2 \operatorname{Log} [a + b x] - 6 a^4 B^2 d^4 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + b x] + \\
 & \quad 6 a^4 B^2 d^4 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + b x] - 6 a^4 B^2 d^4 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \\
 & \quad 24 a^3 A b B d^4 x \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - 6 b^4 B^2 c^3 d n x \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + \\
 & \quad 24 a b^3 B^2 c^2 d^2 n x \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - 36 a^2 b^2 B^2 c d^3 n x \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + \\
 & \quad 18 a^3 b B^2 d^4 n x \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + 36 a^2 A b^2 B d^4 x^2 \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + \\
 & \quad 3 b^4 B^2 c^2 d^2 n x^2 \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - 12 a b^3 B^2 c d^3 n x^2 \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + \\
 & \quad 9 a^2 b^2 B^2 d^4 n x^2 \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + 24 a A b^3 B d^4 x^3 \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] -
 \end{aligned}$$

$$\begin{aligned}
 & 2 b^4 B^2 c d^3 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 2 a b^3 B^2 d^4 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 6 A b^4 B d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 6 a^4 B^2 d^4 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 12 a^3 b B^2 d^4 x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 18 a^2 b^2 B^2 d^4 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 & 12 a b^3 B^2 d^4 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 3 b^4 B^2 d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 6 A b^4 B c^4 n \operatorname{Log}[c+d x] - \\
 & 24 a A b^3 B c^3 d n \operatorname{Log}[c+d x] + 36 a^2 A b^2 B c^2 d^2 n \operatorname{Log}[c+d x] - 24 a^3 A b B c d^3 n \operatorname{Log}[c+d x] + \\
 & 5 b^4 B^2 c^4 n^2 \operatorname{Log}[c+d x] - 14 a b^3 B^2 c^3 d n^2 \operatorname{Log}[c+d x] + 9 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}[c+d x] - \\
 & 6 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + 24 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] - \\
 & 36 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + 24 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + \\
 & 6 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - 24 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] + \\
 & 36 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - 24 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] + \\
 & 6 b^4 B^2 c^4 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] - 24 a b^3 B^2 c^3 d n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] + \\
 & 36 a^2 b^2 B^2 c^2 d^2 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] - 24 a^3 b B^2 c d^3 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] + \\
 & 6 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 24 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 & 36 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 24 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 & 6 b B^2 c \left(b^3 c^3 - 4 a b^2 c^2 d + 6 a^2 b c d^2 - 4 a^3 d^3\right) n^2 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] - \\
 & 6 a^4 B^2 d^4 n^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]
 \end{aligned}$$

Problem 12: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^2 \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2 dx$$

Optimal (type 4, 274 leaves, 6 steps):

$$\begin{aligned}
 & - \frac{B (b c - a d) g^2 n (a + b x)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{3 b d} + \frac{g^2 (a + b x)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)^2}{3 b} + \\
 & \frac{B (b c - a d)^2 g^2 n (a + b x) \left(2 A + B n + 2 B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{3 b d^2} + \\
 & \frac{B (b c - a d)^3 g^2 n \left(2 A + 3 B n + 2 B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right) \operatorname{Log} \left[\frac{-b c - a d}{b (c+d x)} \right]}{3 b d^3} + \\
 & \frac{2 B^2 (b c - a d)^3 g^2 n^2 \operatorname{PolyLog} \left[2, \frac{d (a+b x)}{b (c+d x)} \right]}{3 b d^3}
 \end{aligned}$$

Result (type 4, 1589 leaves):

$$\begin{aligned}
 & g^2 \left(a^2 x \left(A + B \left(\operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right) \right)^2 + \\
 & a b x^2 \left(A + B \left(\operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right) \right)^2 + \\
 & \frac{1}{3} b^2 x^3 \left(A + B \left(\operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right) \right)^2 + \\
 & 2 a^2 B n \left(A + B \left(\operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right) \right) \\
 & \left(x \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] + \frac{(b c - a d) (a d \operatorname{Log} [a+b x] - b c \operatorname{Log} [c+d x])}{b^2 c d - a b d^2} \right) + \\
 & 2 b^2 B n \left(A + B \left(\operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right) \right) \left(\frac{1}{3} x^3 \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] - \frac{1}{6 b^3 d^3} \right. \\
 & \left. (b d (b c - a d) x (-2 b c - 2 a d + b d x) - 2 a^3 d^3 \operatorname{Log} [a+b x] + 2 b^3 c^3 \operatorname{Log} [c+d x]) \right) + \\
 & 4 a b B n \left(A + B \left(\operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right) \right) \\
 & \left(\frac{1}{2} x^2 \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] - \frac{1}{2} (b c - a d) \left(\frac{x}{b d} + \frac{a^2 \operatorname{Log} [a+b x]}{b^2 (b c - a d)} - \frac{c^2 \operatorname{Log} [c+d x]}{d^2 (b c - a d)} \right) \right) + \\
 & a^2 B^2 n^2 \left(x \operatorname{Log} \left[\frac{a+b x}{c+d x} \right]^2 - \frac{1}{b d} \left(-a d \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - b c \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 2 a d \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a+b x] - \right. \right. \\
 & \left. \left. 2 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a+b x] + 2 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a+b x)}{-b c + a d} \right] - \right. \right. \\
 & \left. \left. 2 a d \operatorname{Log} [a+b x] \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] - 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [c+d x] + 2 b c \operatorname{Log} \left[\frac{c}{d} + x \right] \right. \right. \\
 & \left. \left. \operatorname{Log} [c+d x] + 2 b c \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \operatorname{Log} [c+d x] + 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c+d x)}{b c - a d} \right] \right) + \\
 & \left. 2 b c \operatorname{PolyLog} \left[2, \frac{d (a+b x)}{-b c + a d} \right] + 2 a d \operatorname{PolyLog} \left[2, \frac{b (c+d x)}{b c - a d} \right] \right) + 2 a b B^2 n^2 \\
 & \left(\frac{1}{2} x^2 \operatorname{Log} \left[\frac{a+b x}{c+d x} \right]^2 - \frac{1}{2 b^2 d^2} \left(-2 d (-b c + a d) (a+b x) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) + a^2 d^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - \right. \right. \\
 & \left. \left. 2 b (b c - a d) (c+d x) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) + b^2 c^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] \right) - \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left(\text{Log}\left[\frac{a+b x}{c+d x}\right] \right) \left(a^2 d^2 \text{Log}[a+b x] - b (d (-b c+a d) x + b c^2 \text{Log}[c+d x]) \right) \right) - \\
 & 2 b^2 c^2 \left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) - \\
 & 2 a^2 d^2 \left(\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) \left. \right) + \\
 & b^2 B^2 n^2 \left(\frac{1}{3} x^3 \text{Log}\left[\frac{a+b x}{c+d x}\right]^2 - \frac{1}{6 b^3 d^3} \left(4 d (-b c+a d) (b c+a d) (a+b x) \left(-1 + \text{Log}\left[\frac{a}{b} + x\right]\right) \right) - \right. \\
 & \left. 2 a^3 d^3 \text{Log}\left[\frac{a}{b} + x\right]^2 + 4 b (b c-a d) (b c+a d) (c+d x) \left(-1 + \text{Log}\left[\frac{c}{d} + x\right]\right) - \right. \\
 & \left. 2 b^3 c^3 \text{Log}\left[\frac{c}{d} + x\right]^2 + d^2 (b c-a d) \left(b x (2 a-b x) + 2 b^2 x^2 \text{Log}\left[\frac{a}{b} + x\right] - 2 a^2 \text{Log}[a+b x]\right) \right) + \\
 & b^2 (b c-a d) \left(d x (-2 c+d x) - 2 d^2 x^2 \text{Log}\left[\frac{c}{d} + x\right] + 2 c^2 \text{Log}[c+d x] \right) - \\
 & 2 \left(\text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{a+b x}{c+d x}\right] \right) \\
 & \left(b d (b c-a d) x (-2 b c-2 a d+b d x) - 2 a^3 d^3 \text{Log}[a+b x] + 2 b^3 c^3 \text{Log}[c+d x] \right) + \\
 & 4 b^3 c^3 \left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) + \\
 & \left. 4 a^3 d^3 \left(\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) \right) \left. \right)
 \end{aligned}$$

Problem 13: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x) \left(A + B \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \right)^2 dx$$

Optimal (type 4, 196 leaves, 5 steps):

$$\begin{aligned}
 & - \frac{B (b c-a d) g n (a+b x) \left(A + B \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \right)}{b d} + \frac{g (a+b x)^2 \left(A + B \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \right)^2}{2 b} - \\
 & \frac{B (b c-a d)^2 g n \left(A + B n + B \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \right) \text{Log}\left[\frac{b c-a d}{b (c+d x)}\right]}{b d^2} - \frac{B^2 (b c-a d)^2 g n^2 \text{PolyLog}\left[2, \frac{d(a+b x)}{b (c+d x)}\right]}{b d^2}
 \end{aligned}$$

Result (type 4, 911 leaves):

$$g \left(-\frac{a^2 B^2 n^2}{b} - \frac{b B^2 c^2 n^2}{d^2} + \frac{2 a B^2 c n^2}{d} + a A^2 x + a A B n x - \frac{A b B c n x}{d} + \right. \\ \frac{1}{2} A^2 b x^2 + \frac{a^2 B^2 n^2 \text{Log}\left[\frac{a}{b} + x\right]}{b} - \frac{a B^2 c n^2 \text{Log}\left[\frac{a}{b} + x\right]}{d} + \frac{a^2 B^2 n^2 \text{Log}\left[\frac{a}{b} + x\right]^2}{2 b} + \\ \frac{b B^2 c^2 n^2 \text{Log}\left[\frac{c}{d} + x\right]}{d^2} - \frac{a B^2 c n^2 \text{Log}\left[\frac{c}{d} + x\right]}{d} - \frac{b B^2 c^2 n^2 \text{Log}\left[\frac{c}{d} + x\right]^2}{2 d^2} + \frac{a B^2 c n^2 \text{Log}\left[\frac{c}{d} + x\right]^2}{d} + \\ \frac{a^2 A B n \text{Log}[a + b x]}{b} - \frac{a^2 B^2 n^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x]}{b} + \frac{a^2 B^2 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x]}{b} - \\ \frac{a^2 B^2 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]}{b} + 2 a A B x \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + a B^2 n x \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - \\ \frac{b B^2 c n x \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]}{d} + A b B x^2 \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \frac{a^2 B^2 n \text{Log}[a + b x] \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]}{b} + \\ a B^2 x \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \frac{1}{2} b B^2 x^2 \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \frac{A b B c^2 n \text{Log}[c + d x]}{d^2} - \\ \frac{2 a A B c n \text{Log}[c + d x]}{d} - \frac{b B^2 c^2 n^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[c + d x]}{d^2} + \frac{2 a B^2 c n^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[c + d x]}{d} + \\ \frac{b B^2 c^2 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[c + d x]}{d^2} - \frac{2 a B^2 c n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[c + d x]}{d} + \\ \frac{b B^2 c^2 n \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \text{Log}[c + d x]}{d^2} - \frac{2 a B^2 c n \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \text{Log}[c + d x]}{d} + \\ \frac{b B^2 c^2 n^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^2} - \frac{2 a B^2 c n^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d} + \\ \left. \frac{B^2 c (b c - 2 a d) n^2 \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]}{d^2} - \frac{a^2 B^2 n^2 \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]}{b} \right)$$

Problem 14: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{a g + b g x} dx$$

Optimal (type 4, 138 leaves, 4 steps):

$$-\frac{\left(A + B \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2 \text{Log}\left[1 - \frac{b(c+d x)}{d(a+b x)}\right]}{b g} + \\ \frac{2 B n \left(A + B \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right) \text{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]}{b g} + \frac{2 B^2 n^2 \text{PolyLog}\left[3, \frac{b(c+d x)}{d(a+b x)}\right]}{b g}$$

Result (type 4, 537 leaves):

$$\begin{aligned}
 & \frac{1}{3 b g} \left(3 \operatorname{Log}[a+b x] \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log}\left[\frac{a+b x}{c+d x} \right] \right)^2 + \right. \\
 & \quad 3 B n \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log}\left[\frac{a+b x}{c+d x} \right] \right) \\
 & \quad \left(\operatorname{Log}\left[\frac{a}{b}+x \right]^2 - 2 \operatorname{Log}[a+b x] \left(\operatorname{Log}\left[\frac{a}{b}+x \right] - \operatorname{Log}\left[\frac{c}{d}+x \right] - \operatorname{Log}\left[\frac{a+b x}{c+d x} \right] \right) - \right. \\
 & \quad \left. 2 \left(\operatorname{Log}\left[\frac{c}{d}+x \right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d} \right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d} \right] \right) \right) + B^2 n^2 \left(\operatorname{Log}\left[\frac{a}{b}+x \right]^3 + \right. \\
 & \quad \left. 3 \operatorname{Log}\left[\frac{c}{d}+x \right]^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d} \right] + 3 \operatorname{Log}[a+b x] \left(-\operatorname{Log}\left[\frac{a}{b}+x \right] + \operatorname{Log}\left[\frac{c}{d}+x \right] + \operatorname{Log}\left[\frac{a+b x}{c+d x} \right] \right) \right)^2 + \\
 & \quad 3 \operatorname{Log}\left[\frac{a}{b}+x \right]^2 \left(-\operatorname{Log}\left[\frac{c}{d}+x \right] + \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d} \right] \right) + 6 \operatorname{Log}\left[\frac{a}{b}+x \right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d} \right] + \\
 & \quad 6 \operatorname{Log}\left[\frac{c}{d}+x \right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d} \right] - 3 \left(\operatorname{Log}\left[\frac{a}{b}+x \right] - \operatorname{Log}\left[\frac{c}{d}+x \right] - \operatorname{Log}\left[\frac{a+b x}{c+d x} \right] \right) \\
 & \quad \left(\operatorname{Log}\left[\frac{a}{b}+x \right]^2 - 2 \left(\operatorname{Log}\left[\frac{c}{d}+x \right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d} \right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d} \right] \right) \right) - \\
 & \quad \left. 6 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d} \right] - 6 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d} \right] \right) \Bigg)
 \end{aligned}$$

Problem 15: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x} \right)^n \right] \right)^2}{(a g+b g x)^2} dx$$

Optimal (type 3, 136 leaves, 3 steps):

$$-\frac{2 B^2 n^2 (c+d x)}{(b c-a d) g^2 (a+b x)} - \frac{2 B n (c+d x) \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{(b c-a d) g^2 (a+b x)} - \frac{(c+d x) \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x} \right)^n \right] \right)^2}{(b c-a d) g^2 (a+b x)}$$

Result (type 3, 389 leaves):

$$\begin{aligned}
 & \frac{1}{b (b c-a d) g^2 (a+b x)} \\
 & \left(-A^2 b c+a A^2 d-2 A b B c n+2 a A B d n-2 b B^2 c n^2+2 a B^2 d n^2+B^2 (-b c+a d) \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x} \right)^n \right]^2 - \right. \\
 & \quad a B^2 d n^2 \operatorname{Log}\left[\frac{a+b x}{c+d x} \right]^2 - b B^2 d n^2 x \operatorname{Log}\left[\frac{a+b x}{c+d x} \right]^2 - 2 B d n (a+b x) \operatorname{Log}[a+b x] \\
 & \quad \left(A+B n+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log}\left[\frac{a+b x}{c+d x} \right] \right) + 2 a A B d n \operatorname{Log}[c+d x] + \\
 & \quad 2 a B^2 d n^2 \operatorname{Log}[c+d x] + 2 A b B d n x \operatorname{Log}[c+d x] + 2 b B^2 d n^2 x \operatorname{Log}[c+d x] - \\
 & \quad 2 a B^2 d n^2 \operatorname{Log}\left[\frac{a+b x}{c+d x} \right] \operatorname{Log}[c+d x] - 2 b B^2 d n^2 x \operatorname{Log}\left[\frac{a+b x}{c+d x} \right] \operatorname{Log}[c+d x] + \\
 & \quad \left. 2 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x} \right)^n \right] \left(-(b c-a d) (A+B n)+B d n (a+b x) \operatorname{Log}[c+d x] \right) \right)
 \end{aligned}$$

Problem 38: Result more than twice size of optimal antiderivative.

$$\int (c g + d g x)^4 \left(A + B \text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 544 leaves, 19 steps):

$$\begin{aligned} & \frac{13 B^2 (b c - a d)^4 g^4 n^2 x}{30 b^4} + \frac{7 B^2 (b c - a d)^3 g^4 n^2 (c + d x)^2}{60 b^3 d} + \\ & \frac{B^2 (b c - a d)^2 g^4 n^2 (c + d x)^3}{30 b^2 d} - \frac{2 B (b c - a d)^4 g^4 n (a + b x) \left(A + B \text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{5 b^5} - \\ & \frac{B (b c - a d)^3 g^4 n (c + d x)^2 \left(A + B \text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{5 b^3 d} - \\ & \frac{2 B (b c - a d)^2 g^4 n (c + d x)^3 \left(A + B \text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{15 b^2 d} - \\ & \frac{B (b c - a d) g^4 n (c + d x)^4 \left(A + B \text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{10 b d} + \frac{g^4 (c + d x)^5 \left(A + B \text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{5 d} + \\ & \frac{13 B^2 (b c - a d)^5 g^4 n^2 \text{Log} \left[\frac{a + b x}{c + d x} \right]}{30 b^5 d} + \frac{5 B^2 (b c - a d)^5 g^4 n^2 \text{Log} [c + d x]}{6 b^5 d} + \\ & \frac{2 B (b c - a d)^5 g^4 n \left(A + B \text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right) \text{Log} \left[1 - \frac{b (c + d x)}{d (a + b x)} \right]}{5 b^5 d} - \\ & \frac{2 B^2 (b c - a d)^5 g^4 n^2 \text{PolyLog} \left[2, \frac{b (c + d x)}{d (a + b x)} \right]}{5 b^5 d} \end{aligned}$$

Result (type 4, 3163 leaves):

$$\begin{aligned} & \frac{1}{60 b^5 d} \\ & g^4 \left(-96 b^5 B^2 c^5 n^2 + 336 a b^4 B^2 c^4 d n^2 - 480 a^2 b^3 B^2 c^3 d^2 n^2 + 360 a^3 b^2 B^2 c^2 d^3 n^2 - 144 a^4 b B^2 c d^4 n^2 + \right. \\ & 24 a^5 B^2 d^5 n^2 + 60 A^2 b^5 c^4 d x - 96 A b^5 B c^4 d n x + 240 a A b^4 B c^3 d^2 n x - 240 a^2 A b^3 B c^2 d^3 n x + \\ & 120 a^3 A b^2 B c d^4 n x - 24 a^4 A b B d^5 n x + 46 b^5 B^2 c^4 d n^2 x - 158 a b^4 B^2 c^3 d^2 n^2 x + \\ & 204 a^2 b^3 B^2 c^2 d^3 n^2 x - 118 a^3 b^2 B^2 c d^4 n^2 x + 26 a^4 b B^2 d^5 n^2 x + 120 A^2 b^5 c^3 d^2 x^2 - \\ & 72 A b^5 B c^3 d^2 n x^2 + 120 a A b^4 B c^2 d^3 n x^2 - 60 a^2 A b^3 B c d^4 n x^2 + 12 a^3 A b^2 B d^5 n x^2 + \\ & 13 b^5 B^2 c^3 d^2 n^2 x^2 - 33 a b^4 B^2 c^2 d^3 n^2 x^2 + 27 a^2 b^3 B^2 c d^4 n^2 x^2 - 7 a^3 b^2 B^2 d^5 n^2 x^2 + \\ & 120 A^2 b^5 c^2 d^3 x^3 - 32 A b^5 B c^2 d^3 n x^3 + 40 a A b^4 B c d^4 n x^3 - 8 a^2 A b^3 B d^5 n x^3 + \\ & 2 b^5 B^2 c^2 d^3 n^2 x^3 - 4 a b^4 B^2 c d^4 n^2 x^3 + 2 a^2 b^3 B^2 d^5 n^2 x^3 + 60 A^2 b^5 c d^4 x^4 - \\ & 6 A b^5 B c d^4 n x^4 + 6 a A b^4 B d^5 n x^4 + 12 A^2 b^5 d^5 x^5 - 96 a b^4 B^2 c^4 d n^2 \text{Log} \left[\frac{a}{b} + x \right] + \\ & 240 a^2 b^3 B^2 c^3 d^2 n^2 \text{Log} \left[\frac{a}{b} + x \right] - 240 a^3 b^2 B^2 c^2 d^3 n^2 \text{Log} \left[\frac{a}{b} + x \right] + 120 a^4 b B^2 c d^4 n^2 \text{Log} \left[\frac{a}{b} + x \right] - \\ & 24 a^5 B^2 d^5 n^2 \text{Log} \left[\frac{a}{b} + x \right] + 60 a b^4 B^2 c^4 d n^2 \text{Log} \left[\frac{a}{b} + x \right]^2 - 120 a^2 b^3 B^2 c^3 d^2 n^2 \text{Log} \left[\frac{a}{b} + x \right]^2 + \\ & 120 a^3 b^2 B^2 c^2 d^3 n^2 \text{Log} \left[\frac{a}{b} + x \right]^2 - 60 a^4 b B^2 c d^4 n^2 \text{Log} \left[\frac{a}{b} + x \right]^2 + 12 a^5 B^2 d^5 n^2 \text{Log} \left[\frac{a}{b} + x \right]^2 + \end{aligned}$$

$$\begin{aligned}
 & 96 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right]-240 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{c}{d}+x\right]+240 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right]- \\
 & 120 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right]+24 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right]+12 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2+ \\
 & 120 a A b^4 B c^4 d n \operatorname{Log}[a+b x]-240 a^2 A b^3 B c^3 d^2 n \operatorname{Log}[a+b x]+240 a^3 A b^2 B c^2 d^3 n \operatorname{Log}[a+b x]- \\
 & 120 a^4 A b B c d^4 n \operatorname{Log}[a+b x]+24 a^5 A B d^5 n \operatorname{Log}[a+b x]+72 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}[a+b x]- \\
 & 152 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}[a+b x]+106 a^4 b B^2 c d^4 n^2 \operatorname{Log}[a+b x]-26 a^5 B^2 d^5 n^2 \operatorname{Log}[a+b x]- \\
 & 120 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x]+240 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x]- \\
 & 240 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x]+120 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x]- \\
 & 24 a^5 B^2 d^5 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x]+120 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x]- \\
 & 240 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x]+240 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x]- \\
 & 120 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x]+24 a^5 B^2 d^5 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x]- \\
 & 120 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+240 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]- \\
 & 240 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+120 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]- \\
 & 24 a^5 B^2 d^5 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+120 A b^5 B c^4 d x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]- \\
 & 96 b^5 B^2 c^4 d n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+240 a b^4 B^2 c^3 d^2 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]- \\
 & 240 a^2 b^3 B^2 c^2 d^3 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+120 a^3 b^2 B^2 c d^4 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]- \\
 & 24 a^4 b B^2 d^5 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+240 A b^5 B c^3 d^2 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]- \\
 & 72 b^5 B^2 c^3 d^2 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+120 a b^4 B^2 c^2 d^3 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]- \\
 & 60 a^2 b^3 B^2 c d^4 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+12 a^3 b^2 B^2 d^5 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 240 A b^5 B c^2 d^3 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-32 b^5 B^2 c^2 d^3 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 40 a b^4 B^2 c d^4 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-8 a^2 b^3 B^2 d^5 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 120 A b^5 B c d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-6 b^5 B^2 c d^4 n x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 6 a b^4 B^2 d^5 n x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+24 A b^5 B d^5 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 120 a b^4 B^2 c^4 d n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-240 a^2 b^3 B^2 c^3 d^2 n \operatorname{Log}[a+b x] \\
 & \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+240 a^3 b^2 B^2 c^2 d^3 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]- \\
 & 120 a^4 b B^2 c d^4 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+24 a^5 B^2 d^5 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+
 \end{aligned}$$

$$\begin{aligned}
 & 60 b^5 B^2 c^4 d x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 120 b^5 B^2 c^3 d^2 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 & 120 b^5 B^2 c^2 d^3 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 60 b^5 B^2 c d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 & 12 b^5 B^2 d^5 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 - 24 A b^5 B c^5 n \operatorname{Log}[c+d x] - 46 b^5 B^2 c^5 n^2 \operatorname{Log}[c+d x] + \\
 & 86 a b^4 B^2 c^4 d n^2 \operatorname{Log}[c+d x] - 52 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}[c+d x] + \\
 & 12 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}[c+d x] + 24 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] - \\
 & 24 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - 24 b^5 B^2 c^5 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] - \\
 & 24 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 24 b^5 B^2 c^5 n^2 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] - \\
 & 24 a B^2 d\left(5 b^4 c^4 - 10 a b^3 c^3 d + 10 a^2 b^2 c^2 d^2 - 5 a^3 b c d^3 + a^4 d^4\right) n^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]
 \end{aligned}$$

Problem 39: Result more than twice size of optimal antiderivative.

$$\int (c g + d g x)^3 \left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 454 leaves, 15 steps):

$$\begin{aligned}
 & \frac{5 B^2 (b c - a d)^3 g^3 n^2 x}{12 b^3} + \frac{B^2 (b c - a d)^2 g^3 n^2 (c + d x)^2}{12 b^2 d} - \\
 & \frac{B (b c - a d)^3 g^3 n (a + b x) \left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{2 b^4} - \\
 & \frac{B (b c - a d)^2 g^3 n (c + d x)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{4 b^2 d} - \\
 & \frac{B (b c - a d) g^3 n (c + d x)^3 \left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{6 b d} + \frac{g^3 (c + d x)^4 \left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)^2}{4 d} + \\
 & \frac{5 B^2 (b c - a d)^4 g^3 n^2 \operatorname{Log}\left[\frac{a+b x}{c+d x} \right]}{12 b^4 d} + \frac{11 B^2 (b c - a d)^4 g^3 n^2 \operatorname{Log}[c+d x]}{12 b^4 d} + \\
 & \frac{B (b c - a d)^4 g^3 n \left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right) \operatorname{Log}\left[1 - \frac{b(c+d x)}{d(a+b x)} \right]}{2 b^4 d} - \frac{B^2 (b c - a d)^4 g^3 n^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)} \right]}{2 b^4 d}
 \end{aligned}$$

Result (type 4, 2348 leaves):

$$\begin{aligned}
 & \frac{1}{12 b^4 d} \\
 & g^3 \left(-18 b^4 B^2 c^4 n^2 + 54 a b^3 B^2 c^3 d n^2 - 60 a^2 b^2 B^2 c^2 d^2 n^2 + 30 a^3 b B^2 c d^3 n^2 - 6 a^4 B^2 d^4 n^2 + 12 A^2 b^4 c^3 d \right. \\
 & \quad x - 18 A b^4 B c^3 d n x + 36 a A b^3 B c^2 d^2 n x - 24 a^2 A b^2 B c d^3 n x + 6 a^3 A b B d^4 n x + 7 b^4 B^2 c^3 d n^2 x - \\
 & \quad 19 a b^3 B^2 c^2 d^2 n^2 x + 17 a^2 b^2 B^2 c d^3 n^2 x - 5 a^3 b B^2 d^4 n^2 x + 18 A^2 b^4 c^2 d^2 x^2 - 9 A b^4 B c^2 d^2 n x^2 + \\
 & \quad \left. 12 a A b^3 B c d^3 n x^2 - 3 a^2 A b^2 B d^4 n x^2 + b^4 B^2 c^2 d^2 n^2 x^2 - 2 a b^3 B^2 c d^3 n^2 x^2 + a^2 b^2 B^2 d^4 n^2 x^2 + \right.
 \end{aligned}$$

$$\begin{aligned}
 & 12 A^2 b^4 c d^3 x^3 - 2 A b^4 B c d^3 n x^3 + 2 a A b^3 B d^4 n x^3 + 3 A^2 b^4 d^4 x^4 - 18 a b^3 B^2 c^3 d n^2 \text{Log}\left[\frac{a}{b} + x\right] + \\
 & 36 a^2 b^2 B^2 c^2 d^2 n^2 \text{Log}\left[\frac{a}{b} + x\right] - 24 a^3 b B^2 c d^3 n^2 \text{Log}\left[\frac{a}{b} + x\right] + 6 a^4 B^2 d^4 n^2 \text{Log}\left[\frac{a}{b} + x\right] + \\
 & 12 a b^3 B^2 c^3 d n^2 \text{Log}\left[\frac{a}{b} + x\right]^2 - 18 a^2 b^2 B^2 c^2 d^2 n^2 \text{Log}\left[\frac{a}{b} + x\right]^2 + 12 a^3 b B^2 c d^3 n^2 \text{Log}\left[\frac{a}{b} + x\right]^2 - \\
 & 3 a^4 B^2 d^4 n^2 \text{Log}\left[\frac{a}{b} + x\right]^2 + 18 b^4 B^2 c^4 n^2 \text{Log}\left[\frac{c}{d} + x\right] - 36 a b^3 B^2 c^3 d n^2 \text{Log}\left[\frac{c}{d} + x\right] + \\
 & 24 a^2 b^2 B^2 c^2 d^2 n^2 \text{Log}\left[\frac{c}{d} + x\right] - 6 a^3 b B^2 c d^3 n^2 \text{Log}\left[\frac{c}{d} + x\right] + 3 b^4 B^2 c^4 n^2 \text{Log}\left[\frac{c}{d} + x\right]^2 + \\
 & 24 a A b^3 B c^3 d n \text{Log}[a + b x] - 36 a^2 A b^2 B c^2 d^2 n \text{Log}[a + b x] + 24 a^3 A b B c d^3 n \text{Log}[a + b x] - \\
 & 6 a^4 A B d^4 n \text{Log}[a + b x] + 9 a^2 b^2 B^2 c^2 d^2 n^2 \text{Log}[a + b x] - 14 a^3 b B^2 c d^3 n^2 \text{Log}[a + b x] + \\
 & 5 a^4 B^2 d^4 n^2 \text{Log}[a + b x] - 24 a b^3 B^2 c^3 d n^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] + \\
 & 36 a^2 b^2 B^2 c^2 d^2 n^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] - 24 a^3 b B^2 c d^3 n^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] + \\
 & 6 a^4 B^2 d^4 n^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] + 24 a b^3 B^2 c^3 d n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] - \\
 & 36 a^2 b^2 B^2 c^2 d^2 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] + 24 a^3 b B^2 c d^3 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] - \\
 & 6 a^4 B^2 d^4 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] - 24 a b^3 B^2 c^3 d n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\
 & 36 a^2 b^2 B^2 c^2 d^2 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - 24 a^3 b B^2 c d^3 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\
 & 6 a^4 B^2 d^4 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 24 A b^4 B c^3 d x \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
 & 18 b^4 B^2 c^3 d n x \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 36 a b^3 B^2 c^2 d^2 n x \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
 & 24 a^2 b^2 B^2 c d^3 n x \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 6 a^3 b B^2 d^4 n x \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
 & 36 A b^4 B c^2 d^2 x^2 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 9 b^4 B^2 c^2 d^2 n x^2 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
 & 12 a b^3 B^2 c d^3 n x^2 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 3 a^2 b^2 B^2 d^4 n x^2 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
 & 24 A b^4 B c d^3 x^3 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 2 b^4 B^2 c d^3 n x^3 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
 & 2 a b^3 B^2 d^4 n x^3 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 6 A b^4 B d^4 x^4 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
 & 24 a b^3 B^2 c^3 d n \text{Log}[a + b x] \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 36 a^2 b^2 B^2 c^2 d^2 n \text{Log}[a + b x] \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
 & 24 a^3 b B^2 c d^3 n \text{Log}[a + b x] \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 6 a^4 B^2 d^4 n \text{Log}[a + b x] \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
 & 12 b^4 B^2 c^3 d x \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 18 b^4 B^2 c^2 d^2 x^2 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + \\
 & 12 b^4 B^2 c d^3 x^3 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 3 b^4 B^2 d^4 x^4 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - \\
 & 6 A b^4 B c^4 n \text{Log}[c + d x] - 7 b^4 B^2 c^4 n^2 \text{Log}[c + d x] + 10 a b^3 B^2 c^3 d n^2 \text{Log}[c + d x] -
 \end{aligned}$$

$$\begin{aligned}
 & 3 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}[c+d x]+6 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]- \\
 & 6 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]-6 b^4 B^2 c^4 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x]- \\
 & 6 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]-6 b^4 B^2 c^4 n^2 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]+ \\
 & 6 a B^2 d\left(-4 b^3 c^3+6 a b^2 c^2 d-4 a^2 b c d^2+a^3 d^3\right) n^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]
 \end{aligned}$$

Problem 40: Result more than twice size of optimal antiderivative.

$$\int (c g+d g x)^2\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2 d x$$

Optimal (type 4, 361 leaves, 11 steps):

$$\begin{aligned}
 & \frac{B^2(b c-a d)^2 g^2 n^2 x}{3 b^2}-\frac{2 B(b c-a d)^2 g^2 n(a+b x)\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{3 b^3}- \\
 & \frac{B(b c-a d) g^2 n(c+d x)^2\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{3 b d}+\frac{g^2(c+d x)^3\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{3 d}+ \\
 & \frac{B^2(b c-a d)^3 g^2 n^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]}{3 b^3 d}+\frac{B^2(b c-a d)^3 g^2 n^2 \operatorname{Log}[c+d x]}{b^3 d}+ \\
 & \frac{2 B(b c-a d)^3 g^2 n\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right) \operatorname{Log}\left[1-\frac{b(c+d x)}{d(a+b x)}\right]}{3 b^3 d}- \\
 & \frac{2 B^2(b c-a d)^3 g^2 n^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]}{3 b^3 d}
 \end{aligned}$$

Result (type 4, 1589 leaves):

$$\begin{aligned}
 & g^2\left(c^2 x\left(A+B\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right)^2+\right. \\
 & c d x^2\left(A+B\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right)^2+ \\
 & \frac{1}{3} d^2 x^3\left(A+B\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right)^2+ \\
 & 2 B c^2 n\left(A+B\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right) \\
 & \left.\left(x \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]+\frac{(b c-a d)(a d \operatorname{Log}[a+b x]-b c \operatorname{Log}[c+d x])}{b^2 c d-a b d^2}\right)\right)+ \\
 & 2 B d^2 n\left(A+B\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right)\left(\frac{1}{3} x^3 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]-\frac{1}{6 b^3 d^3}\right. \\
 & \left.\left(b d(b c-a d) x(-2 b c-2 a d+b d x)-2 a^3 d^3 \operatorname{Log}[a+b x]+2 b^3 c^3 \operatorname{Log}[c+d x]\right)\right)+ \\
 & 4 B c d n\left(A+B\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(\frac{1}{2} x^2 \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] - \frac{1}{2} (b c - a d) \left(\frac{x}{b d} + \frac{a^2 \operatorname{Log}[a+b x]}{b^2 (b c - a d)} - \frac{c^2 \operatorname{Log}[c+d x]}{d^2 (b c - a d)} \right) \right) + \\
 & B^2 c^2 n^2 \left(x \operatorname{Log} \left[\frac{a+b x}{c+d x} \right]^2 - \frac{1}{b d} \left(-a d \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - b c \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 2 a d \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log}[a+b x] - \right. \right. \\
 & \quad 2 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log}[a+b x] + 2 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(a+b x)}{-b c + a d} \right] - \\
 & \quad 2 a d \operatorname{Log}[a+b x] \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] - 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log}[c+d x] + 2 b c \operatorname{Log} \left[\frac{c}{d} + x \right] \\
 & \quad \operatorname{Log}[c+d x] + 2 b c \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \operatorname{Log}[c+d x] + 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(c+d x)}{b c - a d} \right] + \\
 & \quad \left. \left. 2 b c \operatorname{PolyLog} \left[2, \frac{d(a+b x)}{-b c + a d} \right] + 2 a d \operatorname{PolyLog} \left[2, \frac{b(c+d x)}{b c - a d} \right] \right) \right) + 2 B^2 c d n^2 \\
 & \left(\frac{1}{2} x^2 \operatorname{Log} \left[\frac{a+b x}{c+d x} \right]^2 - \frac{1}{2 b^2 d^2} \left(-2 d (-b c + a d) (a+b x) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) + a^2 d^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - \right. \right. \\
 & \quad 2 b (b c - a d) (c+d x) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) + b^2 c^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \right. \\
 & \quad \left. \left. \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right) \left(a^2 d^2 \operatorname{Log}[a+b x] - b (d (-b c + a d) x + b c^2 \operatorname{Log}[c+d x]) \right) \right) - \\
 & \quad 2 b^2 c^2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(c+d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d(a+b x)}{-b c + a d} \right] \right) - \\
 & \quad \left. \left. 2 a^2 d^2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(a+b x)}{-b c + a d} \right] + \operatorname{PolyLog} \left[2, \frac{b(c+d x)}{b c - a d} \right] \right) \right) \right) + \\
 & B^2 d^2 n^2 \left(\frac{1}{3} x^3 \operatorname{Log} \left[\frac{a+b x}{c+d x} \right]^2 - \frac{1}{6 b^3 d^3} \left(4 d (-b c + a d) (b c + a d) (a+b x) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) - \right. \right. \\
 & \quad 2 a^3 d^3 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 4 b (b c - a d) (b c + a d) (c+d x) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) - \\
 & \quad 2 b^3 c^3 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + d^2 (b c - a d) \left(b x (2 a - b x) + 2 b^2 x^2 \operatorname{Log} \left[\frac{a}{b} + x \right] - 2 a^2 \operatorname{Log}[a+b x] \right) + \\
 & \quad b^2 (b c - a d) \left(d x (-2 c + d x) - 2 d^2 x^2 \operatorname{Log} \left[\frac{c}{d} + x \right] + 2 c^2 \operatorname{Log}[c+d x] \right) - \\
 & \quad 2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right) \\
 & \quad \left. \left. (b d (b c - a d) x (-2 b c - 2 a d + b d x) - 2 a^3 d^3 \operatorname{Log}[a+b x] + 2 b^3 c^3 \operatorname{Log}[c+d x]) \right) + \right. \\
 & \quad 4 b^3 c^3 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(c+d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d(a+b x)}{-b c + a d} \right] \right) + \\
 & \quad \left. \left. 4 a^3 d^3 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(a+b x)}{-b c + a d} \right] + \operatorname{PolyLog} \left[2, \frac{b(c+d x)}{b c - a d} \right] \right) \right) \right) \right)
 \end{aligned}$$

Problem 41: Result more than twice size of optimal antiderivative.

$$\int (c g + d g x) \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 220 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{B (b c - a d) g n (a + b x) \left(A + B \text{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{b^2} + \\
 & \frac{g (c + d x)^2 \left(A + B \text{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)^2}{2 d} + \frac{B^2 (b c - a d)^2 g n^2 \text{Log}[c + d x]}{b^2 d} + \\
 & \frac{B (b c - a d)^2 g n \left(A + B \text{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right) \text{Log} \left[1 - \frac{b (c+d x)}{d (a+b x)} \right]}{b^2 d} - \frac{B^2 (b c - a d)^2 g n^2 \text{PolyLog} \left[2, \frac{b (c+d x)}{d (a+b x)} \right]}{b^2 d}
 \end{aligned}$$

Result (type 4, 941 leaves):

$$\begin{aligned}
 & \frac{1}{2 b^2 d} g \left(-2 b^2 B^2 c^2 n^2 + 4 a b B^2 c d n^2 - 2 a^2 B^2 d^2 n^2 + 2 A^2 b^2 c d x - 2 A b^2 B c d n x + 2 a A b B d^2 n x + \right. \\
 & A^2 b^2 d^2 x^2 - 2 a b B^2 c d n^2 \text{Log} \left[\frac{a}{b} + x \right] + 2 a^2 B^2 d^2 n^2 \text{Log} \left[\frac{a}{b} + x \right] + 2 a b B^2 c d n^2 \text{Log} \left[\frac{a}{b} + x \right]^2 - \\
 & a^2 B^2 d^2 n^2 \text{Log} \left[\frac{a}{b} + x \right]^2 + 2 b^2 B^2 c^2 n^2 \text{Log} \left[\frac{c}{d} + x \right] - 2 a b B^2 c d n^2 \text{Log} \left[\frac{c}{d} + x \right] + \\
 & b^2 B^2 c^2 n^2 \text{Log} \left[\frac{c}{d} + x \right]^2 + 4 a A b B c d n \text{Log}[a + b x] - 2 a^2 A B d^2 n \text{Log}[a + b x] - \\
 & 4 a b B^2 c d n^2 \text{Log} \left[\frac{a}{b} + x \right] \text{Log}[a + b x] + 2 a^2 B^2 d^2 n^2 \text{Log} \left[\frac{a}{b} + x \right] \text{Log}[a + b x] + \\
 & 4 a b B^2 c d n^2 \text{Log} \left[\frac{c}{d} + x \right] \text{Log}[a + b x] - 2 a^2 B^2 d^2 n^2 \text{Log} \left[\frac{c}{d} + x \right] \text{Log}[a + b x] - \\
 & 4 a b B^2 c d n^2 \text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + 2 a^2 B^2 d^2 n^2 \text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \\
 & 4 A b^2 B c d x \text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - 2 b^2 B^2 c d n x \text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + \\
 & 2 a b B^2 d^2 n x \text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + 2 A b^2 B d^2 x^2 \text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + \\
 & 4 a b B^2 c d n \text{Log}[a + b x] \text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - 2 a^2 B^2 d^2 n \text{Log}[a + b x] \text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + \\
 & 2 b^2 B^2 c d x \text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right]^2 + b^2 B^2 d^2 x^2 \text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right]^2 - 2 A b^2 B c^2 n \text{Log}[c + d x] + \\
 & 2 b^2 B^2 c^2 n^2 \text{Log} \left[\frac{a}{b} + x \right] \text{Log}[c + d x] - 2 b^2 B^2 c^2 n^2 \text{Log} \left[\frac{c}{d} + x \right] \text{Log}[c + d x] - \\
 & 2 b^2 B^2 c^2 n \text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \text{Log}[c + d x] - 2 b^2 B^2 c^2 n^2 \text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{b (c + d x)}{b c - a d} \right] - \\
 & \left. 2 b^2 B^2 c^2 n^2 \text{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] + 2 a B^2 d (-2 b c + a d) n^2 \text{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right)
 \end{aligned}$$

Problem 42: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \text{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)^2}{c g + d g x} dx$$

Optimal (type 4, 137 leaves, 4 steps):

$$\begin{aligned}
 & - \frac{\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2 \operatorname{Log}\left[\frac{b c-a d}{b(c+d x)}\right]}{d g} \\
 & \frac{2 B n\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{d g} + \frac{2 B^2 n^2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{b(c+d x)}\right]}{d g}
 \end{aligned}$$

Result (type 4, 537 leaves):

$$\begin{aligned}
 & \frac{1}{3 d g} \left(3 \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right)^2 \operatorname{Log}[c+d x] - \right. \\
 & \quad 3 B n \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right) \\
 & \quad \left(\operatorname{Log}\left[\frac{c}{d}+x\right]^2 + 2 \left(\operatorname{Log}\left[\frac{a}{b}+x\right] - \operatorname{Log}\left[\frac{c}{d}+x\right] - \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right) \operatorname{Log}[c+d x] - \right. \\
 & \quad \left. \left. 2 \left(\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) \right) \right) + \\
 & B^2 n^2 \left(\operatorname{Log}\left[\frac{c}{d}+x\right]^3 + 3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \right) + \right. \\
 & \quad 3 \left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right)^2 \operatorname{Log}[c+d x] + 3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 & \quad 6 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] + 3 \left(\operatorname{Log}\left[\frac{a}{b}+x\right] - \operatorname{Log}\left[\frac{c}{d}+x\right] - \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right) \\
 & \quad \left(\operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2 \left(\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) \right) + 6 \operatorname{Log}\left[\frac{c}{d}+x\right] \\
 & \quad \left. \left. \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] - 6 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] - 6 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right] \right) \right)
 \end{aligned}$$

Problem 43: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(c g+d g x)^2} d x$$

Optimal (type 3, 163 leaves, 4 steps):

$$\begin{aligned}
 & - \frac{2 A B n(a+b x)}{(b c-a d) g^2(c+d x)} + \frac{2 B^2 n^2(a+b x)}{(b c-a d) g^2(c+d x)} - \\
 & \frac{2 B^2 n(a+b x) \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]}{(b c-a d) g^2(c+d x)} + \frac{(a+b x)\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(b c-a d) g^2(c+d x)}
 \end{aligned}$$

Result (type 3, 391 leaves):

$$\frac{1}{d(-bc+ad)g^2(c+dx)} \left(A^2bc - aA^2d - 2AbBcn + 2aABdn + 2bB^2cn^2 - 2aB^2dn^2 + B^2(bc-ad) \log\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 - bB^2cn^2 \log\left[\frac{a+bx}{c+dx}\right]^2 - bB^2dn^2x \log\left[\frac{a+bx}{c+dx}\right]^2 + 2bBn(c+dx) \log[a+bx] \left(-A+Bn - B \log\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + Bn \log\left[\frac{a+bx}{c+dx}\right]\right) + 2AbBcn \log[c+dx] - 2bB^2cn^2 \log[c+dx] + 2aABdnx \log[c+dx] - 2bB^2dn^2x \log[c+dx] - 2bB^2cn^2 \log\left[\frac{a+bx}{c+dx}\right] \log[c+dx] - 2bB^2dn^2x \log\left[\frac{a+bx}{c+dx}\right] \log[c+dx] + 2B \log\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \left((bc-ad)(A-Bn) + bBn(c+dx) \log[c+dx]\right) \right)$$

Problem 67: Result more than twice size of optimal antiderivative.

$$\int (f+g x)^3 \left(A+B \log\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \right)^2 dx$$

Optimal (type 4, 923 leaves, 15 steps):

$$\frac{B^2(bc-ad)^3g^3n^2x}{6b^3d^3} + \frac{B^2(bc-ad)^2g^2(4bdf-3bcg-adg)n^2x}{4b^3d^3} + \frac{B^2(bc-ad)^2g^3n^2(c+dx)^2}{12b^2d^4} - \frac{1}{2b^4d^3}B(bc-ad)g(a^2d^2g^2-2abd g(2df-cg)+b^2(6d^2f^2-8cdfg+3c^2g^2))n(a+bx)\left(A+B \log\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right) - \frac{1}{4b^2d^4}B(bc-ad)g^2(4bdf-3bcg-adg)n(c+dx)^2\left(A+B \log\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right) - \frac{B(bc-ad)g^3n(c+dx)^3\left(A+B \log\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)}{6bd^4} - \frac{(bf-ag)^4\left(A+B \log\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{4b^4g} + \frac{(f+gx)^4\left(A+B \log\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{4g} - \frac{1}{2b^4d^4}B(bc-ad)(2bdf-bcg-adg)(2abd^2fg-a^2d^2g^2-b^2(2d^2f^2-2cdfg+c^2g^2))n\left(A+B \log\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)\log\left[\frac{bc-ad}{b(c+dx)}\right] + \frac{B^2(bc-ad)^4g^3n^2\log\left[\frac{a+bx}{c+dx}\right]}{6b^4d^4} + \frac{B^2(bc-ad)^3g^2(4bdf-3bcg-adg)n^2\log\left[\frac{a+bx}{c+dx}\right]}{4b^4d^4} + \frac{B^2(bc-ad)^4g^3n^2\log[c+dx]}{6b^4d^4} + \frac{B^2(bc-ad)^3g^2(4bdf-3bcg-adg)n^2\log[c+dx]}{4b^4d^4} + \frac{1}{2b^4d^4}B^2(bc-ad)^2g(a^2d^2g^2-2abd g(2df-cg)+b^2(6d^2f^2-8cdfg+3c^2g^2))n^2\log[c+dx] - \frac{1}{2b^4d^4}B^2(bc-ad)(2bdf-bcg-adg)(2abd^2fg-a^2d^2g^2-b^2(2d^2f^2-2cdfg+c^2g^2))n^2\text{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]$$

Result (type 4, 2541 leaves):

$$\begin{aligned}
 & f^3 x \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right)^2 + \\
 & \frac{3}{2} f^2 g x^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right)^2 + \\
 & f g^2 x^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right)^2 + \\
 & \frac{1}{4} g^3 x^4 \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right)^2 - \frac{1}{b d} \\
 & 2 B f^3 n \left(-A - B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] + B n \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right) \\
 & \left(a d \operatorname{Log} [a+b x] + b d x \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] - b c \operatorname{Log} [c+d x] \right) + \\
 & \frac{1}{12} B g^3 n \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right) \left(\frac{6 a^3 x}{b^3} - \frac{6 c^3 x}{d^3} - \frac{3 a^2 x^2}{b^2} + \right. \\
 & \left. \frac{3 c^2 x^2}{d^2} + \frac{2 a x^3}{b} - \frac{2 c x^3}{d} - \frac{6 a^4 \operatorname{Log} [a+b x]}{b^4} + 6 x^4 \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] + \frac{6 c^4 \operatorname{Log} [c+d x]}{d^4} \right) + \\
 & B f g^2 n \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right) \\
 & \left(\frac{(b c - a d) x (2 b c + 2 a d - b d x)}{b^2 d^2} + \frac{2 a^3 \operatorname{Log} [a+b x]}{b^3} + 2 x^3 \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] - \frac{2 c^3 \operatorname{Log} [c+d x]}{d^3} \right) - \\
 & \frac{1}{b^2 d^2} 3 B f^2 g n \left(-A - B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] + B n \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right) \\
 & \left(-a^2 d^2 \operatorname{Log} [a+b x] + b \left(d (-b c + a d) x + b d^2 x^2 \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] + b c^2 \operatorname{Log} [c+d x] \right) \right) + \\
 & \frac{1}{b d} B^2 f^3 n^2 \left(a d \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + b c \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 2 a d \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a+b x] + \right. \\
 & 2 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a+b x] - 2 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a+b x)}{-b c + a d} \right] + \\
 & 2 a d \operatorname{Log} [a+b x] \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] + b d x \operatorname{Log} \left[\frac{a+b x}{c+d x} \right]^2 + 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [c+d x] - \\
 & 2 b c \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [c+d x] - 2 b c \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \operatorname{Log} [c+d x] - 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \\
 & \left. \operatorname{Log} \left[\frac{b (c+d x)}{b c - a d} \right] - 2 b c \operatorname{PolyLog} \left[2, \frac{d (a+b x)}{-b c + a d} \right] - 2 a d \operatorname{PolyLog} \left[2, \frac{b (c+d x)}{b c - a d} \right] \right) + \\
 & \frac{1}{12} B^2 g^3 n^2 \left(3 x^4 \operatorname{Log} \left[\frac{a+b x}{c+d x} \right]^2 + \frac{1}{b^4 d^4} \left(-6 b^4 c^4 + 6 a b^3 c^3 d + 6 a^3 b c d^3 - 6 a^4 d^4 - 5 b^4 c^3 d x + \right. \right. \\
 & 5 a b^3 c^2 d^2 x + 5 a^2 b^2 c d^3 x - 5 a^3 b d^4 x + b^4 c^2 d^2 x^2 - 2 a b^3 c d^3 x^2 + a^2 b^2 d^4 x^2 - \\
 & 6 a b^3 c^3 d \operatorname{Log} \left[\frac{a}{b} + x \right] + 6 a^4 d^4 \operatorname{Log} \left[\frac{a}{b} + x \right] - 3 a^4 d^4 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 6 b^4 c^4 \operatorname{Log} \left[\frac{c}{d} + x \right] - \\
 & 6 a^3 b c d^3 \operatorname{Log} \left[\frac{c}{d} + x \right] - 3 b^4 c^4 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 3 a^2 b^2 c^2 d^2 \operatorname{Log} [a+b x] - 2 a^3 b c d^3 \operatorname{Log} [a+b x] + \\
 & \left. 5 a^4 d^4 \operatorname{Log} [a+b x] + 6 a^4 d^4 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a+b x] - 6 a^4 d^4 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a+b x] + \right.
 \end{aligned}$$

$$\begin{aligned}
& 6 a^4 d^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]-6 b^4 c^3 d x \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]+6 a^3 b d^4 x \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]+ \\
& 3 b^4 c^2 d^2 x^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]-3 a^2 b^2 d^4 x^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]-2 b^4 c d^3 x^3 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]+ \\
& 2 a b^3 d^4 x^3 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]-6 a^4 d^4 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]+5 b^4 c^4 \operatorname{Log}[c+d x]- \\
& 2 a b^3 c^3 d \operatorname{Log}[c+d x]-3 a^2 b^2 c^2 d^2 \operatorname{Log}[c+d x]-6 b^4 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]+ \\
& 6 b^4 c^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]+6 b^4 c^4 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \operatorname{Log}[c+d x]+6 b^4 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \\
& \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+6 b^4 c^4 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]+6 a^4 d^4 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\left.\right\}+\frac{3}{2} B^2 \\
& f^2 g n^2\left(x^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2-\frac{1}{b^2 d^2}\left(-2 d(-b c+a d)(a+b x)\left(-1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)+a^2 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2-\right.\right. \\
& 2 b(b c-a d)(c+d x)\left(-1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)+b^2 c^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2-2\left(\operatorname{Log}\left[\frac{a}{b}+x\right]-\operatorname{Log}\left[\frac{c}{d}+x\right]-\right. \\
& \left.\left.\operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\left(a^2 d^2 \operatorname{Log}[a+b x]-b(d(-b c+a d) x+b c^2 \operatorname{Log}[c+d x])\right)\right)- \\
& 2 b^2 c^2\left(\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+\operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)- \\
& 2 a^2 d^2\left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+\operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right)\left.\right\}+ \\
& 3 B^2 f g^2 n^2\left(\frac{1}{3} x^3 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2-\frac{1}{6 b^3 d^3}\left(4 d(-b c+a d)(b c+a d)(a+b x)\left(-1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)-\right.\right. \\
& 2 a^3 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2+4 b(b c-a d)(b c+a d)(c+d x)\left(-1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)- \\
& 2 b^3 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2+d^2(b c-a d)\left(b x(2 a-b x)+2 b^2 x^2 \operatorname{Log}\left[\frac{a}{b}+x\right]-2 a^2 \operatorname{Log}[a+b x]\right)+ \\
& b^2(b c-a d)\left(d x(-2 c+d x)-2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d}+x\right]+2 c^2 \operatorname{Log}[c+d x]\right)- \\
& 2\left(\operatorname{Log}\left[\frac{a}{b}+x\right]-\operatorname{Log}\left[\frac{c}{d}+x\right]-\operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) \\
& (b d(b c-a d) x(-2 b c-2 a d+b d x)-2 a^3 d^3 \operatorname{Log}[a+b x]+2 b^3 c^3 \operatorname{Log}[c+d x])\left.\right\}+ \\
& 4 b^3 c^3\left(\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+\operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)+ \\
& 4 a^3 d^3\left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+\operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right)\left.\right\}
\end{aligned}$$

Problem 68: Result more than twice size of optimal antiderivative.

$$\int (f+g x)^2\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2 d x$$

Optimal (type 4, 565 leaves, 12 steps):

$$\begin{aligned}
 & \frac{B^2 (b c - a d)^2 g^2 n^2 x}{3 b^2 d^2} - \frac{1}{3 b^3 d^2} \\
 & 2 B (b c - a d) g (3 b d f - 2 b c g - a d g) n (a + b x) \left(A + B \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right) - \\
 & \frac{B (b c - a d) g^2 n (c + d x)^2 \left(A + B \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)}{3 b d^3} - \\
 & \frac{(b f - a g)^3 \left(A + B \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)^2}{3 b^3 g} + \frac{(f + g x)^3 \left(A + B \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)^2}{3 g} + \frac{1}{3 b^3 d^3} \\
 & 2 B (b c - a d) (a^2 d^2 g^2 - a b d g (3 d f - c g) + b^2 (3 d^2 f^2 - 3 c d f g + c^2 g^2)) \\
 & n \left(A + B \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right) \text{Log}\left[\frac{b c - a d}{b (c + d x)}\right] + \\
 & \frac{B^2 (b c - a d)^3 g^2 n^2 \text{Log}\left[\frac{a + b x}{c + d x}\right]}{3 b^3 d^3} + \frac{B^2 (b c - a d)^3 g^2 n^2 \text{Log}[c + d x]}{3 b^3 d^3} + \\
 & \frac{2 B^2 (b c - a d)^2 g (3 b d f - 2 b c g - a d g) n^2 \text{Log}[c + d x]}{3 b^3 d^3} + \frac{1}{3 b^3 d^3} 2 B^2 (b c - a d) \\
 & (a^2 d^2 g^2 - a b d g (3 d f - c g) + b^2 (3 d^2 f^2 - 3 c d f g + c^2 g^2)) n^2 \text{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]
 \end{aligned}$$

Result (type 4, 1534 leaves):

$$\begin{aligned}
 & f^2 x \left(A + B \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - B n \text{Log}\left[\frac{a + b x}{c + d x}\right] \right)^2 + f g x^2 \left(A + B \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - B n \text{Log}\left[\frac{a + b x}{c + d x}\right] \right)^2 + \\
 & \frac{1}{3} g^2 x^3 \left(A + B \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - B n \text{Log}\left[\frac{a + b x}{c + d x}\right] \right)^2 - \frac{1}{b d} \\
 & 2 B f^2 n \left(-A - B \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + B n \text{Log}\left[\frac{a + b x}{c + d x}\right] \right) \\
 & \left(a d \text{Log}[a + b x] + b d x \text{Log}\left[\frac{a + b x}{c + d x}\right] - b c \text{Log}[c + d x] \right) + \\
 & \frac{1}{3} B g^2 n \left(A + B \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - B n \text{Log}\left[\frac{a + b x}{c + d x}\right] \right) \\
 & \left(\frac{(b c - a d) x (2 b c + 2 a d - b d x)}{b^2 d^2} + \frac{2 a^3 \text{Log}[a + b x]}{b^3} + 2 x^3 \text{Log}\left[\frac{a + b x}{c + d x}\right] - \frac{2 c^3 \text{Log}[c + d x]}{d^3} \right) - \\
 & \frac{1}{b^2 d^2} 2 B f g n \left(-A - B \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + B n \text{Log}\left[\frac{a + b x}{c + d x}\right] \right) \\
 & \left(-a^2 d^2 \text{Log}[a + b x] + b \left(d (-b c + a d) x + b d^2 x^2 \text{Log}\left[\frac{a + b x}{c + d x}\right] + b c^2 \text{Log}[c + d x] \right) \right) + \\
 & \frac{1}{b d} B^2 f^2 n^2 \left(a d \text{Log}\left[\frac{a}{b} + x\right]^2 + b c \text{Log}\left[\frac{c}{d} + x\right]^2 - 2 a d \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] + \right. \\
 & 2 a d \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] - 2 a d \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \\
 & 2 a d \text{Log}[a + b x] \text{Log}\left[\frac{a + b x}{c + d x}\right] + b d x \text{Log}\left[\frac{a + b x}{c + d x}\right]^2 + 2 b c \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[c + d x] - \\
 & \left. 2 b c \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[c + d x] - 2 b c \text{Log}\left[\frac{a + b x}{c + d x}\right] \text{Log}[c + d x] - 2 b c \text{Log}\left[\frac{a}{b} + x\right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(\text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 2bc \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - 2ad \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) + \\
 & B^2 f g n^2 \left(x^2 \text{Log}\left[\frac{a+bx}{c+dx}\right]^2 - \frac{1}{b^2 d^2} \left(-2d(-bc+ad)(a+bx) \left(-1 + \text{Log}\left[\frac{a}{b} + x\right] \right) + a^2 d^2 \text{Log}\left[\frac{a}{b} + x\right]^2 - \right. \right. \\
 & \quad \left. \left. 2b(bc-ad)(c+dx) \left(-1 + \text{Log}\left[\frac{c}{d} + x\right] \right) + b^2 c^2 \text{Log}\left[\frac{c}{d} + x\right]^2 - 2 \left(\text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] - \right. \right. \right. \\
 & \quad \left. \left. \left. \text{Log}\left[\frac{a+bx}{c+dx}\right] \right) \left(a^2 d^2 \text{Log}[a+bx] - b(d(-bc+ad)x + bc^2 \text{Log}[c+dx]) \right) \right) - \right. \\
 & \quad \left. 2b^2 c^2 \left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) - \right. \\
 & \quad \left. \left. 2a^2 d^2 \left(\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) \right) + \\
 & B^2 g^2 n^2 \left(\frac{1}{3} x^3 \text{Log}\left[\frac{a+bx}{c+dx}\right]^2 - \frac{1}{6b^3 d^3} \left(4d(-bc+ad)(bc+ad)(a+bx) \left(-1 + \text{Log}\left[\frac{a}{b} + x\right] \right) - \right. \right. \\
 & \quad \left. \left. 2a^3 d^3 \text{Log}\left[\frac{a}{b} + x\right]^2 + 4b(bc-ad)(bc+ad)(c+dx) \left(-1 + \text{Log}\left[\frac{c}{d} + x\right] \right) - \right. \right. \\
 & \quad \left. \left. 2b^3 c^3 \text{Log}\left[\frac{c}{d} + x\right]^2 + d^2(bc-ad) \left(bx(2a-bx) + 2b^2 x^2 \text{Log}\left[\frac{a}{b} + x\right] - 2a^2 \text{Log}[a+bx] \right) \right) + \right. \\
 & \quad \left. b^2(bc-ad) \left(dx(-2c+dx) - 2d^2 x^2 \text{Log}\left[\frac{c}{d} + x\right] + 2c^2 \text{Log}[c+dx] \right) - \right. \\
 & \quad \left. 2 \left(\text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{a+bx}{c+dx}\right] \right) \right. \\
 & \quad \left. \left(bd(bc-ad)x(-2bc-2ad+bdx) - 2a^3 d^3 \text{Log}[a+bx] + 2b^3 c^3 \text{Log}[c+dx] \right) + \right. \\
 & \quad \left. 4b^3 c^3 \left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) + \right. \\
 & \quad \left. \left. 4a^3 d^3 \left(\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) \right)
 \end{aligned}$$

Problem 69: Result more than twice size of optimal antiderivative.

$$\int (f+g x) \left(A+B \text{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 290 leaves, 9 steps):

$$\begin{aligned}
 & \frac{B(bc-ad)gn(a+bx)\left(A+B\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)}{b^2d} - \\
 & \frac{(bf-ag)^2\left(A+B\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{2b^2g} + \frac{(f+gx)^2\left(A+B\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{2g} + \frac{1}{b^2d^2} \\
 & B(bc-ad)(2bdf-bcg-adg)n\left(A+B\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)\text{Log}\left[\frac{bc-ad}{b(c+dx)}\right] + \\
 & \frac{B^2(bc-ad)^2gn^2\text{Log}[c+dx]}{b^2d^2} + \frac{B^2(bc-ad)(2bdf-bcg-adg)n^2\text{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{b^2d^2}
 \end{aligned}$$

Result (type 4, 902 leaves):

$$\begin{aligned}
 & \frac{1}{2 b^2 d^2} \left(2 b^2 d^2 f x \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right)^2 + \right. \\
 & b^2 d^2 g x^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right)^2 + \\
 & 4 b B d f n \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right) \\
 & \left(a d \operatorname{Log} [a+b x] + b d x \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] - b c \operatorname{Log} [c+d x] \right) - \\
 & 2 B g n \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right) \\
 & \left(a^2 d^2 \operatorname{Log} [a+b x] - b \left(d (-b c + a d) x + b d^2 x^2 \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] + b c^2 \operatorname{Log} [c+d x] \right) \right) + \\
 & 2 b B^2 d f n^2 \left(a d \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + b c \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 2 a d \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a+b x] + \right. \\
 & 2 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a+b x] - 2 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a+b x)}{-b c + a d} \right] + \\
 & 2 a d \operatorname{Log} [a+b x] \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] + b d x \operatorname{Log} \left[\frac{a+b x}{c+d x} \right]^2 + 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [c+d x] - \\
 & 2 b c \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [c+d x] - 2 b c \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \operatorname{Log} [c+d x] - 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \\
 & \left. \operatorname{Log} \left[\frac{b (c+d x)}{b c - a d} \right] - 2 b c \operatorname{PolyLog} \left[2, \frac{d (a+b x)}{-b c + a d} \right] - 2 a d \operatorname{PolyLog} \left[2, \frac{b (c+d x)}{b c - a d} \right] \right) + \\
 & B^2 g n^2 \left(2 d (-b c + a d) (a+b x) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) - a^2 d^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + \right. \\
 & 2 b (b c - a d) (c+d x) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) - b^2 c^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + \\
 & b^2 d^2 x^2 \operatorname{Log} \left[\frac{a+b x}{c+d x} \right]^2 + 2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right) \\
 & \left(a^2 d^2 \operatorname{Log} [a+b x] - b \left(d (-b c + a d) x + b c^2 \operatorname{Log} [c+d x] \right) \right) + \\
 & 2 b^2 c^2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c+d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d (a+b x)}{-b c + a d} \right] \right) + \\
 & \left. \left. 2 a^2 d^2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a+b x)}{-b c + a d} \right] + \operatorname{PolyLog} \left[2, \frac{b (c+d x)}{b c - a d} \right] \right) \right) \right)
 \end{aligned}$$

Problem 70: Result more than twice size of optimal antiderivative.

$$\int \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 135 leaves, 6 steps):

$$\frac{(a+b x) \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{b} + \frac{2 B(b c-a d) n \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right) \operatorname{Log}\left[\frac{b c-a d}{b(c+d x)}\right]}{b d} + \frac{2 B^2(b c-a d) n^2 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{b d}$$

Result (type 4, 421 leaves):

$$\begin{aligned} & \frac{1}{b d} \left(A^2 b d x + a B^2 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + b B^2 c n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2 a A B d n \operatorname{Log}[a+b x] - \right. \\ & 2 a B^2 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a+b x] + 2 a B^2 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a+b x] - \\ & 2 a B^2 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + 2 A b B d x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\ & 2 a B^2 d n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + b B^2 d x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 - 2 A b B c n \operatorname{Log}[c+d x] + \\ & 2 b B^2 c n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c+d x] - 2 b B^2 c n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c+d x] - \\ & 2 b B^2 c n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] - 2 b B^2 c n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\ & \left. 2 b B^2 c n^2 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] - 2 a B^2 d n^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) \end{aligned}$$

Problem 71: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{f+g x} d x$$

Optimal (type 4, 297 leaves, 9 steps):

$$\begin{aligned} & -\frac{\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2 \operatorname{Log}\left[\frac{b c-a d}{b(c+d x)}\right]}{g} + \frac{\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2 \operatorname{Log}\left[1-\frac{(d f-c g)(a+b x)}{(b f-a g)(c+d x)}\right]}{g} \\ & \frac{2 B n \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{g} + \\ & \frac{2 B n \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right) \operatorname{PolyLog}\left[2, \frac{(d f-c g)(a+b x)}{(b f-a g)(c+d x)}\right]}{g} + \\ & \frac{2 B^2 n^2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{b(c+d x)}\right]}{g} - \frac{2 B^2 n^2 \operatorname{PolyLog}\left[3, \frac{(d f-c g)(a+b x)}{(b f-a g)(c+d x)}\right]}{g} \end{aligned}$$

Result (type 4, 1441 leaves):

$$\begin{aligned}
 & \frac{1}{g} \left(-B^2 n^2 \operatorname{Log} \left[\frac{-b c + a d}{d (a + b x)} \right] \operatorname{Log} \left[\frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)} \right]^2 + \right. \\
 & A^2 \operatorname{Log} [f + g x] - 2 A B n \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [f + g x] + B^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} [f + g x] + \\
 & 2 A B n \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [f + g x] - 2 B^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [f + g x] + \\
 & B^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \operatorname{Log} [f + g x] + 2 A B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \operatorname{Log} [f + g x] - \\
 & 2 B^2 n \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \operatorname{Log} [f + g x] + 2 B^2 n \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \operatorname{Log} [f + g x] + \\
 & B^2 \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right]^2 \operatorname{Log} [f + g x] + 2 A B n \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \\
 & B^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} \left[\frac{b (f + g x)}{b f - a g} \right] + 2 B^2 n \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \operatorname{Log} \left[\frac{b (f + g x)}{b f - a g} \right] + \\
 & 2 B^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{g (c + d x)}{-d f + c g} \right] \operatorname{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - B^2 n^2 \operatorname{Log} \left[\frac{g (c + d x)}{-d f + c g} \right]^2 \operatorname{Log} \left[\frac{b (f + g x)}{b f - a g} \right] + \\
 & 2 B^2 n^2 \operatorname{Log} \left[\frac{g (c + d x)}{-d f + c g} \right] \operatorname{Log} \left[\frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)} \right] \operatorname{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \\
 & B^2 n^2 \operatorname{Log} \left[\frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)} \right]^2 \operatorname{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - 2 A B n \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (f + g x)}{d f - c g} \right] + \\
 & 2 B^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (f + g x)}{d f - c g} \right] - B^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \operatorname{Log} \left[\frac{d (f + g x)}{d f - c g} \right] - \\
 & 2 B^2 n \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \operatorname{Log} \left[\frac{d (f + g x)}{d f - c g} \right] - \\
 & 2 B^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{g (c + d x)}{-d f + c g} \right] \operatorname{Log} \left[\frac{d (f + g x)}{d f - c g} \right] + B^2 n^2 \operatorname{Log} \left[\frac{g (c + d x)}{-d f + c g} \right]^2 \operatorname{Log} \left[\frac{d (f + g x)}{d f - c g} \right] - \\
 & 2 B^2 n^2 \operatorname{Log} \left[\frac{g (c + d x)}{-d f + c g} \right] \operatorname{Log} \left[\frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)} \right] \operatorname{Log} \left[\frac{d (f + g x)}{d f - c g} \right] + \\
 & B^2 n^2 \operatorname{Log} \left[\frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)} \right]^2 \operatorname{Log} \left[\frac{(-b c + a d) (f + g x)}{(d f - c g) (a + b x)} \right] + \\
 & 2 B n \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + B n \operatorname{Log} \left[\frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)} \right] \right) \operatorname{PolyLog} \left[2, \frac{g (a + b x)}{-b f + a g} \right] - \\
 & 2 B n \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + B n \operatorname{Log} \left[\frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)} \right] \right) \operatorname{PolyLog} \left[2, \frac{g (c + d x)}{-d f + c g} \right] - \\
 & 2 B^2 n^2 \operatorname{Log} \left[\frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)} \right] \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{d (a + b x)} \right] + \\
 & 2 B^2 n^2 \operatorname{Log} \left[\frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)} \right] \operatorname{PolyLog} \left[2, \frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)} \right] + \\
 & \left. 2 B^2 n^2 \operatorname{PolyLog} \left[3, \frac{b (c + d x)}{d (a + b x)} \right] - 2 B^2 n^2 \operatorname{PolyLog} \left[3, \frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)} \right] \right)
 \end{aligned}$$

Problem 72: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{(f+gx)^2} dx$$

Optimal (type 4, 206 leaves, 4 steps):

$$\frac{(a+bx) \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{(bf-ag)(f+gx)} + \frac{2B(bc-ad)n \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right) \operatorname{Log}\left[1 - \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)}\right]}{(bf-ag)(df-cg)} + \frac{2B^2(bc-ad)n^2 \operatorname{PolyLog}\left[2, \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)}\right]}{(bf-ag)(df-cg)}$$

Result (type 4, 3524 leaves):

$$\frac{1}{g(-bf+ag)(-df+cg)(f+gx)} \left(-A^2bd f^2 + A^2bc f g + aA^2dfg - aA^2cg^2 + 2AbBdf^2n \operatorname{Log}\left[\frac{a}{b} + x\right] - 2AbBc f g n \operatorname{Log}\left[\frac{a}{b} + x\right] + 2AbBdf g n x \operatorname{Log}\left[\frac{a}{b} + x\right] - 2AbBcg^2n x \operatorname{Log}\left[\frac{a}{b} + x\right] - bB^2df^2n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + bB^2c f g n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - bB^2df g n^2 x \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + bB^2cg^2n^2 x \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2AbBdf^2n \operatorname{Log}\left[\frac{c}{d} + x\right] + 2aABdf g n \operatorname{Log}\left[\frac{c}{d} + x\right] - 2AbBdf g n x \operatorname{Log}\left[\frac{c}{d} + x\right] + 2aABdg^2n x \operatorname{Log}\left[\frac{c}{d} + x\right] + 2bB^2df^2n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] - 2aB^2df g n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] + 2bB^2df g n^2 x \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] - 2aB^2dg^2n^2 x \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] - bB^2df^2n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + aB^2df g n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - bB^2df g n^2 x \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + aB^2dg^2n^2 x \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2AbBdf^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 2AbBc f g \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 2aABdf g \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - 2aABcg^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 2bB^2df^2n \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - 2bB^2c f g n \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 2bB^2df g n x \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - 2bB^2cg^2n x \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - 2bB^2df^2n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 2aB^2df g n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - 2bB^2df g n x \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 2aB^2dg^2n x \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - bB^2df^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 + bB^2c f g \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 + aB^2df g \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 - aB^2cg^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 - 2bB^2c f g n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right] +$$

$$\begin{aligned}
 & 2 a B^2 d f g n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right]-2 b B^2 c g^2 n^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right]+ \\
 & 2 a B^2 d g^2 n^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right]+b B^2 c f g n^2 \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right]^2- \\
 & a B^2 d f g n^2 \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right]^2+b B^2 c g^2 n^2 x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right]^2- \\
 & a B^2 d g^2 n^2 x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right]^2-2 b B^2 c f g n^2 \operatorname{Log}\left[\frac{-b c+a d}{d(a+b x)}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]+ \\
 & 2 a B^2 d f g n^2 \operatorname{Log}\left[\frac{-b c+a d}{d(a+b x)}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]- \\
 & 2 b B^2 c g^2 n^2 x \operatorname{Log}\left[\frac{-b c+a d}{d(a+b x)}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]+ \\
 & 2 a B^2 d g^2 n^2 x \operatorname{Log}\left[\frac{-b c+a d}{d(a+b x)}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]- \\
 & 2 b B^2 c f g n^2 \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]+ \\
 & 2 a B^2 d f g n^2 \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]- \\
 & 2 b B^2 c g^2 n^2 x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]+ \\
 & 2 a B^2 d g^2 n^2 x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]+ \\
 & b B^2 c f g n^2 \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]^2-a B^2 d f g n^2 \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]^2+ \\
 & b B^2 c g^2 n^2 x \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]^2-a B^2 d g^2 n^2 x \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]^2- \\
 & 2 A b B d f^2 n \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+2 A b B c f g n \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]-2 A b B d f g n x \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+ \\
 & 2 A b B c g^2 n x \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+2 b B^2 d f^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]- \\
 & 2 a B^2 d f g n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+2 b B^2 d f g n^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]- \\
 & 2 a B^2 d g^2 n^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]-2 b B^2 d f^2 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+ \\
 & 2 b B^2 c f g n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]-2 b B^2 d f g n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \\
 & \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+2 b B^2 c g^2 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]-
 \end{aligned}$$

$$\begin{aligned}
 & 2 b B^2 d f^2 n^2 \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+2 b B^2 c f g n^2 \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]- \\
 & 2 b B^2 d f g n^2 x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+ \\
 & 2 b B^2 c g^2 n^2 x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+2 A b B d f^2 n \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]- \\
 & 2 a A B d f g n \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+2 A b B d f g n x \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]-2 a A B d g^2 n x \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]- \\
 & 2 b B^2 d f^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+2 a B^2 d f g n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]- \\
 & 2 b B^2 d f g n^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+2 a B^2 d g^2 n^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+ \\
 & 2 b B^2 d f^2 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]-2 a B^2 d f g n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+ \\
 & 2 b B^2 d f g n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]- \\
 & 2 a B^2 d g^2 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+ \\
 & 2 b B^2 d f^2 n^2 \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]-2 b B^2 c f g n^2 \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+ \\
 & 2 b B^2 d f g n^2 x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]- \\
 & 2 b B^2 c g^2 n^2 x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+2 B^2(b c-a d) g n^2(f+g x) \\
 & \operatorname{PolyLog}\left[2, \frac{g(a+b x)}{-b f+a g}\right]-2 B^2(b c-a d) g n^2(f+g x) \operatorname{PolyLog}\left[2, \frac{g(c+d x)}{-d f+c g}\right]- \\
 & 2 b B^2 c f g n^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]+2 a B^2 d f g n^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]- \\
 & 2 b B^2 c g^2 n^2 x \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]+2 a B^2 d g^2 n^2 x \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]
 \end{aligned}$$

Problem 73: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(f+g x)^3} d x$$

Optimal (type 4, 389 leaves, 9 steps):

$$\frac{B (b c - a d) g n (a + b x) \left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{(b f - a g)^2 (d f - c g) (f + g x)} +$$

$$\frac{b^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)^2}{2 g (b f - a g)^2} - \frac{\left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)^2}{2 g (f + g x)^2} + \frac{B^2 (b c - a d)^2 g n^2 \operatorname{Log}\left[\frac{f+g x}{c+d x} \right]}{(b f - a g)^2 (d f - c g)^2} +$$

$$\left(B (b c - a d) (2 b d f - b c g - a d g) n \left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right) \operatorname{Log}\left[1 - \frac{(d f - c g) (a + b x)}{(b f - a g) (c + d x)} \right] \right) /$$

$$\left((b f - a g)^2 (d f - c g)^2 \right) + \frac{B^2 (b c - a d) (2 b d f - b c g - a d g) n^2 \operatorname{PolyLog}\left[2, \frac{(d f - c g) (a + b x)}{(b f - a g) (c + d x)} \right]}{(b f - a g)^2 (d f - c g)^2}$$

Result(type 4, 18311 leaves):

$$- \frac{\left(A + B \left(\operatorname{Log}\left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x} \right] \right) \right)^2}{2 g (f + g x)^2} +$$

$$2 B n \left(A + B \left(\operatorname{Log}\left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x} \right] \right) \right) \left(\frac{1}{2 g} \left(\frac{g \left(\frac{a}{b} + x \right)}{\left(-f + \frac{a g}{b} \right)^3 \left(1 - \frac{g \left(\frac{a}{b} + x \right)}{-f + \frac{a g}{b}} \right)} - \right.$$

$$\left. \left(\frac{g^2 \left(\frac{a}{b} + x \right)^2}{\left(-f + \frac{a g}{b} \right)^4 \left(1 - \frac{g \left(\frac{a}{b} + x \right)}{-f + \frac{a g}{b}} \right)^2} + \frac{2 g \left(\frac{a}{b} + x \right)}{\left(-f + \frac{a g}{b} \right)^3 \left(1 - \frac{g \left(\frac{a}{b} + x \right)}{-f + \frac{a g}{b}} \right)} \right) \operatorname{Log}\left[\frac{a}{b} + x \right] - \frac{\operatorname{Log}\left[1 - \frac{g \left(\frac{a}{b} + x \right)}{-f + \frac{a g}{b}} \right]}{\left(-f + \frac{a g}{b} \right)^2} \right) - \frac{1}{2 g}$$

$$\left(\frac{g \left(\frac{c}{d} + x \right)}{\left(-f + \frac{c g}{d} \right)^3 \left(1 - \frac{g \left(\frac{c}{d} + x \right)}{-f + \frac{c g}{d}} \right)} - \left(\frac{g^2 \left(\frac{c}{d} + x \right)^2}{\left(-f + \frac{c g}{d} \right)^4 \left(1 - \frac{g \left(\frac{c}{d} + x \right)}{-f + \frac{c g}{d}} \right)^2} + \frac{2 g \left(\frac{c}{d} + x \right)}{\left(-f + \frac{c g}{d} \right)^3 \left(1 - \frac{g \left(\frac{c}{d} + x \right)}{-f + \frac{c g}{d}} \right)} \right) \operatorname{Log}\left[\frac{c}{d} + x \right] - \right.$$

$$\left. \frac{\operatorname{Log}\left[1 - \frac{g \left(\frac{c}{d} + x \right)}{-f + \frac{c g}{d}} \right]}{\left(-f + \frac{c g}{d} \right)^2} \right) - \frac{-\operatorname{Log}\left[\frac{a}{b} + x \right] + \operatorname{Log}\left[\frac{c}{d} + x \right] + \operatorname{Log}\left[\frac{-a}{c+d x} + \frac{b x}{c+d x} \right]}{2 g (f + g x)^2} \right) +$$

$$B^2 n^2 \left(2 \left(\frac{1}{2 g} \left(\frac{g \left(\frac{a}{b} + x \right)}{\left(-f + \frac{a g}{b} \right)^3 \left(1 - \frac{g \left(\frac{a}{b} + x \right)}{-f + \frac{a g}{b}} \right)} - \left(\frac{g^2 \left(\frac{a}{b} + x \right)^2}{\left(-f + \frac{a g}{b} \right)^4 \left(1 - \frac{g \left(\frac{a}{b} + x \right)}{-f + \frac{a g}{b}} \right)^2} + \frac{2 g \left(\frac{a}{b} + x \right)}{\left(-f + \frac{a g}{b} \right)^3 \left(1 - \frac{g \left(\frac{a}{b} + x \right)}{-f + \frac{a g}{b}} \right)} \right) \right.$$

$$\left. \operatorname{Log}\left[\frac{a}{b} + x \right] - \frac{\operatorname{Log}\left[1 - \frac{g \left(\frac{a}{b} + x \right)}{-f + \frac{a g}{b}} \right]}{\left(-f + \frac{a g}{b} \right)^2} \right) - \frac{1}{2 g} \left(\frac{g \left(\frac{c}{d} + x \right)}{\left(-f + \frac{c g}{d} \right)^3 \left(1 - \frac{g \left(\frac{c}{d} + x \right)}{-f + \frac{c g}{d}} \right)} - \right.$$

$$\left(\frac{g^2 \left(\frac{c}{d} + x\right)^2}{\left(-f + \frac{c g}{d}\right)^4 \left(1 - \frac{g \left(\frac{c}{d} + x\right)}{-f + \frac{c g}{d}}\right)^2} + \frac{2 g \left(\frac{c}{d} + x\right)}{\left(-f + \frac{c g}{d}\right)^3 \left(1 - \frac{g \left(\frac{c}{d} + x\right)}{-f + \frac{c g}{d}}\right)} \right) \text{Log} \left[\frac{c}{d} + x \right] - \frac{\text{Log} \left[1 - \frac{g \left(\frac{c}{d} + x\right)}{-f + \frac{c g}{d}} \right]}{\left(-f + \frac{c g}{d}\right)^2} \right)$$

$$\left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a}{c+d x} + \frac{b x}{c+d x} \right] \right) -$$

$$\frac{\left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a}{c+d x} + \frac{b x}{c+d x} \right] \right)^2}{2 g (f + g x)^2} + \frac{1}{g}$$

$$\left(-\frac{1}{2} \left(\frac{g^2 \left(\frac{a}{b} + x\right)^2}{\left(-f + \frac{a g}{b}\right)^4 \left(1 - \frac{g \left(\frac{a}{b} + x\right)}{-f + \frac{a g}{b}}\right)^2} + \frac{2 g \left(\frac{a}{b} + x\right)}{\left(-f + \frac{a g}{b}\right)^3 \left(1 - \frac{g \left(\frac{a}{b} + x\right)}{-f + \frac{a g}{b}}\right)} \right) \text{Log} \left[\frac{a}{b} + x \right]^2 + \frac{\text{Log} \left[1 - \frac{g \left(\frac{a}{b} + x\right)}{-f + \frac{a g}{b}} \right]}{\left(-f + \frac{a g}{b}\right)^2} + \right.$$

$$\left. \text{Log} \left[\frac{a}{b} + x \right] \left(\frac{g \left(\frac{a}{b} + x\right)}{\left(-f + \frac{a g}{b}\right)^3 \left(1 - \frac{g \left(\frac{a}{b} + x\right)}{-f + \frac{a g}{b}}\right)} - \frac{\text{Log} \left[1 - \frac{g \left(\frac{a}{b} + x\right)}{-f + \frac{a g}{b}} \right]}{\left(-f + \frac{a g}{b}\right)^2} \right) - \frac{\text{PolyLog} \left[2, \frac{g \left(\frac{a}{b} + x\right)}{-f + \frac{a g}{b}} \right]}{\left(-f + \frac{a g}{b}\right)^2} + \frac{1}{g} \right.$$

$$\left(-\frac{1}{2} \left(\frac{g^2 \left(\frac{c}{d} + x\right)^2}{\left(-f + \frac{c g}{d}\right)^4 \left(1 - \frac{g \left(\frac{c}{d} + x\right)}{-f + \frac{c g}{d}}\right)^2} + \frac{2 g \left(\frac{c}{d} + x\right)}{\left(-f + \frac{c g}{d}\right)^3 \left(1 - \frac{g \left(\frac{c}{d} + x\right)}{-f + \frac{c g}{d}}\right)} \right) \text{Log} \left[\frac{c}{d} + x \right]^2 + \frac{\text{Log} \left[1 - \frac{g \left(\frac{c}{d} + x\right)}{-f + \frac{c g}{d}} \right]}{\left(-f + \frac{c g}{d}\right)^2} + \right.$$

$$\left. \text{Log} \left[\frac{c}{d} + x \right] \left(\frac{g \left(\frac{c}{d} + x\right)}{\left(-f + \frac{c g}{d}\right)^3 \left(1 - \frac{g \left(\frac{c}{d} + x\right)}{-f + \frac{c g}{d}}\right)} - \frac{\text{Log} \left[1 - \frac{g \left(\frac{c}{d} + x\right)}{-f + \frac{c g}{d}} \right]}{\left(-f + \frac{c g}{d}\right)^2} \right) - \frac{\text{PolyLog} \left[2, \frac{g \left(\frac{c}{d} + x\right)}{-f + \frac{c g}{d}} \right]}{\left(-f + \frac{c g}{d}\right)^2} \right)$$

$$\frac{1}{f^2} \left(\frac{1}{g} 2 \left(\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] + \frac{1}{2} \text{Log} \left[\frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right] \right.$$

$$\left. \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right] \right) \left(\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) + \text{Log} \left[\right.$$

$$\left. \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right] \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \left(-\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] + \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) +$$

$$\frac{1}{2} \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right]^2 \left(\text{Log} \left[\frac{-b c + a d}{b d \left(\frac{a}{b} + x\right)} \right] + \text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \right.$$

$$\begin{aligned}
 & \left. \text{Log}\left[-\frac{(-bc+ad)(f+gx)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right]\right) + \left(\text{Log}\left[\frac{c}{d}+x\right] - \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right]\right) \\
 & \text{PolyLog}\left[2, -\frac{bg\left(\frac{a}{b}+x\right)}{bf-ag}\right] + \left(\text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right]\right) \\
 & \text{PolyLog}\left[2, \frac{dg\left(\frac{c}{d}+x\right)}{-df+cg}\right] + \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right] \left(\text{PolyLog}\left[2, \frac{\frac{c}{d}+x}{\frac{a}{b}+x}\right] - \right. \\
 & \left. \text{PolyLog}\left[2, -\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right]\right) - \text{PolyLog}\left[3, -\frac{bg\left(\frac{a}{b}+x\right)}{bf-ag}\right] - \\
 & \left. \text{PolyLog}\left[3, \frac{dg\left(\frac{c}{d}+x\right)}{-df+cg}\right] - \text{PolyLog}\left[3, \frac{\frac{c}{d}+x}{\frac{a}{b}+x}\right] + \text{PolyLog}\left[3, -\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right]\right) + \\
 & g^2 \left(\frac{1}{g} \left(\left(\frac{(bf-ag)\left(\frac{-2abx}{(bf-ag)^2} + \frac{2a^2b(f+gx)}{(bf-ag)^3}\right)}{b(f+gx)} - \frac{(bf-ag)x\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)^2} - \right. \right. \right. \\
 & \left. \left. \frac{a\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)} \right) \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{c}{d}+x\right] - \left(2b(-df+cg)\left(\frac{a}{b}+x\right) \right. \right. \\
 & \left. \left(\frac{cd(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)} + \frac{ad\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)} \right) \left(\frac{(bf-ag)\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)} + \right. \right. \\
 & \left. \left. \left(b(-df+cg)\left(\frac{a}{b}+x\right) \left(-\frac{(-bc+ad)x}{b(-df+cg)\left(\frac{a}{b}+x\right)} + \frac{c(-bc+ad)(f+gx)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)} \right) \right) \right) / \right. \\
 & \left. \left((-bc+ad)(f+gx) \right) \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right] \right) / \left(d(bf-ag)\left(\frac{c}{d}+ \right. \right. \\
 & \left. \left. x \right) \right) + \left(-\frac{(bf-ag)\left(\frac{-2abx}{(bf-ag)^2} + \frac{2a^2b(f+gx)}{(bf-ag)^3}\right)}{b(f+gx)} + \frac{(bf-ag)x\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)^2} + \right. \\
 & \left. \frac{a\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)} - \frac{(-df+cg)\left(\frac{-2cdx}{(-df+cg)^2} - \frac{2c^2d(f+gx)}{(-df+cg)^3}\right)}{d(f+gx)} + \right. \\
 & \left. \frac{(-df+cg)x\left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2}\right)}{d(f+gx)^2} - \frac{c\left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2}\right)}{d(f+gx)} \right) \text{Log}\left[\frac{dg\left(\frac{c}{d}+x\right)}{-df+cg}\right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right] + \frac{1}{2} \left(\frac{(bf-ag)\left(\frac{2abx}{(bf-ag)^2} + \frac{2a^2b(f+gx)}{(bf-ag)^3}\right)}{b(f+gx)} - \right. \\
 & \left. \frac{(bf-ag)x\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)^2} - \frac{a\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)} + \right. \\
 & \left. \left(b(-df+cg)\left(\frac{a}{b}+x\right) \left(\frac{2c(-bc+ad)x}{b(-df+cg)^2\left(\frac{a}{b}+x\right)} - \frac{2c^2(-bc+ad)(f+gx)}{b(-df+cg)^3\left(\frac{a}{b}+x\right)} \right) \right) / \right. \\
 & \left. \left((-bc+ad)(f+gx) \right) - \left(b(-df+cg)x\left(\frac{a}{b}+x\right) \left(-\frac{(-bc+ad)x}{b(-df+cg)\left(\frac{a}{b}+x\right)} + \right. \right. \right. \\
 & \left. \left. \left. \frac{c(-bc+ad)(f+gx)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)} \right) \right) \right) / \left((-bc+ad)(f+gx)^2 \right) + \\
 & \left. \frac{bc\left(\frac{a}{b}+x\right) \left(-\frac{(-bc+ad)x}{b(-df+cg)\left(\frac{a}{b}+x\right)} + \frac{c(-bc+ad)(f+gx)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)} \right)}{(-bc+ad)(f+gx)} \right) \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right]^2 + \\
 & 2 \left(-\frac{(bf-ag)\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)} - \frac{(-df+cg)\left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2}\right)}{d(f+gx)} \right) \\
 & \left(-\left(\left(b(-df+cg)\left(\frac{a}{b}+x\right) \left(\frac{cd(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)} + \frac{ad\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)} \right) \right) \right. \right. \\
 & \left. \left. \text{Log}\left[\frac{dg\left(\frac{c}{d}+x\right)}{-df+cg}\right] / \left(d(bf-ag)\left(\frac{c}{d}+x\right) \right) \right) + \frac{1}{dg\left(\frac{c}{d}+x\right)} \right. \\
 & \left. (-df+cg) \left(-\frac{cdg\left(\frac{c}{d}+x\right)}{(-df+cg)^2} + \frac{d\left(\frac{c}{d}+x\right)}{-df+cg} \right) \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right] \right) + \\
 & \frac{1}{dg\left(\frac{c}{d}+x\right)} (-df+cg) \left(-\frac{cdg\left(\frac{c}{d}+x\right)}{(-df+cg)^2} + \frac{d\left(\frac{c}{d}+x\right)}{-df+cg} \right) \\
 & \left(\left(\frac{(bf-ag)\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)} + \frac{(-df+cg)\left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2}\right)}{d(f+gx)} \right) \right. \\
 & \left. \left(-2 \text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{dg\left(\frac{c}{d}+x\right)}{-df+cg}\right] \right) + \frac{1}{dg\left(\frac{c}{d}+x\right)} (-df+cg) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(-\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g} \right) \left(\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) + \\
 & \frac{1}{2} \text{Log} \left[\frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right] \left(\frac{1}{d g \left(\frac{c}{d} + x\right)} - 2 (-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g} \right) \right. \\
 & \left. \left(\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2}\right)}{b (f + g x)} + \frac{(-d f + c g) \left(-\frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2}\right)}{d (f + g x)} \right) + \right. \\
 & \left. \left(\frac{(b f - a g) \left(\frac{2 a b x}{(b f - a g)^2} + \frac{2 a^2 b (f + g x)}{(b f - a g)^3}\right)}{b (f + g x)} - \frac{(b f - a g) x \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2}\right)}{b (f + g x)^2} - \right. \right. \\
 & \left. \frac{a \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2}\right)}{b (f + g x)} + \frac{(-d f + c g) \left(\frac{2 c d x}{(-d f + c g)^2} - \frac{2 c^2 d (f + g x)}{(-d f + c g)^3}\right)}{d (f + g x)} - \right. \\
 & \left. \frac{(-d f + c g) x \left(-\frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2}\right)}{d (f + g x)^2} + \right. \\
 & \left. \frac{c \left(-\frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2}\right)}{d (f + g x)} \right) \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right] \right) + \\
 & \left(\frac{(-d f + c g) \left(\frac{2 c^2 d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^3} - \frac{2 c d \left(\frac{c}{d} + x\right)}{(-d f + c g)^2}\right)}{d g \left(\frac{c}{d} + x\right)} + \frac{c \left(-\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g}\right)}{d g \left(\frac{c}{d} + x\right)} - \right. \\
 & \left. \frac{(-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g}\right)}{d g^2 \left(\frac{c}{d} + x\right)} \right) \left(\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) + \\
 & \frac{1}{2} \left(\frac{(-d f + c g) \left(\frac{2 c^2 d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^3} - \frac{2 c d \left(\frac{c}{d} + x\right)}{(-d f + c g)^2}\right)}{d g \left(\frac{c}{d} + x\right)} + \frac{c \left(-\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g}\right)}{d g \left(\frac{c}{d} + x\right)} - \right. \\
 & \left. \frac{(-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g}\right)}{d g^2 \left(\frac{c}{d} + x\right)} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(-2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{d g\left(\frac{c}{d} + x\right)}{-d f + c g}\right] \right) \left(\operatorname{Log}\left[\frac{b(f+g x)}{b f - a g}\right] - \operatorname{Log}\left[-\frac{d(f+g x)}{-d f + c g}\right] \right) + \\
 & \left(- \left(\left(2 b (-d f + c g)^2 \left(\frac{a}{b} + x\right) \left(-\frac{c d g\left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d\left(\frac{c}{d} + x\right)}{-d f + c g} \right) \left(\frac{c d (b f - a g)\left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{a d\left(\frac{c}{d} + x\right)}{b (-d f + c g)\left(\frac{a}{b} + x\right)} \right) \right) / \left(d^2 g (b f - a g) \left(\frac{c}{d} + x\right)^2 \right) \right) + \\
 & \left(- \left(\left(b (-d f + c g) \left(\frac{a}{b} + x\right) \left(-\frac{2 c^2 d (b f - a g)\left(\frac{c}{d} + x\right)}{b (-d f + c g)^3 \left(\frac{a}{b} + x\right)} - \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{2 a c d\left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} \right) \right) / \left(d (b f - a g) \left(\frac{c}{d} + x\right) \right) \right) - \\
 & \frac{b c\left(\frac{a}{b} + x\right) \left(\frac{c d (b f - a g)\left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d\left(\frac{c}{d} + x\right)}{b (-d f + c g)\left(\frac{a}{b} + x\right)} \right)}{d (b f - a g)\left(\frac{c}{d} + x\right)} - \left(a b (-d f + c g) \left(\frac{a}{b} + x\right) \right. \\
 & \quad \left. \left(\frac{c d (b f - a g)\left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d\left(\frac{c}{d} + x\right)}{b (-d f + c g)\left(\frac{a}{b} + x\right)} \right) \right) / \left(d (b f - a g)^2 \right. \\
 & \quad \left. \left(\frac{c}{d} + x\right) \right) \operatorname{Log}\left[\frac{d g\left(\frac{c}{d} + x\right)}{-d f + c g}\right] + \left(\frac{(-d f + c g) \left(\frac{2 c^2 d g\left(\frac{c}{d} + x\right)}{(-d f + c g)^3} - \frac{2 c d\left(\frac{c}{d} + x\right)}{(-d f + c g)^2} \right)}{d g\left(\frac{c}{d} + x\right)} + \right. \\
 & \quad \left. \frac{c \left(-\frac{c d g\left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d\left(\frac{c}{d} + x\right)}{-d f + c g} \right)}{d g\left(\frac{c}{d} + x\right)} - \frac{(-d f + c g) \left(-\frac{c d g\left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d\left(\frac{c}{d} + x\right)}{-d f + c g} \right)}{d g^2\left(\frac{c}{d} + x\right)} \right) \\
 & \left. \operatorname{Log}\left[-\frac{d (b f - a g)\left(\frac{c}{d} + x\right)}{b (-d f + c g)\left(\frac{a}{b} + x\right)}\right] \right) \left(-\operatorname{Log}\left[\frac{b(f+g x)}{b f - a g}\right] + \operatorname{Log}\left[-\frac{d(f+g x)}{-d f + c g}\right] \right) + \\
 & \frac{1}{2} \left(\left(2 b^2 (-d f + c g)^2 \left(\frac{a}{b} + x\right)^2 \left(\frac{c d (b f - a g)\left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d\left(\frac{c}{d} + x\right)}{b (-d f + c g)\left(\frac{a}{b} + x\right)} \right) \right) / \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(d^2 (b f - a g)^2 \left(\frac{c}{d} + x \right)^2 - \left(2 b (-d f + c g) \left(\frac{a}{b} + x \right) \left(-\frac{2 c^2 d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^3 \left(\frac{a}{b} + x \right)} - \right. \right. \\
 & \quad \left. \left. \frac{2 a c d \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) / \left(d (b f - a g) \right. \\
 & \quad \left. \left(\frac{c}{d} + x \right) \right) - \left(2 b c \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right. \\
 & \quad \left. \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) - \\
 & \quad \left(2 a b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right. \\
 & \quad \left. \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) / \left(d (b f - a g)^2 \left(\frac{c}{d} + x \right) \right) \Bigg) \\
 & \left(\text{Log} \left[\frac{-b c + a d}{b d \left(\frac{a}{b} + x \right)} \right] + \text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \text{Log} \left[-\frac{(-b c + a d) (f + g x)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) + \\
 & \frac{(b f - a g)^2 \left(-\frac{a b g \left(\frac{a}{b} + x \right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x \right)}{b f - a g} \right)^2 \text{Log} \left[1 + \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right]}{b^2 g^2 \left(\frac{a}{b} + x \right)^2} + \frac{1}{d g \left(\frac{c}{d} + x \right)} 2 (-d f + c g) \\
 & \left(-\frac{a b g \left(\frac{a}{b} + x \right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x \right)}{b f - a g} \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \\
 & \text{Log} \left[1 + \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right] + \left(\text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) \\
 & \left(\frac{(b f - a g) \left(-\frac{a b g \left(\frac{a}{b} + x \right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x \right)}{b f - a g} \right) \left(\frac{a b g \left(\frac{a}{b} + x \right)}{(b f - a g)^2} + \frac{b \left(\frac{a}{b} + x \right)}{b f - a g} \right)}{b g \left(\frac{a}{b} + x \right) \left(1 + \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right)} + \frac{1}{b g \left(\frac{a}{b} + x \right)} \right. \\
 & \quad \left. (b f - a g) \left(-\frac{2 a^2 b g \left(\frac{a}{b} + x \right)}{(b f - a g)^3} - \frac{2 a b \left(\frac{a}{b} + x \right)}{(b f - a g)^2} \right) \text{Log} \left[1 + \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right] - \right. \\
 & \quad \left. a \left(-\frac{a b g \left(\frac{a}{b} + x \right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x \right)}{b f - a g} \right) \text{Log} \left[1 + \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right] \right) \\
 & \quad \left. \frac{1}{b g \left(\frac{a}{b} + x \right)} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{(b f - a g) \left(-\frac{a b g \left(\frac{a+x}{b}\right)}{(b f - a g)^2} - \frac{b \left(\frac{a+x}{b}\right)}{b f - a g} \right) \text{Log} \left[1 + \frac{b g \left(\frac{a+x}{b}\right)}{b f - a g} \right]}{b g^2 \left(\frac{a}{b} + x\right)} \right\} + \\
 & \frac{(-d f + c g)^2 \left(-\frac{c d g \left(\frac{c+x}{d}\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c+x}{d}\right)}{-d f + c g} \right)^2 \text{Log} \left[1 - \frac{d g \left(\frac{c+x}{d}\right)}{-d f + c g} \right]}{d^2 g^2 \left(\frac{c}{d} + x\right)^2} + \\
 & \left(2 b (-d f + c g)^2 \left(\frac{a}{b} + x\right) \left(-\frac{c d g \left(\frac{c+x}{d}\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c+x}{d}\right)}{-d f + c g} \right) \right. \\
 & \left. \left(\frac{c d (b f - a g) \left(\frac{c+x}{d}\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c+x}{d}\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \text{Log} \left[1 - \frac{d g \left(\frac{c+x}{d}\right)}{-d f + c g} \right] \right) / \\
 & \left(d^2 g (b f - a g) \left(\frac{c}{d} + x\right)^2 \right) + \left(\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c+x}{d}\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \right) \\
 & \left(- \left(\left((-d f + c g) \left(\frac{c d g \left(\frac{c+x}{d}\right)}{(-d f + c g)^2} - \frac{d \left(\frac{c+x}{d}\right)}{-d f + c g} \right) \left(-\frac{c d g \left(\frac{c+x}{d}\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c+x}{d}\right)}{-d f + c g} \right) \right) \right) / \right. \\
 & \left. \left(d g \left(\frac{c}{d} + x\right) \left(1 - \frac{d g \left(\frac{c+x}{d}\right)}{-d f + c g} \right) \right) \right) - \frac{1}{d g \left(\frac{c}{d} + x\right)} \\
 & (-d f + c g) \left(\frac{2 c^2 d g \left(\frac{c+x}{d}\right)}{(-d f + c g)^3} - \frac{2 c d \left(\frac{c+x}{d}\right)}{(-d f + c g)^2} \right) \text{Log} \left[1 - \frac{d g \left(\frac{c+x}{d}\right)}{-d f + c g} \right] - \\
 & \frac{c \left(-\frac{c d g \left(\frac{c+x}{d}\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c+x}{d}\right)}{-d f + c g} \right) \text{Log} \left[1 - \frac{d g \left(\frac{c+x}{d}\right)}{-d f + c g} \right]}{d g \left(\frac{c}{d} + x\right)} + \\
 & \left. \frac{(-d f + c g) \left(-\frac{c d g \left(\frac{c+x}{d}\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c+x}{d}\right)}{-d f + c g} \right) \text{Log} \left[1 - \frac{d g \left(\frac{c+x}{d}\right)}{-d f + c g} \right]}{d g^2 \left(\frac{c}{d} + x\right)} \right\} + \\
 & \left(b^2 (-d f + c g)^2 \left(\frac{a}{b} + x\right)^2 \left(\frac{c d (b f - a g) \left(\frac{c+x}{d}\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c+x}{d}\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right)^2 \right. \\
 & \left. \text{Log} \left[1 + \frac{d (b f - a g) \left(\frac{c+x}{d}\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left(d^2 (b f - a g)^2 \left(\frac{c}{d} + x \right)^2 \right) + \text{Log} \left[- \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \\
 & \left(- \left(\left(b (-d f + c g) \left(\frac{a}{b} + x \right) \left(- \frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} - \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right. \right. \right. \\
 & \quad \left. \left. \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right) \right) / \\
 & \quad \left(d (b f - a g) \left(\frac{c}{d} + x \right) \left(1 + \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right) \right) - \\
 & \left(b (-d f + c g) \left(\frac{a}{b} + x \right) \left(- \frac{2 c^2 d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^3 \left(\frac{a}{b} + x \right)} - \frac{2 a c d \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right) \right. \\
 & \quad \left. \text{Log} \left[1 + \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) - \\
 & \left(b c \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right. \\
 & \quad \left. \text{Log} \left[1 + \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) - \\
 & \left(a b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right. \\
 & \quad \left. \text{Log} \left[1 + \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) / \left(d (b f - a g)^2 \left(\frac{c}{d} + x \right) \right) + \frac{1}{b g \left(\frac{a}{b} + x \right)} \\
 & (b f - a g) \left(- \frac{2 a^2 b g \left(\frac{a}{b} + x \right)}{(b f - a g)^3} - \frac{2 a b \left(\frac{a}{b} + x \right)}{(b f - a g)^2} \right) \text{PolyLog} \left[2, - \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right] - \\
 & a \left(- \frac{a b g \left(\frac{a}{b} + x \right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x \right)}{b f - a g} \right) \text{PolyLog} \left[2, - \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right] \\
 & \quad \quad \quad b g \left(\frac{a}{b} + x \right) - \\
 & (b f - a g) \left(- \frac{a b g \left(\frac{a}{b} + x \right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x \right)}{b f - a g} \right) \text{PolyLog} \left[2, - \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right] \\
 & \quad \quad \quad b g^2 \left(\frac{a}{b} + x \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left(\left(b (-d f + c g) \left(\frac{a}{b} + x \right) \left(-\frac{2 c^2 d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^3 \left(\frac{a}{b} + x \right)} - \frac{2 a c d \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right) \right) / \\
 & \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) + \frac{b c \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right)}{d (b f - a g) \left(\frac{c}{d} + x \right)} + \\
 & \left(a b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right) / \\
 & \left(d (b f - a g)^2 \left(\frac{c}{d} + x \right) \right) \left. \text{PolyLog} \left[2, -\frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right] - \frac{1}{d g \left(\frac{c}{d} + x \right)} \right. \\
 & (-d f + c g) \left(\frac{2 c^2 d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^3} - \frac{2 c d \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} \right) \text{PolyLog} \left[2, \frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] - \\
 & \frac{c \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \text{PolyLog} \left[2, \frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right]}{d g \left(\frac{c}{d} + x \right)} + \\
 & \frac{(-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \text{PolyLog} \left[2, \frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right]}{d g^2 \left(\frac{c}{d} + x \right)} + \\
 & \left(-\left(\left(b (-d f + c g) \left(\frac{a}{b} + x \right) \left(-\frac{2 c^2 d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^3 \left(\frac{a}{b} + x \right)} - \frac{2 a c d \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right) \right) / \right. \\
 & \left. \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) \right) - \frac{b c \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right)}{d (b f - a g) \left(\frac{c}{d} + x \right)} - \\
 & \left(a b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right) / \\
 & \left(d (b f - a g)^2 \left(\frac{c}{d} + x \right) \right) \left. \text{PolyLog} \left[2, \frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(- \left(\left(b (-d f + c g) \left(\frac{a}{b} + x \right) \left(- \frac{2 c^2 d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^3 \left(\frac{a}{b} + x \right)} - \frac{2 a c d \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right) \right) / \right. \\
 & \quad \left. \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) \right) - \frac{b c \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right)}{d (b f - a g) \left(\frac{c}{d} + x \right)} - \\
 & \quad \left(a b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right) / \\
 & \quad \left(d (b f - a g)^2 \left(\frac{c}{d} + x \right) \right) \Bigg) \\
 & \quad \left(\text{PolyLog}\left[2, \frac{c}{b} + x\right] - \text{PolyLog}\left[2, - \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) - \\
 & \quad \left(b (-d f + c g) \left(\frac{a}{b} + x \right) \left(- \frac{2 c^2 d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^3 \left(\frac{a}{b} + x \right)} - \frac{2 a c d \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right) \right. \\
 & \quad \left. \text{PolyLog}\left[2, - \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) - \\
 & \quad \left(b c \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right. \\
 & \quad \left. \text{PolyLog}\left[2, - \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) - \\
 & \quad \left(a b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right. \\
 & \quad \left. \text{PolyLog}\left[2, - \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) / \left(d (b f - a g)^2 \left(\frac{c}{d} + x \right) \right) \Bigg) - \\
 & \quad \frac{1}{g^2} 2 \left(\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right) \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right]}{b (f + g x)} + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{2} \left(\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right)}{b (f + g x)} + \frac{(-d f + c g) \left(-\frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2} \right)}{d (f + g x)} \right) \\
 & \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right) + \\
 & \left(-\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right)}{b (f + g x)} - \frac{(-d f + c g) \left(-\frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2} \right)}{d (f + g x)} \right) \text{Log} \left[\right. \\
 & \left. \frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] + \frac{1}{2} \left(\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right)}{b (f + g x)} + \right. \\
 & \left. \left(b (-d f + c g) \left(\frac{a}{b} + x \right) \left(-\frac{(-b c + a d) x}{b (-d f + c g) \left(\frac{a}{b} + x \right)} + \frac{c (-b c + a d) (f + g x)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right) \right) \right) / \\
 & \left((-b c + a d) (f + g x) \right) \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right]^2 + \\
 & \frac{1}{2 d g \left(\frac{c}{d} + x \right)} (-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \\
 & \left(\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) + \frac{1}{2 d g \left(\frac{c}{d} + x \right)} \\
 & (-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right) \\
 & \left(\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) - \left(b (-d f + c g) \left(\frac{a}{b} + x \right) \right. \\
 & \left. \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right. \\
 & \left. \left(-\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] + \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) \right) / \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) + \frac{1}{d g \left(\frac{c}{d} + x \right)} \\
 & (-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \\
 & \left(-\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] + \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) - \left(b (-d f + c g) \left(\frac{a}{b} + x \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \\
 & \left(\text{Log} \left[\frac{-b c + a d}{b d \left(\frac{a}{b} + x\right)} \right] + \text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \text{Log} \left[-\frac{(-b c + a d) (f + g x)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \right) / \\
 & \left(d (b f - a g) \left(\frac{c}{d} + x\right) \right) + \frac{1}{b g \left(\frac{a}{b} + x\right)} (b f - a g) \left(-\frac{a b g \left(\frac{a}{b} + x\right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x\right)}{b f - a g} \right) \\
 & \left(\text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \right) \text{Log} \left[1 + \frac{b g \left(\frac{a}{b} + x\right)}{b f - a g} \right] - \\
 & \frac{1}{d g \left(\frac{c}{d} + x\right)} (-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g} \right) \left(\text{Log} \left[\frac{a}{b} + x \right] + \right. \\
 & \left. \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \right) \text{Log} \left[1 - \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right] - \left(b (-d f + c g) \left(\frac{a}{b} + x\right) \right. \\
 & \left. \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \right. \\
 & \left. \text{Log} \left[1 + \frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x\right) \right) + \frac{1}{b g \left(\frac{a}{b} + x\right)} \\
 & (b f - a g) \left(-\frac{a b g \left(\frac{a}{b} + x\right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x\right)}{b f - a g} \right) \text{PolyLog} \left[2, -\frac{b g \left(\frac{a}{b} + x\right)}{b f - a g} \right] + \\
 & \left(b (-d f + c g) \left(\frac{a}{b} + x\right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \right. \\
 & \left. \text{PolyLog} \left[2, -\frac{b g \left(\frac{a}{b} + x\right)}{b f - a g} \right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x\right) \right) - \frac{1}{d g \left(\frac{c}{d} + x\right)} \\
 & (-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g} \right) \text{PolyLog} \left[2, \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right] - \\
 & \left(b (-d f + c g) \left(\frac{a}{b} + x\right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \right. \\
 & \left. \text{PolyLog} \left[2, \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x\right) \right) - \left(b (-d f + c g) \left(\frac{a}{b} + x\right) \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \left(\text{PolyLog}\left[2, \frac{\frac{c}{d} + x}{\frac{a}{b} + x}\right] - \right. \\
 & \left. \text{PolyLog}\left[2, -\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \right) \Big/ \left(d (b f - a g) \left(\frac{c}{d} + x\right) \right) - \\
 & \left(b (-d f + c g) \left(\frac{a}{b} + x\right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \right. \\
 & \left. \text{PolyLog}\left[2, -\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \right) \Big/ \left(d (b f - a g) \left(\frac{c}{d} + x\right) \right) \Big) + \\
 & \frac{1}{g^3} 2 \left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{b (f + g x)}{b f - a g}\right] + \frac{1}{2} \text{Log}\left[\frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g}\right] \right. \\
 & \left. \left(-2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g}\right] \right) \left(\text{Log}\left[\frac{b (f + g x)}{b f - a g}\right] - \text{Log}\left[-\frac{d (f + g x)}{-d f + c g}\right] \right) \right) + \\
 & \text{Log}\left[\frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g}\right] \text{Log}\left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \left(-\text{Log}\left[\frac{b (f + g x)}{b f - a g}\right] + \right. \\
 & \left. \text{Log}\left[-\frac{d (f + g x)}{-d f + c g}\right] \right) + \frac{1}{2} \text{Log}\left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right]^2 \\
 & \left(\text{Log}\left[\frac{-b c + a d}{b d \left(\frac{a}{b} + x\right)}\right] + \text{Log}\left[\frac{b (f + g x)}{b f - a g}\right] - \text{Log}\left[-\frac{(-b c + a d) (f + g x)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \right) + \\
 & \left(\text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \right) \text{PolyLog}\left[2, -\frac{b g \left(\frac{a}{b} + x\right)}{b f - a g}\right] + \\
 & \left(\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \right) \text{PolyLog}\left[2, \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g}\right] + \\
 & \text{Log}\left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \left(\text{PolyLog}\left[2, \frac{\frac{c}{d} + x}{\frac{a}{b} + x}\right] - \right. \\
 & \left. \text{PolyLog}\left[2, -\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \right) - \text{PolyLog}\left[3, -\frac{b g \left(\frac{a}{b} + x\right)}{b f - a g}\right] - \text{PolyLog}\left[3, \right. \\
 & \left. \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g}\right] - \text{PolyLog}\left[3, \frac{\frac{c}{d} + x}{\frac{a}{b} + x}\right] + \text{PolyLog}\left[3, -\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \Big) \Big) +
 \end{aligned}$$

$$\begin{aligned}
 & 4 g \left(\frac{1}{g} \left(\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right) \text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{c}{d} + x \right]}{b (f + g x)} + \right. \right. \\
 & \frac{1}{2} \left(\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right)}{b (f + g x)} + \frac{(-d f + c g) \left(-\frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2} \right)}{d (f + g x)} \right) \\
 & \left. \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right) + \right. \\
 & \left. \left(-\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right)}{b (f + g x)} - \frac{(-d f + c g) \left(-\frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2} \right)}{d (f + g x)} \right) \right. \\
 & \left. \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] + \frac{1}{2} \left(\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right)}{b (f + g x)} \right. \right. \\
 & \left. \left. \left(b (-d f + c g) \left(\frac{a}{b} + x \right) \left(-\frac{(-b c + a d) x}{b (-d f + c g) \left(\frac{a}{b} + x \right)} + \frac{c (-b c + a d) (f + g x)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right) \right) \right. \right. \\
 & \left. \left. \left((-b c + a d) (f + g x) \right) \right) \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right]^2 + \right. \\
 & \frac{1}{2 d g \left(\frac{c}{d} + x \right)} (-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \\
 & \left(\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) + \frac{1}{2 d g \left(\frac{c}{d} + x \right)} \\
 & (-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right) \\
 & \left(\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) - \left(b (-d f + c g) \left(\frac{a}{b} + x \right) \right. \\
 & \left. \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right. \\
 & \left. \left(-\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] + \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) \right) \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) + \frac{1}{d g \left(\frac{c}{d} + x \right)} \\
 & (-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right]
 \end{aligned}$$

$$\begin{aligned}
 & \left(-\text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + \text{Log}\left[-\frac{d(f+gx)}{-df+cg}\right] \right) - \left(b(-df+cg) \left(\frac{a}{b} + x\right) \right. \\
 & \left. \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x\right)}{b(-df+cg)^2 \left(\frac{a}{b} + x\right)} + \frac{ad \left(\frac{c}{d} + x\right)}{b(-df+cg) \left(\frac{a}{b} + x\right)} \right) \text{Log}\left[-\frac{d(bf-ag) \left(\frac{c}{d} + x\right)}{b(-df+cg) \left(\frac{a}{b} + x\right)} \right] \right) \\
 & \left(\text{Log}\left[\frac{-bc+ad}{bd \left(\frac{a}{b} + x\right)}\right] + \text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - \text{Log}\left[-\frac{(-bc+ad)(f+gx)}{b(-df+cg) \left(\frac{a}{b} + x\right)}\right] \right) \Big/ \\
 & \left(d(bf-ag) \left(\frac{c}{d} + x\right) \right) + \frac{1}{bg \left(\frac{a}{b} + x\right)} (bf-ag) \left(-\frac{abg \left(\frac{a}{b} + x\right)}{(bf-ag)^2} - \frac{b \left(\frac{a}{b} + x\right)}{bf-ag} \right) \\
 & \left(\text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[-\frac{d(bf-ag) \left(\frac{c}{d} + x\right)}{b(-df+cg) \left(\frac{a}{b} + x\right)}\right] \right) \text{Log}\left[1 + \frac{bg \left(\frac{a}{b} + x\right)}{bf-ag}\right] - \\
 & \frac{1}{dg \left(\frac{c}{d} + x\right)} (-df+cg) \left(-\frac{cdg \left(\frac{c}{d} + x\right)}{(-df+cg)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-df+cg} \right) \\
 & \left(\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[-\frac{d(bf-ag) \left(\frac{c}{d} + x\right)}{b(-df+cg) \left(\frac{a}{b} + x\right)}\right] \right) \text{Log}\left[1 - \frac{dg \left(\frac{c}{d} + x\right)}{-df+cg}\right] - \\
 & \left(b(-df+cg) \left(\frac{a}{b} + x\right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x\right)}{b(-df+cg)^2 \left(\frac{a}{b} + x\right)} + \frac{ad \left(\frac{c}{d} + x\right)}{b(-df+cg) \left(\frac{a}{b} + x\right)} \right) \right. \\
 & \left. \text{Log}\left[-\frac{d(bf-ag) \left(\frac{c}{d} + x\right)}{b(-df+cg) \left(\frac{a}{b} + x\right)}\right] \text{Log}\left[1 + \frac{d(bf-ag) \left(\frac{c}{d} + x\right)}{b(-df+cg) \left(\frac{a}{b} + x\right)}\right] \right) \Big/ \\
 & \left(d(bf-ag) \left(\frac{c}{d} + x\right) \right) + \frac{(bf-ag) \left(-\frac{abg \left(\frac{a}{b} + x\right)}{(bf-ag)^2} - \frac{b \left(\frac{a}{b} + x\right)}{bf-ag} \right) \text{PolyLog}\left[2, -\frac{bg \left(\frac{a}{b} + x\right)}{bf-ag}\right]}{bg \left(\frac{a}{b} + x\right)} + \\
 & \left(b(-df+cg) \left(\frac{a}{b} + x\right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x\right)}{b(-df+cg)^2 \left(\frac{a}{b} + x\right)} + \frac{ad \left(\frac{c}{d} + x\right)}{b(-df+cg) \left(\frac{a}{b} + x\right)} \right) \right. \\
 & \left. \text{PolyLog}\left[2, -\frac{bg \left(\frac{a}{b} + x\right)}{bf-ag}\right] \right) \Big/ \left(d(bf-ag) \left(\frac{c}{d} + x\right) \right) - \\
 & \frac{(-df+cg) \left(-\frac{cdg \left(\frac{c}{d} + x\right)}{(-df+cg)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-df+cg} \right) \text{PolyLog}\left[2, \frac{dg \left(\frac{c}{d} + x\right)}{-df+cg}\right]}{dg \left(\frac{c}{d} + x\right)} - \\
 & \left(b(-df+cg) \left(\frac{a}{b} + x\right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x\right)}{b(-df+cg)^2 \left(\frac{a}{b} + x\right)} + \frac{ad \left(\frac{c}{d} + x\right)}{b(-df+cg) \left(\frac{a}{b} + x\right)} \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{PolyLog}\left[2, \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g}\right] \Big/ \left(d (b f - a g) \left(\frac{c}{d} + x\right)\right) - \\
 & \left(b (-d f + c g) \left(\frac{a}{b} + x\right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right) \left(\text{PolyLog}\left[\right.\right. \\
 & \quad \left.\left.2, \frac{c}{d} + x\right] - \text{PolyLog}\left[2, -\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right]\right) \Big/ \left(d (b f - a g) \left(\frac{c}{d} + x\right)\right) - \\
 & \left(b (-d f + c g) \left(\frac{a}{b} + x\right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right) \right. \\
 & \quad \left. \text{PolyLog}\left[2, -\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \Big/ \left(d (b f - a g) \left(\frac{c}{d} + x\right)\right)\right] - \\
 & \frac{1}{g^2} \left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{b (f + g x)}{b f - a g}\right] + \frac{1}{2} \text{Log}\left[\frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g}\right] \right. \\
 & \quad \left. \left(-2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g}\right]\right) \left(\text{Log}\left[\frac{b (f + g x)}{b f - a g}\right] - \text{Log}\left[-\frac{d (f + g x)}{-d f + c g}\right]\right) + \\
 & \quad \text{Log}\left[\frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g}\right] \text{Log}\left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \\
 & \quad \left(-\text{Log}\left[\frac{b (f + g x)}{b f - a g}\right] + \text{Log}\left[-\frac{d (f + g x)}{-d f + c g}\right]\right) + \frac{1}{2} \text{Log}\left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right]^2 \\
 & \quad \left(\text{Log}\left[\frac{-b c + a d}{b d \left(\frac{a}{b} + x\right)}\right] + \text{Log}\left[\frac{b (f + g x)}{b f - a g}\right] - \text{Log}\left[-\frac{(-b c + a d) (f + g x)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right]\right) + \\
 & \quad \left(\text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right]\right) \text{PolyLog}\left[2, -\frac{b g \left(\frac{a}{b} + x\right)}{b f - a g}\right] + \\
 & \quad \left(\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right]\right) \text{PolyLog}\left[2, \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g}\right] + \\
 & \quad \text{Log}\left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \\
 & \quad \left(\text{PolyLog}\left[2, \frac{c}{d} + x\right] - \text{PolyLog}\left[2, -\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right]\right) -
 \end{aligned}$$

$$\text{PolyLog}\left[3, -\frac{b g \left(\frac{a}{b} + x\right)}{b f - a g}\right] - \text{PolyLog}\left[3, \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g}\right] - \left. \left. \left. \left. \left. \text{PolyLog}\left[3, \frac{\frac{c}{d} + x}{\frac{a}{b} + x}\right] + \text{PolyLog}\left[3, -\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right]\right)\right)\right)\right)\right)$$

Problem 74: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \text{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{(f + g x)^4} dx$$

Optimal (type 4, 747 leaves, 12 steps):

$$\frac{B^2 (b c - a d)^2 g^2 n^2 (c + d x)}{3 (b f - a g)^2 (d f - c g)^3 (f + g x)} - \frac{B (b c - a d) g^2 n (c + d x)^2 \left(A + B \text{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right)}{3 (b f - a g) (d f - c g)^3 (f + g x)^2} + \left(2 B (b c - a d) g (3 b d f - b c g - 2 a d g) n (a + b x) \left(A + B \text{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right)\right) / \left(3 (b f - a g)^3 (d f - c g)^2 (f + g x)\right) + \frac{b^3 \left(A + B \text{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{3 g (b f - a g)^3} - \frac{\left(A + B \text{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{3 g (f + g x)^3} + \frac{B^2 (b c - a d)^3 g^2 n^2 \text{Log}\left[\frac{a+bx}{c+dx}\right]}{3 (b f - a g)^3 (d f - c g)^3} - \frac{B^2 (b c - a d)^3 g^2 n^2 \text{Log}\left[\frac{f+gx}{c+dx}\right]}{3 (b f - a g)^3 (d f - c g)^3} + \frac{2 B^2 (b c - a d)^2 g (3 b d f - b c g - 2 a d g) n^2 \text{Log}\left[\frac{f+gx}{c+dx}\right]}{3 (b f - a g)^3 (d f - c g)^3} + \left(2 B (b c - a d) (a^2 d^2 g^2 - a b d g (3 d f - c g) + b^2 (3 d^2 f^2 - 3 c d f g + c^2 g^2)) n \left(A + B \text{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right) \text{Log}\left[1 - \frac{(d f - c g) (a + b x)}{(b f - a g) (c + d x)}\right]\right) / \left(3 (b f - a g)^3 (d f - c g)^3\right) + \left(2 B^2 (b c - a d) (a^2 d^2 g^2 - a b d g (3 d f - c g) + b^2 (3 d^2 f^2 - 3 c d f g + c^2 g^2)) n^2 \text{PolyLog}\left[2, \frac{(d f - c g) (a + b x)}{(b f - a g) (c + d x)}\right]\right) / \left(3 (b f - a g)^3 (d f - c g)^3\right)$$

Result (type 4, 55 186 leaves): Display of huge result suppressed!

Problem 75: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \text{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{(f + g x)^5} dx$$

Optimal (type 4, 1208 leaves, 15 steps):

$$\begin{aligned}
 & - \frac{B^2 (b c - a d)^2 g^3 n^2 (c + d x)^2}{12 (b f - a g)^2 (d f - c g)^4 (f + g x)^2} - \frac{B^2 (b c - a d)^3 g^3 n^2 (c + d x)}{6 (b f - a g)^3 (d f - c g)^4 (f + g x)} + \\
 & \frac{B^2 (b c - a d)^2 g^2 (4 b d f - b c g - 3 a d g) n^2 (c + d x)}{4 (b f - a g)^3 (d f - c g)^4 (f + g x)} + \\
 & \frac{B (b c - a d) g^3 n (c + d x)^3 \left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{6 (b f - a g) (d f - c g)^4 (f + g x)^3} - \\
 & \left(\frac{B (b c - a d) g^2 (4 b d f - b c g - 3 a d g) n (c + d x)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{4 (b f - a g)^2 (d f - c g)^4 (f + g x)^2} \right) + \\
 & \left(\frac{B (b c - a d) g (3 a^2 d^2 g^2 - 2 a b d g (4 d f - c g) + b^2 (6 d^2 f^2 - 4 c d f g + c^2 g^2))}{n (a + b x) \left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)} \right) / \left(2 (b f - a g)^4 (d f - c g)^3 (f + g x) \right) + \\
 & \frac{b^4 \left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)^2}{4 g (b f - a g)^4} - \frac{\left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)^2}{4 g (f + g x)^4} - \frac{B^2 (b c - a d)^4 g^3 n^2 \operatorname{Log}\left[\frac{a+b x}{c+d x} \right]}{6 (b f - a g)^4 (d f - c g)^4} + \\
 & \frac{B^2 (b c - a d)^3 g^2 (4 b d f - b c g - 3 a d g) n^2 \operatorname{Log}\left[\frac{a+b x}{c+d x} \right]}{4 (b f - a g)^4 (d f - c g)^4} + \\
 & \frac{B^2 (b c - a d)^4 g^3 n^2 \operatorname{Log}\left[\frac{f+g x}{c+d x} \right]}{6 (b f - a g)^4 (d f - c g)^4} - \frac{B^2 (b c - a d)^3 g^2 (4 b d f - b c g - 3 a d g) n^2 \operatorname{Log}\left[\frac{f+g x}{c+d x} \right]}{4 (b f - a g)^4 (d f - c g)^4} + \\
 & \left(\frac{B^2 (b c - a d)^2 g (3 a^2 d^2 g^2 - 2 a b d g (4 d f - c g) + b^2 (6 d^2 f^2 - 4 c d f g + c^2 g^2)) n^2 \operatorname{Log}\left[\frac{f+g x}{c+d x} \right]}{2 (b f - a g)^4 (d f - c g)^4} \right) / \\
 & \left(2 (b f - a g)^4 (d f - c g)^4 \right) - \\
 & \left(\frac{B (b c - a d) (2 b d f - b c g - a d g) (2 a b d^2 f g - a^2 d^2 g^2 - b^2 (2 d^2 f^2 - 2 c d f g + c^2 g^2)) n}{\left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right) \operatorname{Log}\left[1 - \frac{(d f - c g) (a + b x)}{(b f - a g) (c + d x)} \right]} \right) / \left(2 (b f - a g)^4 (d f - c g)^4 \right) - \\
 & \left(\frac{B^2 (b c - a d) (2 b d f - b c g - a d g) (2 a b d^2 f g - a^2 d^2 g^2 - b^2 (2 d^2 f^2 - 2 c d f g + c^2 g^2))}{n^2 \operatorname{PolyLog}\left[2, \frac{(d f - c g) (a + b x)}{(b f - a g) (c + d x)} \right]} \right) / \left(2 (b f - a g)^4 (d f - c g)^4 \right)
 \end{aligned}$$

Result (type 4, 142969 leaves): Display of huge result suppressed!

Problem 97: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^4 \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x} \right] \right)^2 dx$$

Optimal (type 4, 365 leaves, 8 steps):

$$\begin{aligned}
 & - \frac{B (b c - a d) g^4 (a + b x)^4 \left(A + B \operatorname{Log} \left[\frac{e (a+b x)}{c+d x} \right] \right)}{10 b d} + \\
 & \frac{g^4 (a + b x)^5 \left(A + B \operatorname{Log} \left[\frac{e (a+b x)}{c+d x} \right] \right)^2}{5 b} + \frac{B (b c - a d)^2 g^4 (a + b x)^3 \left(4 A + B + 4 B \operatorname{Log} \left[\frac{e (a+b x)}{c+d x} \right] \right)}{30 b d^2} - \\
 & \frac{B (b c - a d)^3 g^4 (a + b x)^2 \left(12 A + 7 B + 12 B \operatorname{Log} \left[\frac{e (a+b x)}{c+d x} \right] \right)}{60 b d^3} + \\
 & \frac{B (b c - a d)^4 g^4 (a + b x) \left(12 A + 13 B + 12 B \operatorname{Log} \left[\frac{e (a+b x)}{c+d x} \right] \right)}{30 b d^4} + \\
 & \frac{B (b c - a d)^5 g^4 \operatorname{Log} \left[\frac{b c - a d}{b (c+d x)} \right] \left(12 A + 25 B + 12 B \operatorname{Log} \left[\frac{e (a+b x)}{c+d x} \right] \right)}{30 b d^5} + \\
 & \frac{2 B^2 (b c - a d)^5 g^4 \operatorname{PolyLog} \left[2, \frac{d (a+b x)}{b (c+d x)} \right]}{5 b d^5}
 \end{aligned}$$

Result (type 4, 2878 leaves):

$$\begin{aligned}
 g^4 \left(- \frac{8 a^5 B^2}{5 b} + \frac{2 b^4 B^2 c^5}{5 d^5} - \frac{12 a b^3 B^2 c^4}{5 d^4} + \frac{6 a^2 b^2 B^2 c^3}{d^3} - \frac{8 a^3 b B^2 c^2}{d^2} + \frac{28 a^4 B^2 c}{5 d} + a^4 A^2 x + \right. \\
 \frac{8}{5} a^4 A B x + \frac{23}{30} a^4 B^2 x + \frac{2 A b^4 B c^4 x}{5 d^4} + \frac{13 b^4 B^2 c^4 x}{30 d^4} - \frac{2 a A b^3 B c^3 x}{d^3} - \frac{59 a b^3 B^2 c^3 x}{30 d^3} + \\
 \frac{4 a^2 A b^2 B c^2 x}{d^2} + \frac{17 a^2 b^2 B^2 c^2 x}{5 d^2} - \frac{4 a^3 A b B c x}{d} - \frac{79 a^3 b B^2 c x}{30 d} + 2 a^3 A^2 b x^2 + \frac{6}{5} a^3 A b B x^2 + \\
 \frac{13}{60} a^3 b B^2 x^2 - \frac{A b^4 B c^3 x^2}{5 d^3} - \frac{7 b^4 B^2 c^3 x^2}{60 d^3} + \frac{a A b^3 B c^2 x^2}{d^2} + \frac{9 a b^3 B^2 c^2 x^2}{20 d^2} - \frac{2 a^2 A b^2 B c x^2}{d} - \\
 \frac{11 a^2 b^2 B^2 c x^2}{20 d} + 2 a^2 A^2 b^2 x^3 + \frac{8}{15} a^2 A b^2 B x^3 + \frac{1}{30} a^2 b^2 B^2 x^3 + \frac{2 A b^4 B c^2 x^3}{15 d^2} + \frac{b^4 B^2 c^2 x^3}{30 d^2} - \\
 \frac{2 a A b^3 B c x^3}{3 d} - \frac{a b^3 B^2 c x^3}{15 d} + a A^2 b^3 x^4 + \frac{1}{10} a A b^3 B x^4 - \frac{A b^4 B c x^4}{10 d} + \frac{1}{5} A^2 b^4 x^5 + \\
 \frac{8 a^5 B^2 \operatorname{Log} \left[\frac{a}{b} + x \right]}{5 b} + \frac{2 a b^3 B^2 c^4 \operatorname{Log} \left[\frac{a}{b} + x \right]}{5 d^4} - \frac{2 a^2 b^2 B^2 c^3 \operatorname{Log} \left[\frac{a}{b} + x \right]}{d^3} + \frac{4 a^3 b B^2 c^2 \operatorname{Log} \left[\frac{a}{b} + x \right]}{d^2} - \\
 \frac{4 a^4 B^2 c \operatorname{Log} \left[\frac{a}{b} + x \right]}{d} + \frac{a^5 B^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2}{5 b} - \frac{2 b^4 B^2 c^5 \operatorname{Log} \left[\frac{c}{d} + x \right]}{5 d^5} + \frac{2 a b^3 B^2 c^4 \operatorname{Log} \left[\frac{c}{d} + x \right]}{d^4} - \\
 \frac{4 a^2 b^2 B^2 c^3 \operatorname{Log} \left[\frac{c}{d} + x \right]}{d^3} + \frac{4 a^3 b B^2 c^2 \operatorname{Log} \left[\frac{c}{d} + x \right]}{d^2} - \frac{8 a^4 B^2 c \operatorname{Log} \left[\frac{c}{d} + x \right]}{5 d} + \frac{b^4 B^2 c^5 \operatorname{Log} \left[\frac{c}{d} + x \right]^2}{5 d^5} - \\
 \frac{a b^3 B^2 c^4 \operatorname{Log} \left[\frac{c}{d} + x \right]^2}{d^4} + \frac{2 a^2 b^2 B^2 c^3 \operatorname{Log} \left[\frac{c}{d} + x \right]^2}{d^3} - \frac{2 a^3 b B^2 c^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2}{d^2} + \\
 \frac{a^4 B^2 c \operatorname{Log} \left[\frac{c}{d} + x \right]^2}{d} + \frac{2 a^5 A B \operatorname{Log} [a + b x]}{5 b} - \frac{23 a^5 B^2 \operatorname{Log} [a + b x]}{30 b} + \frac{a^2 b^2 B^2 c^3 \operatorname{Log} [a + b x]}{5 d^3} - \\
 \frac{13 a^3 b B^2 c^2 \operatorname{Log} [a + b x]}{15 d^2} + \frac{43 a^4 B^2 c \operatorname{Log} [a + b x]}{30 d} - \frac{2 a^5 B^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + b x]}{5 b} +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{2 a^5 B^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x]}{5 b}-\frac{2 a^5 B^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]}{5 b}+2 a^4 A B x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & \frac{8}{5} a^4 B^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+\frac{2 b^4 B^2 c^4 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{5 d^4}-\frac{2 a b^3 B^2 c^3 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{d^3}+ \\
 & \frac{4 a^2 b^2 B^2 c^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{d^2}-\frac{4 a^3 b B^2 c x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{d}+4 a^3 A b B x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & \frac{6}{5} a^3 b B^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-\frac{b^4 B^2 c^3 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{5 d^3}+\frac{a b^3 B^2 c^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{d^2}- \\
 & \frac{2 a^2 b^2 B^2 c x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{d}+4 a^2 A b^2 B x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+\frac{8}{15} a^2 b^2 B^2 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & \frac{2 b^4 B^2 c^2 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{15 d^2}-\frac{2 a b^3 B^2 c x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{3 d}+2 a A b^3 B x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & \frac{1}{10} a b^3 B^2 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-\frac{b^4 B^2 c x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{10 d}+\frac{2}{5} A b^4 B x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & \frac{2 a^5 B^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{5 b}+a^4 B^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2+2 a^3 b B^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2+ \\
 & 2 a^2 b^2 B^2 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2+a b^3 B^2 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2+\frac{1}{5} b^4 B^2 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2- \\
 & \frac{2 A b^4 B c^5 \operatorname{Log}[c+d x]}{5 d^5}-\frac{13 b^4 B^2 c^5 \operatorname{Log}[c+d x]}{30 d^5}+\frac{2 a A b^3 B c^4 \operatorname{Log}[c+d x]}{d^4}+ \\
 & \frac{53 a b^3 B^2 c^4 \operatorname{Log}[c+d x]}{30 d^4}-\frac{4 a^2 A b^2 B c^3 \operatorname{Log}[c+d x]}{d^3}-\frac{38 a^2 b^2 B^2 c^3 \operatorname{Log}[c+d x]}{15 d^3}+ \\
 & \frac{4 a^3 A b B c^2 \operatorname{Log}[c+d x]}{d^2}+\frac{6 a^3 b B^2 c^2 \operatorname{Log}[c+d x]}{5 d^2}-\frac{2 a^4 A B c \operatorname{Log}[c+d x]}{d}+ \\
 & \frac{2 b^4 B^2 c^5 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]}{5 d^5}-\frac{2 a b^3 B^2 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]}{d^4}+ \\
 & \frac{4 a^2 b^2 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]}{d^3}-\frac{4 a^3 b B^2 c^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]}{d^2}+ \\
 & \frac{2 a^4 B^2 c \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]}{d}-\frac{2 b^4 B^2 c^5 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]}{5 d^5}+ \\
 & \frac{2 a b^3 B^2 c^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]}{d^4}-\frac{4 a^2 b^2 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]}{d^3}+ \\
 & \frac{4 a^3 b B^2 c^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]}{d^2}-\frac{2 a^4 B^2 c \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]}{d}- \\
 & \frac{2 b^4 B^2 c^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]}{5 d^5}+\frac{2 a b^3 B^2 c^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]}{d^4}- \\
 & \frac{4 a^2 b^2 B^2 c^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]}{d^3}+\frac{4 a^3 b B^2 c^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]}{d^2}-
 \end{aligned}$$

$$\begin{aligned} & \frac{2 a^4 B^2 c \operatorname{Log}\left[\frac{e^{-(a+b x)}}{c+d x}\right] \operatorname{Log}[c+d x]}{d} - \frac{2 b^4 B^2 c^5 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{5 d^5} + \\ & \frac{2 a b^3 B^2 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^4} - \frac{4 a^2 b^2 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^3} + \\ & \frac{4 a^3 b B^2 c^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^2} - \frac{2 a^4 B^2 c \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d} - \frac{1}{5 d^5} \\ & 2 B^2 c\left(b^4 c^4-5 a b^3 c^3 d+10 a^2 b^2 c^2 d^2-10 a^3 b c d^3+5 a^4 d^4\right) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] - \\ & \left. \frac{2 a^5 B^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]}{5 b}\right) \end{aligned}$$

Problem 98: Result more than twice size of optimal antiderivative.

$$\int(a g+b g x)^3\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2 d x$$

Optimal (type 4, 309 leaves, 7 steps):

$$\begin{aligned} & \frac{B(b c-a d) g^3(a+b x)^3\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{6 b d} + \\ & \frac{g^3(a+b x)^4\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{4 b} + \frac{B(b c-a d)^2 g^3(a+b x)^2\left(3 A+B+3 B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{12 b d^2} - \\ & \frac{B(b c-a d)^3 g^3(a+b x)\left(6 A+5 B+6 B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{12 b d^3} - \\ & \frac{B(b c-a d)^4 g^3 \operatorname{Log}\left[\frac{b c-a d}{b(c+d x)}\right]\left(6 A+11 B+6 B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{12 b d^4} - \frac{B^2(b c-a d)^4 g^3 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{2 b d^4} \end{aligned}$$

Result (type 4, 2110 leaves):

$$\begin{aligned} & \frac{1}{12 b d^4} \\ & g^3\left(-6 b^4 B^2 c^4+30 a b^3 B^2 c^3 d-60 a^2 b^2 B^2 c^2 d^2+54 a^3 b B^2 c d^3-18 a^4 B^2 d^4-6 A b^4 B c^3 d x-5 b^4 B^2 c^3\right. \\ & d x+24 a A b^3 B c^2 d^2 x+17 a b^3 B^2 c^2 d^2 x-36 a^2 A b^2 B c d^3 x-19 a^2 b^2 B^2 c d^3 x+12 a^3 A^2 b d^4 x+ \\ & 18 a^3 A b B d^4 x+7 a^3 b B^2 d^4 x+3 A b^4 B c^2 d^2 x^2+b^4 B^2 c^2 d^2 x^2-12 a A b^3 B c d^3 x^2-2 a b^3 B^2 c d^3 x^2+ \\ & 18 a^2 A^2 b^2 d^4 x^2+9 a^2 A b^2 B d^4 x^2+a^2 b^2 B^2 d^4 x^2-2 A b^4 B c d^3 x^3+12 a A^2 b^3 d^4 x^3+2 a A b^3 B d^4 x^3+ \\ & 3 A^2 b^4 d^4 x^4-6 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b}+x\right]+24 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right]-36 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{a}{b}+x\right]+ \\ & 18 a^4 B^2 d^4 \operatorname{Log}\left[\frac{a}{b}+x\right]+3 a^4 B^2 d^4 \operatorname{Log}\left[\frac{a}{b}+x\right]^2+6 b^4 B^2 c^4 \operatorname{Log}\left[\frac{c}{d}+x\right]-24 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{c}{d}+x\right]+ \\ & 36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{c}{d}+x\right]-18 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{c}{d}+x\right]-3 b^4 B^2 c^4 \operatorname{Log}\left[\frac{c}{d}+x\right]^2+ \\ & \left. 12 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{c}{d}+x\right]^2-18 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2+12 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2-\right) \end{aligned}$$

$$\begin{aligned}
 & 3 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}[a+b x] + 10 a^3 b B^2 c d^3 \operatorname{Log}[a+b x] + 6 a^4 A B d^4 \operatorname{Log}[a+b x] - \\
 & 7 a^4 B^2 d^4 \operatorname{Log}[a+b x] - 6 a^4 B^2 d^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x] + 6 a^4 B^2 d^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] - \\
 & 6 a^4 B^2 d^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] - 6 b^4 B^2 c^3 d x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 24 a b^3 B^2 c^2 d^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 36 a^2 b^2 B^2 c d^3 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 24 a^3 A b B d^4 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 18 a^3 b B^2 d^4 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 3 b^4 B^2 c^2 d^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 12 a b^3 B^2 c d^3 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 36 a^2 A b^2 B d^4 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 9 a^2 b^2 B^2 d^4 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \\
 & 2 b^4 B^2 c d^3 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 24 a A b^3 B d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 2 a b^3 B^2 d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 6 A b^4 B d^4 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 6 a^4 B^2 d^4 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 12 a^3 b B^2 d^4 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 18 a^2 b^2 B^2 d^4 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 12 a b^3 B^2 d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 3 b^4 B^2 d^4 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 6 A b^4 B c^4 \operatorname{Log}[c+d x] + 5 b^4 B^2 c^4 \operatorname{Log}[c+d x] - \\
 & 24 a A b^3 B c^3 d \operatorname{Log}[c+d x] - 14 a b^3 B^2 c^3 d \operatorname{Log}[c+d x] + 36 a^2 A b^2 B c^2 d^2 \operatorname{Log}[c+d x] + \\
 & 9 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}[c+d x] - 24 a^3 A b B c d^3 \operatorname{Log}[c+d x] - 6 b^4 B^2 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + \\
 & 24 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] - 36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + \\
 & 24 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + 6 b^4 B^2 c^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - \\
 & 24 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] + 36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - \\
 & 24 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] + 6 b^4 B^2 c^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] - \\
 & 24 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] + 36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] - \\
 & 24 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] + 6 b^4 B^2 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
 & 24 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
 & 24 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 6 b B^2 c \left(b^3 c^3 - 4 a b^2 c^2 d + 6 a^2 b c d^2 - 4 a^3 d^3\right) \\
 & \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] - 6 a^4 B^2 d^4 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]
 \end{aligned}$$

Problem 99: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^2 \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)^2 dx$$

Optimal (type 4, 253 leaves, 6 steps):

$$\begin{aligned} & -\frac{B(b c-a d) g^2(a+b x)^2\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{3 b d}+ \\ & \frac{g^2(a+b x)^3\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{3 b}+\frac{B(b c-a d)^2 g^2(a+b x)\left(2 A+B+2 B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{3 b d^2}+ \\ & \frac{B(b c-a d)^3 g^2 \operatorname{Log}\left[\frac{b c-a d}{b(c+d x)}\right]\left(2 A+3 B+2 B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{3 b d^3}+\frac{2 B^2(b c-a d)^3 g^2 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{3 b d^3} \end{aligned}$$

Result (type 4, 1292 leaves):

$$\begin{aligned} & g^2\left(a^2 A^2 x+a A^2 b x^2+\frac{1}{3} A^2 b^2 x^3+\frac{2 a^2 A B\left(a d \operatorname{Log}[a+b x]+b d x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-b c \operatorname{Log}[c+d x]\right)}{b d}+\right. \\ & \left.\frac{1}{3} A b^2 B\left(\frac{(b c-a d) x(2 b c+2 a d-b d x)}{b^2 d^2}+\right.\right. \\ & \left.\left.\frac{2 a^3 \operatorname{Log}[a+b x]}{b^3}+2 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-\frac{2 c^3 \operatorname{Log}[c+d x]}{d^3}\right)\right)+ \\ & 2 a A B\left(a x-\frac{b c x}{d}-\frac{a^2 \operatorname{Log}[a+b x]}{b}+b x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+\frac{b c^2 \operatorname{Log}[c+d x]}{d^2}\right)+ \\ & \frac{1}{b d} a^2 B^2\left(a d \operatorname{Log}\left[\frac{a}{b}+x\right]^2+b c \operatorname{Log}\left[\frac{c}{d}+x\right]^2-2 a d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x]+ \right. \\ & \left. 2 a d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x]-2 a d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+ \right. \\ & \left. 2 a d \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+b d x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2+2 b c \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]- \right. \\ & \left. 2 b c \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]-2 b c \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]-2 b c \operatorname{Log}\left[\frac{a}{b}+x\right] \right. \\ & \left. \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]-2 b c \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]-2 a d \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right)+ \\ & \frac{1}{b d^2} a B^2\left(2 d(-b c+a d)(a+b x)\left(-1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)-a^2 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2+\right. \\ & \left. 2 b(b c-a d)(c+d x)\left(-1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)-b^2 c^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2+\right. \\ & \left. b^2 d^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2+2\left(\operatorname{Log}\left[\frac{a}{b}+x\right]-\operatorname{Log}\left[\frac{c}{d}+x\right]-\operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)\right) \\ & \left.\left(a^2 d^2 \operatorname{Log}[a+b x]-b(d(-b c+a d) x+b c^2 \operatorname{Log}[c+d x])\right)\right)+ \end{aligned}$$

$$\begin{aligned}
 & 2 b^2 c^2 \left(\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{b(c+d x)}{b c - a d} \right] + \text{PolyLog} \left[2, \frac{d(a+b x)}{-b c + a d} \right] \right) + \\
 & 2 a^2 d^2 \left(\text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d(a+b x)}{-b c + a d} \right] + \text{PolyLog} \left[2, \frac{b(c+d x)}{b c - a d} \right] \right) + \\
 & b^2 B^2 \left(\frac{1}{3} x^3 \text{Log} \left[\frac{e(a+b x)}{c+d x} \right]^2 - \frac{1}{6 b^3 d^3} \left(4 d(-b c + a d)(b c + a d)(a+b x) \left(-1 + \text{Log} \left[\frac{a}{b} + x \right] \right) - \right. \right. \\
 & \quad 2 a^3 d^3 \text{Log} \left[\frac{a}{b} + x \right]^2 + 4 b(b c - a d)(b c + a d)(c+d x) \left(-1 + \text{Log} \left[\frac{c}{d} + x \right] \right) - \\
 & \quad 2 b^3 c^3 \text{Log} \left[\frac{c}{d} + x \right]^2 + d^2(b c - a d) \left(b x(2 a - b x) + 2 b^2 x^2 \text{Log} \left[\frac{a}{b} + x \right] - 2 a^2 \text{Log} [a+b x] \right) + \\
 & \quad \left. b^2(b c - a d) \left(d x(-2 c + d x) - 2 d^2 x^2 \text{Log} \left[\frac{c}{d} + x \right] + 2 c^2 \text{Log} [c+d x] \right) - \right. \\
 & \quad \left. 2 \left(\text{Log} \left[\frac{a}{b} + x \right] - \text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[\frac{e(a+b x)}{c+d x} \right] \right) \right. \\
 & \quad \left. (b d(b c - a d) x(-2 b c - 2 a d + b d x) - 2 a^3 d^3 \text{Log} [a+b x] + 2 b^3 c^3 \text{Log} [c+d x]) + \right. \\
 & \quad \left. 4 b^3 c^3 \left(\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{b(c+d x)}{b c - a d} \right] + \text{PolyLog} \left[2, \frac{d(a+b x)}{-b c + a d} \right] \right) + \right. \\
 & \quad \left. \left. 4 a^3 d^3 \left(\text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d(a+b x)}{-b c + a d} \right] + \text{PolyLog} \left[2, \frac{b(c+d x)}{b c - a d} \right] \right) \right) \right)
 \end{aligned}$$

Problem 100: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x) \left(A + B \text{Log} \left[\frac{e(a+b x)}{c+d x} \right] \right)^2 dx$$

Optimal (type 4, 180 leaves, 5 steps):

$$\begin{aligned}
 & - \frac{B(b c - a d) g(a+b x) \left(A + B \text{Log} \left[\frac{e(a+b x)}{c+d x} \right] \right)}{b d} + \frac{g(a+b x)^2 \left(A + B \text{Log} \left[\frac{e(a+b x)}{c+d x} \right] \right)^2}{2 b} - \\
 & \frac{B(b c - a d)^2 g \text{Log} \left[\frac{b c - a d}{b(c+d x)} \right] \left(A + B + B \text{Log} \left[\frac{e(a+b x)}{c+d x} \right] \right)}{b d^2} - \frac{B^2(b c - a d)^2 g \text{PolyLog} \left[2, \frac{d(a+b x)}{b(c+d x)} \right]}{b d^2}
 \end{aligned}$$

Result (type 4, 733 leaves):

$$\begin{aligned}
 & g \left(a A^2 x + \frac{1}{2} A^2 b x^2 + \frac{2 a A B \left(a d \operatorname{Log}[a+b x] + b d x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - b c \operatorname{Log}[c+d x]\right)}{b d} + \right. \\
 & A B \left(a x - \frac{b c x}{d} - \frac{a^2 \operatorname{Log}[a+b x]}{b} + b x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \frac{b c^2 \operatorname{Log}[c+d x]}{d^2} \right) + \\
 & \frac{1}{b d} a B^2 \left(a d \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + b c \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2 a d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x] + 2 a d \operatorname{Log}\left[\frac{c}{d}+x\right] \right. \\
 & \quad \left. \operatorname{Log}[a+b x] - 2 a d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + 2 a d \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \right. \\
 & b d x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 2 b c \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] - 2 b c \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - \\
 & 2 b c \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] - 2 b c \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
 & \left. 2 b c \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] - 2 a d \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) + \frac{1}{2} b B^2 \\
 & \left(x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 - \frac{1}{b^2 d^2} \left(-2 d(-b c+a d)(a+b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b}+x\right] \right) + a^2 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 - \right. \right. \\
 & \quad \left. \left. 2 b(b c-a d)(c+d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d}+x\right] \right) + b^2 c^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2 \left(\operatorname{Log}\left[\frac{a}{b}+x\right] - \operatorname{Log}\left[\frac{c}{d}+x\right] - \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right) \left(a^2 d^2 \operatorname{Log}[a+b x] - b(d(-b c+a d)x + b c^2 \operatorname{Log}[c+d x]) \right) \right) - \right. \\
 & \left. 2 b^2 c^2 \left(\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) - \right. \\
 & \left. \left. 2 a^2 d^2 \left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) \right) \right)
 \end{aligned}$$

Problem 101: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)^2}{a g + b g x} dx$$

Optimal (type 4, 128 leaves, 4 steps):

$$\begin{aligned}
 & - \frac{\left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)^2 \operatorname{Log}\left[1 - \frac{b(c+d x)}{d(a+b x)}\right]}{b g} + \\
 & \frac{2 B \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]}{b g} + \frac{2 B^2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{d(a+b x)}\right]}{b g}
 \end{aligned}$$

Result (type 4, 458 leaves):

$$\frac{1}{3 b g} \left(3 A^2 \operatorname{Log}[a+b x] + 3 A B \left(\operatorname{Log}\left[\frac{a}{b}+x\right]^2 - 2 \operatorname{Log}[a+b x] \left(\operatorname{Log}\left[\frac{a}{b}+x\right] - \operatorname{Log}\left[\frac{c}{d}+x\right] - \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right) - 2 \left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) \right) + B^2 \left(\operatorname{Log}\left[\frac{a}{b}+x\right]^3 + 3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + 3 \operatorname{Log}[a+b x] \left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)^2 + 3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \left(-\operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \right) + 6 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] + 6 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] - 3 \left(\operatorname{Log}\left[\frac{a}{b}+x\right] - \operatorname{Log}\left[\frac{c}{d}+x\right] - \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right) \left(\operatorname{Log}\left[\frac{a}{b}+x\right]^2 - 2 \left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) \right) - 6 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] - 6 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right] \right)$$

Problem 106: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}\left[\frac{d(a+b x)}{b(c+d x)}\right]}{c f+d f x} d x$$

Optimal (type 4, 28 leaves, 1 step):

$$\frac{\operatorname{PolyLog}\left[2, \frac{b c-a d}{b(c+d x)}\right]}{d f}$$

Result (type 4, 130 leaves):

$$\frac{1}{2 d f} \left(-\operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + 2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] + 2 \operatorname{Log}\left[\frac{d(a+b x)}{b(c+d x)}\right] \operatorname{Log}[c+d x] + 2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 2 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right)$$

Problem 128: Result more than twice size of optimal antiderivative.

$$\int (a g+b g x)^4 \left(A+B \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \right)^2 d x$$

Optimal (type 4, 377 leaves, 8 steps):

$$\begin{aligned}
 & - \frac{B (b c - a d) g^4 (a + b x)^4 \left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)}{5 b d} + \frac{g^4 (a + b x)^5 \left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)^2}{5 b} + \\
 & \frac{2 B (b c - a d)^2 g^4 (a + b x)^3 \left(2 A + B + 2 B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)}{15 b d^2} - \\
 & \frac{B (b c - a d)^3 g^4 (a + b x)^2 \left(6 A + 7 B + 6 B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)}{15 b d^3} + \\
 & \frac{2 B (b c - a d)^4 g^4 (a + b x) \left(6 A + 13 B + 6 B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)}{15 b d^4} + \\
 & \frac{2 B (b c - a d)^5 g^4 \left(6 A + 25 B + 6 B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right) \operatorname{Log} \left[\frac{b c - a d}{b (c+d x)} \right]}{15 b d^5} + \\
 & \frac{8 B^2 (b c - a d)^5 g^4 \operatorname{PolyLog} \left[2, \frac{d (a+b x)}{b (c+d x)} \right]}{5 b d^5}
 \end{aligned}$$

Result (type 4, 2907 leaves):

$$\begin{aligned}
 & \frac{1}{15 b d^5} \\
 & g^4 \left(24 b^5 B^2 c^5 - 144 a b^4 B^2 c^4 d + 360 a^2 b^3 B^2 c^3 d^2 - 480 a^3 b^2 B^2 c^2 d^3 + 336 a^4 b B^2 c d^4 - 96 a^5 B^2 d^5 + \right. \\
 & 12 A b^5 B c^4 d x + 26 b^5 B^2 c^4 d x - 60 a A b^4 B c^3 d^2 x - 118 a b^4 B^2 c^3 d^2 x + 120 a^2 A b^3 B c^2 d^3 x + \\
 & 204 a^2 b^3 B^2 c^2 d^3 x - 120 a^3 A b^2 B c d^4 x - 158 a^3 b^2 B^2 c d^4 x + 15 a^4 A^2 b d^5 x + 48 a^4 A b B d^5 x + \\
 & 46 a^4 b B^2 d^5 x - 6 A b^5 B c^3 d^2 x^2 - 7 b^5 B^2 c^3 d^2 x^2 + 30 a A b^4 B c^2 d^3 x^2 + 27 a b^4 B^2 c^2 d^3 x^2 - \\
 & 60 a^2 A b^3 B c d^4 x^2 - 33 a^2 b^3 B^2 c d^4 x^2 + 30 a^3 A^2 b^2 d^5 x^2 + 36 a^3 A b^2 B d^5 x^2 + \\
 & 13 a^3 b^2 B^2 d^5 x^2 + 4 A b^5 B c^2 d^3 x^3 + 2 b^5 B^2 c^2 d^3 x^3 - 20 a A b^4 B c d^4 x^3 - 4 a b^4 B^2 c d^4 x^3 + \\
 & 30 a^2 A^2 b^3 d^5 x^3 + 16 a^2 A b^3 B d^5 x^3 + 2 a^2 b^3 B^2 d^5 x^3 - 3 A b^5 B c d^4 x^4 + 15 a A^2 b^4 d^5 x^4 + \\
 & 3 a A b^4 B d^5 x^4 + 3 A^2 b^5 d^5 x^5 + 24 a b^4 B^2 c^4 d \operatorname{Log} \left[\frac{a}{b} + x \right] - 120 a^2 b^3 B^2 c^3 d^2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \\
 & 240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log} \left[\frac{a}{b} + x \right] - 240 a^4 b B^2 c d^4 \operatorname{Log} \left[\frac{a}{b} + x \right] + 96 a^5 B^2 d^5 \operatorname{Log} \left[\frac{a}{b} + x \right] + \\
 & 12 a^5 B^2 d^5 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - 24 b^5 B^2 c^5 \operatorname{Log} \left[\frac{c}{d} + x \right] + 120 a b^4 B^2 c^4 d \operatorname{Log} \left[\frac{c}{d} + x \right] - \\
 & 240 a^2 b^3 B^2 c^3 d^2 \operatorname{Log} \left[\frac{c}{d} + x \right] + 240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log} \left[\frac{c}{d} + x \right] - 96 a^4 b B^2 c d^4 \operatorname{Log} \left[\frac{c}{d} + x \right] + \\
 & 12 b^5 B^2 c^5 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 60 a b^4 B^2 c^4 d \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 120 a^2 b^3 B^2 c^3 d^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - \\
 & 120 a^3 b^2 B^2 c^2 d^3 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 60 a^4 b B^2 c d^4 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 12 a^2 b^3 B^2 c^3 d^2 \operatorname{Log} [a + b x] - \\
 & 52 a^3 b^2 B^2 c^2 d^3 \operatorname{Log} [a + b x] + 86 a^4 b B^2 c d^4 \operatorname{Log} [a + b x] + 12 a^5 A B d^5 \operatorname{Log} [a + b x] - \\
 & 46 a^5 B^2 d^5 \operatorname{Log} [a + b x] - 24 a^5 B^2 d^5 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + b x] + 24 a^5 B^2 d^5 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + b x] - \\
 & 24 a^5 B^2 d^5 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + 12 b^5 B^2 c^4 d x \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] - \\
 & 60 a b^4 B^2 c^3 d^2 x \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] + 120 a^2 b^3 B^2 c^2 d^3 x \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] -
 \end{aligned}$$

$$\begin{aligned}
 & 120 a^3 b^2 B^2 c d^4 x \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + 30 a^4 A b B d^5 x \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + \\
 & 48 a^4 b B^2 d^5 x \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] - 6 b^5 B^2 c^3 d^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + \\
 & 30 a b^4 B^2 c^2 d^3 x^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] - 60 a^2 b^3 B^2 c d^4 x^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + \\
 & 60 a^3 A b^2 B d^5 x^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + 36 a^3 b^2 B^2 d^5 x^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + \\
 & 4 b^5 B^2 c^2 d^3 x^3 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] - 20 a b^4 B^2 c d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + \\
 & 60 a^2 A b^3 B d^5 x^3 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + 16 a^2 b^3 B^2 d^5 x^3 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] - \\
 & 3 b^5 B^2 c d^4 x^4 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + 30 a A b^4 B d^5 x^4 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + \\
 & 3 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + 6 A b^5 B d^5 x^5 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + \\
 & 12 a^5 B^2 d^5 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + 15 a^4 b B^2 d^5 x \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]^2 + \\
 & 30 a^3 b^2 B^2 d^5 x^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]^2 + 30 a^2 b^3 B^2 d^5 x^3 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]^2 + \\
 & 15 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]^2 + 3 b^5 B^2 d^5 x^5 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]^2 - \\
 & 12 A b^5 B c^5 \operatorname{Log}[c+d x] - 26 b^5 B^2 c^5 \operatorname{Log}[c+d x] + 60 a A b^4 B c^4 d \operatorname{Log}[c+d x] + \\
 & 106 a b^4 B^2 c^4 d \operatorname{Log}[c+d x] - 120 a^2 A b^3 B c^3 d^2 \operatorname{Log}[c+d x] - 152 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}[c+d x] + \\
 & 120 a^3 A b^2 B c^2 d^3 \operatorname{Log}[c+d x] + 72 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}[c+d x] - 60 a^4 A b B c d^4 \operatorname{Log}[c+d x] + \\
 & 24 b^5 B^2 c^5 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] - 120 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + \\
 & 240 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] - 240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + \\
 & 120 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] - 24 b^5 B^2 c^5 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] + \\
 & 120 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - 240 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] + \\
 & 240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - 120 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - \\
 & 12 b^5 B^2 c^5 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \operatorname{Log}[c+d x] + 60 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \operatorname{Log}[c+d x] - \\
 & 120 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \operatorname{Log}[c+d x] + 120 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \operatorname{Log}[c+d x] -
 \end{aligned}$$

$$\begin{aligned}
 & 60 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \operatorname{Log}[c+d x] - 24 b^5 B^2 c^5 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 & 120 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 240 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 & 240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 120 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
 & 24 b B^2 c\left(b^4 c^4-5 a b^3 c^3 d+10 a^2 b^2 c^2 d^2-10 a^3 b c d^3+5 a^4 d^4\right) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] - \\
 & 24 a^5 B^2 d^5 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]
 \end{aligned}$$

Problem 129: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^3 \left(A + B \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \right)^2 dx$$

Optimal (type 4, 319 leaves, 7 steps):

$$\begin{aligned}
 & -\frac{B(b c-a d) g^3(a+b x)^3\left(A+B \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]\right)}{3 b d} + \frac{g^3(a+b x)^4\left(A+B \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]\right)^2}{4 b} + \\
 & \frac{B(b c-a d)^2 g^3(a+b x)^2\left(3 A+2 B+3 B \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]\right)}{6 b d^2} - \\
 & \frac{B(b c-a d)^3 g^3(a+b x)\left(3 A+5 B+3 B \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]\right)}{3 b d^3} - \\
 & \frac{B(b c-a d)^4 g^3\left(3 A+11 B+3 B \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]\right) \operatorname{Log}\left[\frac{b c-a d}{b(c+d x)}\right]}{3 b d^4} - \\
 & \frac{2 B^2(b c-a d)^4 g^3 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{b d^4}
 \end{aligned}$$

Result (type 4, 2125 leaves):

$$\begin{aligned}
 & g^3 \left(-\frac{6 a^4 B^2}{b} - \frac{2 b^3 B^2 c^4}{d^4} + \frac{10 a b^2 B^2 c^3}{d^3} - \frac{20 a^2 b B^2 c^2}{d^2} + \frac{18 a^3 B^2 c}{d} + a^3 A^2 x + \right. \\
 & 3 a^3 A B x + \frac{7}{3} a^3 B^2 x - \frac{A b^3 B c^3 x}{d^3} - \frac{5 b^3 B^2 c^3 x}{3 d^3} + \frac{4 a A b^2 B c^2 x}{d^2} + \frac{17 a b^2 B^2 c^2 x}{3 d^2} - \\
 & \frac{6 a^2 A b B c x}{d} - \frac{19 a^2 b B^2 c x}{3 d} + \frac{3}{2} a^2 A^2 b x^2 + \frac{3}{2} a^2 A b B x^2 + \frac{1}{3} a^2 b B^2 x^2 + \frac{A b^3 B c^2 x^2}{2 d^2} + \\
 & \frac{b^3 B^2 c^2 x^2}{3 d^2} - \frac{2 a A b^2 B c x^2}{d} - \frac{2 a b^2 B^2 c x^2}{3 d} + a A^2 b^2 x^3 + \frac{1}{3} a A b^2 B x^3 - \frac{A b^3 B c x^3}{3 d} + \\
 & \left. \frac{1}{4} A^2 b^3 x^4 + \frac{6 a^4 B^2 \operatorname{Log}\left[\frac{a}{b}+x\right]}{b} - \frac{2 a b^2 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right]}{d^3} + \frac{8 a^2 b B^2 c^2 \operatorname{Log}\left[\frac{a}{b}+x\right]}{d^2} - \right)
 \end{aligned}$$

$$\begin{aligned}
 & \frac{12 a^3 B^2 c \operatorname{Log}\left[\frac{a}{b}+x\right]}{d} + \frac{a^4 B^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2}{b} + \frac{2 b^3 B^2 c^4 \operatorname{Log}\left[\frac{c}{d}+x\right]}{d^4} - \frac{8 a b^2 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right]}{d^3} + \\
 & \frac{12 a^2 b B^2 c^2 \operatorname{Log}\left[\frac{c}{d}+x\right]}{d^2} - \frac{6 a^3 B^2 c \operatorname{Log}\left[\frac{c}{d}+x\right]}{d} - \frac{b^3 B^2 c^4 \operatorname{Log}\left[\frac{c}{d}+x\right]^2}{d^4} + \frac{4 a b^2 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2}{d^3} - \\
 & \frac{6 a^2 b B^2 c^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2}{d^2} + \frac{4 a^3 B^2 c \operatorname{Log}\left[\frac{c}{d}+x\right]^2}{d} + \frac{a^4 A B \operatorname{Log}[a+b x]}{b} - \frac{7 a^4 B^2 \operatorname{Log}[a+b x]}{3 b} - \\
 & \frac{a^2 b B^2 c^2 \operatorname{Log}[a+b x]}{d^2} + \frac{10 a^3 B^2 c \operatorname{Log}[a+b x]}{3 d} - \frac{2 a^4 B^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x]}{b} + \\
 & \frac{2 a^4 B^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x]}{b} - \frac{2 a^4 B^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]}{b} + 2 a^3 A B x \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + \\
 & 3 a^3 B^2 x \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] - \frac{b^3 B^2 c^3 x \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]}{d^3} + \frac{4 a b^2 B^2 c^2 x \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]}{d^2} - \\
 & \frac{6 a^2 b B^2 c x \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]}{d} + 3 a^2 A b B x^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + \frac{3}{2} a^2 b B^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + \\
 & \frac{b^3 B^2 c^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]}{2 d^2} - \frac{2 a b^2 B^2 c x^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]}{d} + 2 a A b^2 B x^3 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + \\
 & \frac{1}{3} a b^2 B^2 x^3 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] - \frac{b^3 B^2 c x^3 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]}{3 d} + \frac{1}{2} A b^3 B x^4 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + \\
 & \frac{a^4 B^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]}{b} + a^3 B^2 x \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]^2 + \frac{3}{2} a^2 b B^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]^2 + \\
 & a b^2 B^2 x^3 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]^2 + \frac{1}{4} b^3 B^2 x^4 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]^2 + \frac{A b^3 B c^4 \operatorname{Log}[c+d x]}{d^4} + \\
 & \frac{5 b^3 B^2 c^4 \operatorname{Log}[c+d x]}{3 d^4} - \frac{4 a A b^2 B c^3 \operatorname{Log}[c+d x]}{d^3} - \frac{14 a b^2 B^2 c^3 \operatorname{Log}[c+d x]}{3 d^3} + \\
 & \frac{6 a^2 A b B c^2 \operatorname{Log}[c+d x]}{d^2} + \frac{3 a^2 b B^2 c^2 \operatorname{Log}[c+d x]}{d^2} - \frac{4 a^3 A B c \operatorname{Log}[c+d x]}{d} - \\
 & \frac{2 b^3 B^2 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]}{d^4} + \frac{8 a b^2 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]}{d^3} - \\
 & \frac{12 a^2 b B^2 c^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]}{d^2} + \frac{8 a^3 B^2 c \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]}{d} + \\
 & \frac{2 b^3 B^2 c^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]}{d^4} - \frac{8 a b^2 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]}{d^3} + \\
 & \frac{12 a^2 b B^2 c^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]}{d^2} - \frac{8 a^3 B^2 c \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]}{d} +
 \end{aligned}$$

$$\begin{aligned} & \frac{b^3 B^2 c^4 \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right] \operatorname{Log}[c+dx]}{d^4} - \frac{4 a b^2 B^2 c^3 \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right] \operatorname{Log}[c+dx]}{d^3} + \\ & \frac{6 a^2 b B^2 c^2 \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right] \operatorname{Log}[c+dx]}{d^2} - \frac{4 a^3 B^2 c \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right] \operatorname{Log}[c+dx]}{d} + \\ & \frac{2 b^3 B^2 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right]}{d^4} - \frac{8 a b^2 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right]}{d^3} + \\ & \frac{12 a^2 b B^2 c^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right]}{d^2} - \frac{8 a^3 B^2 c \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right]}{d} + \\ & \frac{2 B^2 c \left(b^3 c^3 - 4 a b^2 c^2 d + 6 a^2 b c d^2 - 4 a^3 d^3\right) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]}{d^4} - \frac{2 a^4 B^2 \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]}{b} \end{aligned}$$

Problem 130: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^2 \left(A + B \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right] \right)^2 dx$$

Optimal (type 4, 255 leaves, 6 steps):

$$\begin{aligned} & - \frac{2 B (b c - a d) g^2 (a + b x)^2 \left(A + B \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right] \right)}{3 b d} + \\ & \frac{g^2 (a + b x)^3 \left(A + B \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right] \right)^2}{3 b} + \frac{4 B (b c - a d)^2 g^2 (a + b x) \left(A + B + B \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right] \right)}{3 b d^2} + \\ & \frac{4 B (b c - a d)^3 g^2 \left(A + 3 B + B \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right] \right) \operatorname{Log}\left[\frac{b c - a d}{b(c+dx)}\right]}{3 b d^3} + \frac{8 B^2 (b c - a d)^3 g^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{3 b d^3} \end{aligned}$$

Result (type 4, 1316 leaves):

$$\begin{aligned} & g^2 \left(a^2 A^2 x + a A^2 b x^2 + \frac{1}{3} A^2 b^2 x^3 + \right. \\ & \frac{2 a^2 A B \left(2 a d \operatorname{Log}[a + b x] + b d x \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right] - 2 b c \operatorname{Log}[c + d x] \right)}{b d} + \frac{2}{3} A b^2 B \\ & \left. \left(\frac{(b c - a d) x (2 b c + 2 a d - b d x)}{b^2 d^2} + \frac{2 a^3 \operatorname{Log}[a + b x]}{b^3} + x^3 \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right] - \frac{2 c^3 \operatorname{Log}[c + d x]}{d^3} \right) + \right. \\ & 2 a A B \left(2 a x - \frac{2 b c x}{d} - \frac{2 a^2 \operatorname{Log}[a + b x]}{b} + b x^2 \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right] + \frac{2 b c^2 \operatorname{Log}[c + d x]}{d^2} \right) + \\ & \left. \frac{1}{b d} a^2 B^2 \left(4 a d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 4 b c \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 8 a d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + \right. \right. \end{aligned}$$

$$\begin{aligned}
 & 8 a d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x]-8 a d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+ \\
 & 4 a d \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]+b d x \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]^2+8 b c \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]- \\
 & 8 b c \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]-4 b c \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \operatorname{Log}[c+d x]-8 b c \operatorname{Log}\left[\frac{a}{b}+x\right] \\
 & \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]-8 b c \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]-8 a d \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]+ \\
 & \frac{1}{b} a B^2\left(b^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]^2-\frac{1}{d^2} 4\left(-2 d(-b c+a d)(a+b x)\left(-1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)+\right. \\
 & \left.a^2 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2-2 b(b c-a d)(c+d x)\left(-1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)+\right. \\
 & \left.b^2 c^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2-\left(2 \operatorname{Log}\left[\frac{a}{b}+x\right]-2 \operatorname{Log}\left[\frac{c}{d}+x\right]-\operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]\right)\right. \\
 & \left.\left(a^2 d^2 \operatorname{Log}[a+b x]-b(d(-b c+a d) x+b c^2 \operatorname{Log}[c+d x])\right)\right)- \\
 & 2 b^2 c^2\left(\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+\operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)- \\
 & 2 a^2 d^2\left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+\operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right)\left.\right)+ \\
 & \frac{1}{3} b^2 B^2\left(x^3 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]^2-\frac{1}{b^3 d^3} 2\left(4 d(-b c+a d)(b c+a d)(a+b x)\left(-1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)-\right. \\
 & \left.2 a^3 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2+4 b(b c-a d)(b c+a d)(c+d x)\left(-1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)-\right. \\
 & \left.2 b^3 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2+d^2(b c-a d)\left(b x(2 a-b x)+2 b^2 x^2 \operatorname{Log}\left[\frac{a}{b}+x\right]-2 a^2 \operatorname{Log}[a+b x]\right)+\right. \\
 & \left.b^2(b c-a d)\left(d x(-2 c+d x)-2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d}+x\right]+2 c^2 \operatorname{Log}[c+d x]\right)-\right. \\
 & \left.\left(2 \operatorname{Log}\left[\frac{a}{b}+x\right]-2 \operatorname{Log}\left[\frac{c}{d}+x\right]-\operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]\right)\right. \\
 & \left.\left(b d(b c-a d) x(-2 b c-2 a d+b d x)-2 a^3 d^3 \operatorname{Log}[a+b x]+2 b^3 c^3 \operatorname{Log}[c+d x]\right)+\right. \\
 & \left.4 b^3 c^3\left(\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+\operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)+\right. \\
 & \left.4 a^3 d^3\left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+\operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right)\left.\right)\left.\right)
 \end{aligned}$$

Problem 131: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x) \left(A + B \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \right)^2 dx$$

Optimal (type 4, 188 leaves, 5 steps):

$$\frac{2 B (b c - a d) g (a + b x) \left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)}{b d} + \frac{g (a + b x)^2 \left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)^2}{2 b} - \frac{2 B (b c - a d)^2 g \left(A + 2 B + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right) \operatorname{Log} \left[\frac{b c - a d}{b (c+d x)} \right]}{b d^2} - \frac{4 B^2 (b c - a d)^2 g \operatorname{PolyLog} \left[2, \frac{d (a+b x)}{b (c+d x)} \right]}{b d^2}$$

Result (type 4, 849 leaves):

$$g \left(a A^2 x + \frac{1}{2} A^2 b x^2 + 2 a A B \left(\frac{2 (b c - a d) (a d \operatorname{Log} [a + b x] - b c \operatorname{Log} [c + d x])}{b^2 c d - a b d^2} + x \operatorname{Log} \left[\frac{a^2 e + 2 a b e x + b^2 e x^2}{(c + d x)^2} \right] \right) + 2 A b B \left(- (b c - a d) \left(\frac{x}{b d} + \frac{a^2 \operatorname{Log} [a + b x]}{b^2 (b c - a d)} - \frac{c^2 \operatorname{Log} [c + d x]}{d^2 (b c - a d)} \right) + \frac{1}{2} x^2 \operatorname{Log} \left[\frac{a^2 e + 2 a b e x + b^2 e x^2}{(c + d x)^2} \right] \right) + a B^2 \left(x \operatorname{Log} \left[\frac{a^2 e + 2 a b e x + b^2 e x^2}{(c + d x)^2} \right]^2 - \frac{1}{b d} 4 \left(- a d \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - b c \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 2 a d \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + b x] - 2 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + b x] + 2 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] - a d \operatorname{Log} [a + b x] \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] - 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [c + d x] + 2 b c \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [c + d x] + b c \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \operatorname{Log} [c + d x] + 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + 2 b c \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] + 2 a d \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) + b B^2 \left(\frac{1}{2} x^2 \operatorname{Log} \left[\frac{a^2 e + 2 a b e x + b^2 e x^2}{(c + d x)^2} \right]^2 - \frac{1}{b^2 d^2} 2 \left(-2 d (-b c + a d) (a + b x) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) + a^2 d^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - 2 b (b c - a d) (c + d x) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) + b^2 c^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - \left(2 \operatorname{Log} \left[\frac{a}{b} + x \right] - 2 \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right) \left(a^2 d^2 \operatorname{Log} [a + b x] - b (d (-b c + a d) x + b c^2 \operatorname{Log} [c + d x]) \right) - 2 b^2 c^2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) - 2 a^2 d^2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) \right)$$

Problem 132: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right]\right)^2}{ag + bgx} dx$$

Optimal (type 4, 132 leaves, 4 steps):

$$-\frac{\left(A + B \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right]\right)^2 \operatorname{Log}\left[1 - \frac{b(c+dx)}{d(a+bx)}\right]}{bg} + \frac{4B \left(A + B \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right]\right) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right]}{bg} + \frac{8B^2 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right]}{bg}$$

Result (type 4, 622 leaves):

$$\frac{A^2 \operatorname{Log}[a + b x]}{b g} + \frac{1}{g} 2 A B \left(\frac{\operatorname{Log}\left[\frac{a}{b} + x\right]^2}{b} + \frac{1}{b} \operatorname{Log}[a + b x] \left(-2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a^2 e}{(c+d x)^2} + \frac{2 a b e x}{(c+d x)^2} + \frac{b^2 e x^2}{(c+d x)^2}\right] \right) - \frac{2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[1 - \frac{b\left(\frac{c+x}{d}\right)}{-a + \frac{b c}{d}}\right] + \operatorname{PolyLog}\left[2, \frac{b\left(\frac{c+x}{d}\right)}{-a + \frac{b c}{d}}\right] \right)}{b} \right) + \frac{1}{g} B^2 \left(\frac{4 \operatorname{Log}\left[\frac{a}{b} + x\right]^3}{3 b} + \frac{1}{b} \operatorname{Log}[a + b x] \left(-2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a^2 e}{(c+d x)^2} + \frac{2 a b e x}{(c+d x)^2} + \frac{b^2 e x^2}{(c+d x)^2}\right] \right)^2 + 2 \left(-2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a^2 e}{(c+d x)^2} + \frac{2 a b e x}{(c+d x)^2} + \frac{b^2 e x^2}{(c+d x)^2}\right] \right) \left(\frac{\operatorname{Log}\left[\frac{a}{b} + x\right]^2}{b} - \frac{2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[1 - \frac{b\left(\frac{c+x}{d}\right)}{-a + \frac{b c}{d}}\right] + \operatorname{PolyLog}\left[2, \frac{b\left(\frac{c+x}{d}\right)}{-a + \frac{b c}{d}}\right] \right)}{b} \right) + \frac{1}{b} 8 \left(\frac{1}{2} \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[1 - \frac{b\left(\frac{c+x}{d}\right)}{-a + \frac{b c}{d}}\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b\left(\frac{c+x}{d}\right)}{-a + \frac{b c}{d}}\right] - \operatorname{PolyLog}\left[3, \frac{b\left(\frac{c+x}{d}\right)}{-a + \frac{b c}{d}}\right] \right) - \frac{1}{b} 8 \left(\frac{1}{2} \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{b d\left(\frac{c+x}{d}\right)}{b c - a d}\right] \right) - \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, -\frac{d(a+b x)}{b c - a d}\right] + \operatorname{PolyLog}\left[3, -\frac{d(a+b x)}{b c - a d}\right] \right) \right)$$

Problem 140: Unable to integrate problem.

$$\int \frac{1}{(a g + b g x)^2 \left(A + B \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \right)} dx$$

Optimal (type 4, 91 leaves, 3 steps):

$$\frac{e^{\frac{A}{2B}} \sqrt{\frac{e(a+b x)^2}{(c+d x)^2}} (c+d x) \operatorname{ExpIntegralEi}\left[-\frac{A+B \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]}{2 B}\right]}{2 B (b c - a d) g^2 (a+b x)}$$

Result (type 8, 36 leaves):

$$\int \frac{1}{(a g + b g x)^2 \left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)} dx$$

Problem 141: Unable to integrate problem.

$$\int \frac{1}{(a g + b g x)^3 \left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)} dx$$

Optimal (type 4, 149 leaves, 7 steps):

$$\frac{b e^{A/B} \operatorname{ExpIntegralEi} \left[-\frac{A+B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right]}{B} \right]}{2 B (b c - a d)^2 g^3} - \frac{d e^{\frac{A}{2B}} \sqrt{\frac{e (a+b x)^2}{(c+d x)^2}} (c+d x) \operatorname{ExpIntegralEi} \left[-\frac{A+B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right]}{2 B} \right]}{2 B (b c - a d)^2 g^3 (a+b x)}$$

Result (type 8, 36 leaves):

$$\int \frac{1}{(a g + b g x)^3 \left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)} dx$$

Problem 145: Unable to integrate problem.

$$\int \frac{1}{(a g + b g x)^2 \left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)^2} dx$$

Optimal (type 4, 147 leaves, 4 steps):

$$\frac{e^{\frac{A}{2B}} \sqrt{\frac{e (a+b x)^2}{(c+d x)^2}} (c+d x) \operatorname{ExpIntegralEi} \left[-\frac{A+B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right]}{2 B} \right]}{4 B^2 (b c - a d) g^2 (a+b x)} - \frac{c+d x}{2 B (b c - a d) g^2 (a+b x) \left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)}$$

Result (type 8, 36 leaves):

$$\int \frac{1}{(a g + b g x)^2 \left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)^2} dx$$

Problem 146: Unable to integrate problem.

$$\int \frac{1}{(a g + b g x)^3 \left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)^2} dx$$

Optimal (type 4, 263 leaves, 9 steps):

$$\begin{aligned}
& - \frac{b e^{A/B} \text{ExpIntegralEi} \left[-\frac{A+B \text{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right]}{B} \right]}{2 B^2 (bc-ad)^2 g^3} + \\
& \frac{d e^{\frac{A}{2B}} \sqrt{\frac{e^{(a+bx)^2}}{(c+dx)^2}} (c+dx) \text{ExpIntegralEi} \left[-\frac{A+B \text{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right]}{2 B} \right]}{4 B^2 (bc-ad)^2 g^3 (a+bx)} + \\
& \frac{d (c+dx)}{2 B (bc-ad)^2 g^3 (a+bx) \left(A+B \text{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] \right)} - \frac{b (c+dx)^2}{2 B (bc-ad)^2 g^3 (a+bx)^2 \left(A+B \text{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] \right)}
\end{aligned}$$

Result (type 8, 36 leaves):

$$\int \frac{1}{(ag+bgx)^3 \left(A+B \text{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] \right)^2} dx$$

Problem 156: Result more than twice size of optimal antiderivative.

$$\int (a+bx)^3 \left(A+B \text{Log} \left[e^{(a+bx)^n} (c+dx)^{-n} \right] \right)^2 dx$$

Optimal (type 4, 322 leaves, 8 steps):

$$\begin{aligned}
& - \frac{B (bc-ad) n (a+bx)^3 \left(A+B \text{Log} \left[e^{(a+bx)^n} (c+dx)^{-n} \right] \right)}{6 b d} + \\
& \frac{(a+bx)^4 \left(A+B \text{Log} \left[e^{(a+bx)^n} (c+dx)^{-n} \right] \right)^2}{4 b} + \\
& \frac{B (bc-ad)^2 n (a+bx)^2 \left(3A+Bn+3B \text{Log} \left[e^{(a+bx)^n} (c+dx)^{-n} \right] \right)}{12 b d^2} - \\
& \frac{B (bc-ad)^3 n (a+bx) \left(6A+5Bn+6B \text{Log} \left[e^{(a+bx)^n} (c+dx)^{-n} \right] \right)}{12 b d^3} - \frac{1}{12 b d^4} \\
& B (bc-ad)^4 n \text{Log} \left[\frac{bc-ad}{b(c+dx)} \right] \left(6A+11Bn+6B \text{Log} \left[e^{(a+bx)^n} (c+dx)^{-n} \right] \right) - \\
& \frac{B^2 (bc-ad)^4 n^2 \text{PolyLog} \left[2, \frac{d(a+bx)}{b(c+dx)} \right]}{2 b d^4}
\end{aligned}$$

Result (type 4, 1709 leaves):

1
12 b d⁴

$$\begin{aligned}
 & \left(-24 a^4 A B d^4 n + 6 a b^3 B^2 c^3 d n^2 - 24 a^2 b^2 B^2 c^2 d^2 n^2 + 36 a^3 b B^2 c d^3 n^2 - 24 a^4 B^2 d^4 n^2 + 12 a^3 A^2 b d^4 x - \right. \\
 & 6 A b^4 B c^3 d n x + 24 a A b^3 B c^2 d^2 n x - 36 a^2 A b^2 B c d^3 n x + 18 a^3 A b B d^4 n x - 5 b^4 B^2 c^3 d n^2 x + \\
 & 17 a b^3 B^2 c^2 d^2 n^2 x - 19 a^2 b^2 B^2 c d^3 n^2 x + 7 a^3 b B^2 d^4 n^2 x + 18 a^2 A^2 b^2 d^4 x^2 + 3 A b^4 B c^2 d^2 n x^2 - \\
 & 12 a A b^3 B c d^3 n x^2 + 9 a^2 A b^2 B d^4 n x^2 + b^4 B^2 c^2 d^2 n^2 x^2 - 2 a b^3 B^2 c d^3 n^2 x^2 + a^2 b^2 B^2 d^4 n^2 x^2 + \\
 & 12 a A^2 b^3 d^4 x^3 - 2 A b^4 B c d^3 n x^3 + 2 a A b^3 B d^4 n x^3 + 3 A^2 b^4 d^4 x^4 - 3 a^4 B^2 d^4 n^2 \text{Log}[a + b x]^2 + \\
 & 6 A b^4 B c^4 n \text{Log}[c + d x] - 24 a A b^3 B c^3 d n \text{Log}[c + d x] + 36 a^2 A b^2 B c^2 d^2 n \text{Log}[c + d x] - \\
 & 24 a^3 A b B c d^3 n \text{Log}[c + d x] + 11 b^4 B^2 c^4 n^2 \text{Log}[c + d x] - 38 a b^3 B^2 c^3 d n^2 \text{Log}[c + d x] + \\
 & 45 a^2 b^2 B^2 c^2 d^2 n^2 \text{Log}[c + d x] - 18 a^3 b B^2 c d^3 n^2 \text{Log}[c + d x] - 24 a^4 B^2 d^4 n^2 \text{Log}[c + d x] + \\
 & 3 b^4 B^2 c^4 n^2 \text{Log}[c + d x]^2 - 12 a b^3 B^2 c^3 d n^2 \text{Log}[c + d x]^2 + 18 a^2 b^2 B^2 c^2 d^2 n^2 \text{Log}[c + d x]^2 - \\
 & 12 a^3 b B^2 c d^3 n^2 \text{Log}[c + d x]^2 - 24 a^4 B^2 d^4 n \text{Log}[e (a + b x)^n (c + d x)^{-n}] + \\
 & 24 a^3 A b B d^4 x \text{Log}[e (a + b x)^n (c + d x)^{-n}] - 6 b^4 B^2 c^3 d n x \text{Log}[e (a + b x)^n (c + d x)^{-n}] + \\
 & 24 a b^3 B^2 c^2 d^2 n x \text{Log}[e (a + b x)^n (c + d x)^{-n}] - 36 a^2 b^2 B^2 c d^3 n x \text{Log}[e (a + b x)^n (c + d x)^{-n}] + \\
 & 18 a^3 b B^2 d^4 n x \text{Log}[e (a + b x)^n (c + d x)^{-n}] + 36 a^2 A b^2 B d^4 x^2 \text{Log}[e (a + b x)^n (c + d x)^{-n}] + \\
 & 3 b^4 B^2 c^2 d^2 n x^2 \text{Log}[e (a + b x)^n (c + d x)^{-n}] - 12 a b^3 B^2 c d^3 n x^2 \text{Log}[e (a + b x)^n (c + d x)^{-n}] + \\
 & 9 a^2 b^2 B^2 d^4 n x^2 \text{Log}[e (a + b x)^n (c + d x)^{-n}] + 24 a A b^3 B d^4 x^3 \text{Log}[e (a + b x)^n (c + d x)^{-n}] - \\
 & 2 b^4 B^2 c d^3 n x^3 \text{Log}[e (a + b x)^n (c + d x)^{-n}] + 2 a b^3 B^2 d^4 n x^3 \text{Log}[e (a + b x)^n (c + d x)^{-n}] + \\
 & 6 A b^4 B d^4 x^4 \text{Log}[e (a + b x)^n (c + d x)^{-n}] + 6 b^4 B^2 c^4 n \text{Log}[c + d x] \text{Log}[e (a + b x)^n (c + d x)^{-n}] - \\
 & 24 a b^3 B^2 c^3 d n \text{Log}[c + d x] \text{Log}[e (a + b x)^n (c + d x)^{-n}] + \\
 & 36 a^2 b^2 B^2 c^2 d^2 n \text{Log}[c + d x] \text{Log}[e (a + b x)^n (c + d x)^{-n}] - \\
 & 24 a^3 b B^2 c d^3 n \text{Log}[c + d x] \text{Log}[e (a + b x)^n (c + d x)^{-n}] + \\
 & 12 a^3 b B^2 d^4 x \text{Log}[e (a + b x)^n (c + d x)^{-n}]^2 + 18 a^2 b^2 B^2 d^4 x^2 \text{Log}[e (a + b x)^n (c + d x)^{-n}]^2 + \\
 & 12 a b^3 B^2 d^4 x^3 \text{Log}[e (a + b x)^n (c + d x)^{-n}]^2 + 3 b^4 B^2 d^4 x^4 \text{Log}[e (a + b x)^n (c + d x)^{-n}]^2 + \\
 & B n \text{Log}[a + b x] \left(-6 b B c (b^3 c^3 - 4 a b^2 c^2 d + 6 a^2 b c d^2 - 4 a^3 d^3) n \text{Log}[c + d x] + 6 B (b c - a d)^4 n \right. \\
 & \left. \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + a d (-6 b^3 B c^3 n + 21 a b^2 B c^2 d n - 26 a^2 b B c d^2 n + a^3 d^3 (6 A + 35 B n) + \right. \\
 & \left. 6 a^3 B d^3 \text{Log}[e (a + b x)^n (c + d x)^{-n}]) \right) + 6 B^2 (b c - a d)^4 n^2 \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \Big)
 \end{aligned}$$

Problem 157: Result more than twice size of optimal antiderivative.

$$\int (a + b x)^2 (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^2 dx$$

Optimal (type 4, 263 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{B (b c - a d) n (a + b x)^2 (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])}{3 b d} + \\
 & \frac{(a + b x)^3 (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{3 b} + \\
 & \frac{B (b c - a d)^2 n (a + b x) (2 A + B n + 2 B \text{Log}[e (a + b x)^n (c + d x)^{-n}])}{3 b d^2} + \frac{1}{3 b d^3} \\
 & B (b c - a d)^3 n \text{Log}\left[\frac{b c - a d}{b (c + d x)}\right] (2 A + 3 B n + 2 B \text{Log}[e (a + b x)^n (c + d x)^{-n}]) + \\
 & \frac{2 B^2 (b c - a d)^3 n^2 \text{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]}{3 b d^3}
 \end{aligned}$$

Result (type 4, 1149 leaves):

$$\begin{aligned}
 & \frac{1}{3 b d^3} \left(-6 a^3 A B d^3 n - 2 a b^2 B^2 c^2 d n^2 + 6 a^2 b B^2 c d^2 n^2 - 6 a^3 B^2 d^3 n^2 + 3 a^2 A^2 b d^3 x + 2 A b^3 B c^2 d n x - \right. \\
 & 6 a A b^2 B c d^2 n x + 4 a^2 A b B d^3 n x + b^3 B^2 c^2 d n^2 x - 2 a b^2 B^2 c d^2 n^2 x + a^2 b B^2 d^3 n^2 x + 3 a A^2 b^2 d^3 x^2 - \\
 & A b^3 B c d^2 n x^2 + a A b^2 B d^3 n x^2 + A^2 b^3 d^3 x^3 - a^3 B^2 d^3 n^2 \text{Log}[a + b x]^2 - 2 A b^3 B c^3 n \text{Log}[c + d x] + \\
 & 6 a A b^2 B c^2 d n \text{Log}[c + d x] - 6 a^2 A b B c d^2 n \text{Log}[c + d x] - 3 b^3 B^2 c^3 n^2 \text{Log}[c + d x] + \\
 & 7 a b^2 B^2 c^2 d n^2 \text{Log}[c + d x] - 4 a^2 b B^2 c d^2 n^2 \text{Log}[c + d x] - 6 a^3 B^2 d^3 n^2 \text{Log}[c + d x] - \\
 & b^3 B^2 c^3 n^2 \text{Log}[c + d x]^2 + 3 a b^2 B^2 c^2 d n^2 \text{Log}[c + d x]^2 - 3 a^2 b B^2 c d^2 n^2 \text{Log}[c + d x]^2 - \\
 & 6 a^3 B^2 d^3 n \text{Log}[e (a + b x)^n (c + d x)^{-n}] + 6 a^2 A b B d^3 x \text{Log}[e (a + b x)^n (c + d x)^{-n}] + \\
 & 2 b^3 B^2 c^2 d n x \text{Log}[e (a + b x)^n (c + d x)^{-n}] - 6 a b^2 B^2 c d^2 n x \text{Log}[e (a + b x)^n (c + d x)^{-n}] + \\
 & 4 a^2 b B^2 d^3 n x \text{Log}[e (a + b x)^n (c + d x)^{-n}] + 6 a A b^2 B d^3 x^2 \text{Log}[e (a + b x)^n (c + d x)^{-n}] - \\
 & b^3 B^2 c d^2 n x^2 \text{Log}[e (a + b x)^n (c + d x)^{-n}] + a b^2 B^2 d^3 n x^2 \text{Log}[e (a + b x)^n (c + d x)^{-n}] + \\
 & 2 A b^3 B d^3 x^3 \text{Log}[e (a + b x)^n (c + d x)^{-n}] - 2 b^3 B^2 c^3 n \text{Log}[c + d x] \text{Log}[e (a + b x)^n (c + d x)^{-n}] + \\
 & 6 a b^2 B^2 c^2 d n \text{Log}[c + d x] \text{Log}[e (a + b x)^n (c + d x)^{-n}] - \\
 & 6 a^2 b B^2 c d^2 n \text{Log}[c + d x] \text{Log}[e (a + b x)^n (c + d x)^{-n}] + \\
 & 3 a^2 b B^2 d^3 x \text{Log}[e (a + b x)^n (c + d x)^{-n}]^2 + 3 a b^2 B^2 d^3 x^2 \text{Log}[e (a + b x)^n (c + d x)^{-n}]^2 + \\
 & b^3 B^2 d^3 x^3 \text{Log}[e (a + b x)^n (c + d x)^{-n}]^2 + B n \text{Log}[a + b x] \\
 & \left. \left(2 b B c (b^2 c^2 - 3 a b c d + 3 a^2 d^2) n \text{Log}[c + d x] - 2 B (b c - a d)^3 n \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \right. \right. \\
 & \left. \left. a d (2 b^2 B c^2 n - 5 a b B c d n + a^2 d^2 (2 A + 9 B n) + 2 a^2 B d^2 \text{Log}[e (a + b x)^n (c + d x)^{-n}]) \right) - \right. \\
 & \left. 2 B^2 (b c - a d)^3 n^2 \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right)
 \end{aligned}$$

Problem 158: Result more than twice size of optimal antiderivative.

$$\int (a + b x) (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^2 dx$$

Optimal (type 4, 195 leaves, 6 steps):

$$\begin{aligned}
 & - \frac{B (b c - a d) n (a + b x) (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])}{b d} + \\
 & \frac{(a + b x)^2 (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{2 b} - \\
 & \frac{B (b c - a d)^2 n \text{Log}\left[\frac{b c - a d}{b (c + d x)}\right] (A + B n + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])}{b d^2} - \\
 & \frac{B^2 (b c - a d)^2 n^2 \text{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]}{b d^2}
 \end{aligned}$$

Result (type 4, 656 leaves):

$$\begin{aligned}
 & - \frac{2 a^2 A B n}{b} - \frac{2 a^2 B^2 n^2}{b} + \frac{a B^2 c n^2}{d} + a A^2 x + a A B n x - \frac{A b B c n x}{d} + \frac{1}{2} A^2 b x^2 - \\
 & \frac{a^2 B^2 n^2 \text{Log}[a + b x]^2}{2 b} + \frac{A b B c^2 n \text{Log}[c + d x]}{d^2} - \frac{2 a A B c n \text{Log}[c + d x]}{d} - \frac{2 a^2 B^2 n^2 \text{Log}[c + d x]}{b} + \\
 & \frac{b B^2 c^2 n^2 \text{Log}[c + d x]}{d^2} - \frac{a B^2 c n^2 \text{Log}[c + d x]}{d} + \frac{b B^2 c^2 n^2 \text{Log}[c + d x]^2}{2 d^2} - \frac{a B^2 c n^2 \text{Log}[c + d x]^2}{d} - \\
 & \frac{2 a^2 B^2 n \text{Log}[e (a + b x)^n (c + d x)^{-n}]}{b} + 2 a A B x \text{Log}[e (a + b x)^n (c + d x)^{-n}] + \\
 & a B^2 n x \text{Log}[e (a + b x)^n (c + d x)^{-n}] - \frac{b B^2 c n x \text{Log}[e (a + b x)^n (c + d x)^{-n}]}{d} + \\
 & A b B x^2 \text{Log}[e (a + b x)^n (c + d x)^{-n}] + \frac{b B^2 c^2 n \text{Log}[c + d x] \text{Log}[e (a + b x)^n (c + d x)^{-n}]}{d^2} - \\
 & \frac{2 a B^2 c n \text{Log}[c + d x] \text{Log}[e (a + b x)^n (c + d x)^{-n}]}{d} + \\
 & a B^2 x \text{Log}[e (a + b x)^n (c + d x)^{-n}]^2 + \frac{1}{2} b B^2 x^2 \text{Log}[e (a + b x)^n (c + d x)^{-n}]^2 + \frac{1}{b d^2} \\
 & B n \text{Log}[a + b x] \left(b B c (-b c + 2 a d) n \text{Log}[c + d x] + B (b c - a d)^2 n \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \right. \\
 & \quad \left. a d (-b B c n + a d (A + 3 B n) + a B d \text{Log}[e (a + b x)^n (c + d x)^{-n}]) \right) + \\
 & \frac{B^2 (b c - a d)^2 n^2 \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right]}{b d^2}
 \end{aligned}$$

Problem 159: Result more than twice size of optimal antiderivative.

$$\int \frac{(A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{a + b x} dx$$

Optimal (type 4, 131 leaves, 5 steps):

$$-\frac{(A+B \operatorname{Log}[e (a+b x)^n (c+d x)^{-n}])^2 \operatorname{Log}\left[1-\frac{b(c+d x)}{d(a+b x)}\right]}{b} + \frac{2 B n (A+B \operatorname{Log}[e (a+b x)^n (c+d x)^{-n}]) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]}{b} + \frac{2 B^2 n^2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{d(a+b x)}\right]}{b}$$

Result (type 4, 443 leaves):

$$\begin{aligned} & \frac{1}{3 b} \left(B^2 n^2 \operatorname{Log}[a+b x]^3 + \right. \\ & 3 B n \operatorname{Log}[a+b x]^2 \left(A+B \left(-n \operatorname{Log}[a+b x] + n \operatorname{Log}[c+d x] + \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n} \right] \right) \right) + \\ & 3 \operatorname{Log}[a+b x] \left(A+B \left(-n \operatorname{Log}[a+b x] + n \operatorname{Log}[c+d x] + \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n} \right] \right) \right)^2 - \\ & 6 A B n \left(\operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d} \right] \operatorname{Log}[c+d x] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d} \right] \right) - \\ & 6 B^2 n \left(-n \operatorname{Log}[a+b x] + n \operatorname{Log}[c+d x] + \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n} \right] \right) \\ & \left(\operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d} \right] \operatorname{Log}[c+d x] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d} \right] \right) - \\ & 6 B^2 n^2 \left(\frac{1}{2} \operatorname{Log}[a+b x]^2 \left(\operatorname{Log}[c+d x] - \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d} \right] \right) - \operatorname{Log}[a+b x] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d} \right] + \right. \\ & \left. \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d} \right] \right) + 3 B^2 n^2 \left(\operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d} \right] \operatorname{Log}[c+d x]^2 + \right. \\ & \left. 2 \operatorname{Log}[c+d x] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d} \right] - 2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d} \right] \right) \Big) \end{aligned}$$

Problem 164: Result more than twice size of optimal antiderivative.

$$\int (a+b x)^3 (A+B \operatorname{Log}[e (a+b x)^n (c+d x)^{-n}])^3 dx$$

Optimal (type 4, 809 leaves, 27 steps):

$$\begin{aligned}
 & - \frac{B^3 (b c - a d)^3 n^3 x}{4 d^3} - \frac{B^3 (b c - a d)^4 n^3 \text{Log}\left[\frac{a+b x}{c+d x}\right]}{4 b d^4} + \frac{3 B^3 (b c - a d)^4 n^3 \text{Log}[c+d x]}{2 b d^4} - \\
 & \frac{7 B^2 (b c - a d)^3 n^2 (a+b x) (A+B \text{Log}[e (a+b x)^n (c+d x)^{-n}])}{4 b d^3} + \\
 & \frac{b B^2 (b c - a d)^2 n^2 (c+d x)^2 (A+B \text{Log}[e (a+b x)^n (c+d x)^{-n}])}{4 d^4} - \\
 & \frac{9 B^2 (b c - a d)^4 n^2 \text{Log}\left[\frac{b c - a d}{b (c+d x)}\right] (A+B \text{Log}[e (a+b x)^n (c+d x)^{-n}])}{2 b d^4} - \\
 & \frac{9 B (b c - a d)^3 n (a+b x) (A+B \text{Log}[e (a+b x)^n (c+d x)^{-n}])^2}{4 b d^3} + \\
 & \frac{9 b B (b c - a d)^2 n (c+d x)^2 (A+B \text{Log}[e (a+b x)^n (c+d x)^{-n}])^2}{8 d^4} - \\
 & \frac{b^2 B (b c - a d) n (c+d x)^3 (A+B \text{Log}[e (a+b x)^n (c+d x)^{-n}])^2}{4 d^4} - \\
 & \frac{3 B (b c - a d)^4 n \text{Log}\left[\frac{b c - a d}{b (c+d x)}\right] (A+B \text{Log}[e (a+b x)^n (c+d x)^{-n}])^2}{4 b d^4} + \\
 & \frac{(a+b x)^4 (A+B \text{Log}[e (a+b x)^n (c+d x)^{-n}])^3}{4 b} + \frac{1}{4 b d^4} \\
 & 7 B^2 (b c - a d)^4 n^2 (A+B \text{Log}[e (a+b x)^n (c+d x)^{-n}]) \text{Log}\left[1 - \frac{b (c+d x)}{d (a+b x)}\right] - \\
 & \frac{9 B^3 (b c - a d)^4 n^3 \text{PolyLog}\left[2, \frac{d (a+b x)}{b (c+d x)}\right]}{2 b d^4} - \frac{1}{2 b d^4} \\
 & 3 B^2 (b c - a d)^4 n^2 (A+B \text{Log}[e (a+b x)^n (c+d x)^{-n}]) \text{PolyLog}\left[2, \frac{d (a+b x)}{b (c+d x)}\right] - \\
 & \frac{7 B^3 (b c - a d)^4 n^3 \text{PolyLog}\left[2, \frac{b (c+d x)}{d (a+b x)}\right]}{4 b d^4} + \frac{3 B^3 (b c - a d)^4 n^3 \text{PolyLog}\left[3, \frac{d (a+b x)}{b (c+d x)}\right]}{2 b d^4}
 \end{aligned}$$

Result (type 4, 6899 leaves):

$$\begin{aligned}
 & \frac{1}{8 b d^4} \left(12 a A b^3 B^2 c^3 d n^2 - 48 a^2 A b^2 B^2 c^2 d^2 n^2 + 60 a^3 A b B^2 c d^3 n^2 - 48 a^4 A B^2 d^4 n^2 - 12 b^4 B^3 c^4 n^3 + \right. \\
 & 58 a b^3 B^3 c^3 d n^3 - 100 a^2 b^2 B^3 c^2 d^2 n^3 + 54 a^3 b B^3 c d^3 n^3 + 12 a^4 B^3 d^4 n^3 + 8 a^3 A^3 b d^4 x - \\
 & 6 A^2 b^4 B c^3 d n x + 24 a A^2 b^3 B c^2 d^2 n x - 36 a^2 A^2 b^2 B c d^3 n x + 18 a^3 A^2 b B d^4 n x - \\
 & 10 A b^4 B^2 c^3 d n^2 x + 34 a A b^3 B^2 c^2 d^2 n^2 x - 38 a^2 A b^2 B^2 c d^3 n^2 x + 14 a^3 A b B^2 d^4 n^2 x - \\
 & 2 b^4 B^3 c^3 d n^3 x + 6 a b^3 B^3 c^2 d^2 n^3 x - 6 a^2 b^2 B^3 c d^3 n^3 x + 2 a^3 b B^3 d^4 n^3 x + 12 a^2 A^3 b^2 d^4 x^2 + \\
 & 3 A^2 b^4 B c^2 d^2 n x^2 - 12 a A^2 b^3 B c d^3 n x^2 + 9 a^2 A^2 b^2 B d^4 n x^2 + 2 A b^4 B^2 c^2 d^2 n^2 x^2 - \\
 & 4 a A b^3 B^2 c d^3 n^2 x^2 + 2 a^2 A b^2 B^2 d^4 n^2 x^2 + 8 a A^3 b^3 d^4 x^3 - 2 A^2 b^4 B c d^3 n x^3 + \\
 & 2 a A^2 b^3 B d^4 n x^3 + 2 A^3 b^4 d^4 x^4 + 6 a^4 A^2 B d^4 n \text{Log}[a+b x] - 12 a A b^3 B^2 c^3 d n^2 \text{Log}[a+b x] + \\
 & 42 a^2 A b^2 B^2 c^2 d^2 n^2 \text{Log}[a+b x] - 52 a^3 A b B^2 c d^3 n^2 \text{Log}[a+b x] + 22 a^4 A B^2 d^4 n^2 \text{Log}[a+b x] - \\
 & 22 a b^3 B^3 c^3 d n^3 \text{Log}[a+b x] + 80 a^2 b^2 B^3 c^2 d^2 n^3 \text{Log}[a+b x] - 94 a^3 b B^3 c d^3 n^3 \text{Log}[a+b x] + \\
 & 60 a^4 B^3 d^4 n^3 \text{Log}[a+b x] - 6 a^4 A B^2 d^4 n^2 \text{Log}[a+b x]^2 + 6 a b^3 B^3 c^3 d n^3 \text{Log}[a+b x]^2 - \\
 & 21 a^2 b^2 B^3 c^2 d^2 n^3 \text{Log}[a+b x]^2 + 26 a^3 b B^3 c d^3 n^3 \text{Log}[a+b x]^2 - 11 a^4 B^3 d^4 n^3 \text{Log}[a+b x]^2 + \\
 & 2 a^4 B^3 d^4 n^3 \text{Log}[a+b x]^3 + 6 A^2 b^4 B c^4 n \text{Log}[c+d x] - 24 a A^2 b^3 B c^3 d n \text{Log}[c+d x] +
 \end{aligned}$$

$$\begin{aligned}
& 36 a^2 A^2 b^2 B c^2 d^2 n \operatorname{Log}[c+d x] - 24 a^3 A^2 b B c d^3 n \operatorname{Log}[c+d x] + 22 A b^4 B^2 c^4 n^2 \operatorname{Log}[c+d x] - \\
& 76 a A b^3 B^2 c^3 d n^2 \operatorname{Log}[c+d x] + 90 a^2 A b^2 B^2 c^2 d^2 n^2 \operatorname{Log}[c+d x] - 36 a^3 A b B^2 c d^3 n^2 \operatorname{Log}[c+d x] + \\
& 12 b^4 B^3 c^4 n^3 \operatorname{Log}[c+d x] - 26 a b^3 B^3 c^3 d n^3 \operatorname{Log}[c+d x] - 8 a^2 b^2 B^3 c^2 d^2 n^3 \operatorname{Log}[c+d x] + \\
& 46 a^3 b B^3 c d^3 n^3 \operatorname{Log}[c+d x] - 48 a^4 B^3 d^4 n^3 \operatorname{Log}[c+d x] - 12 A b^4 B^2 c^4 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] + \\
& 48 a A b^3 B^2 c^3 d n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] - 72 a^2 A b^2 B^2 c^2 d^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] + \\
& 48 a^3 A b B^2 c d^3 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] + 12 a^4 A B^2 d^4 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] - \\
& 22 b^4 B^3 c^4 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] + 76 a b^3 B^3 c^3 d n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] - \\
& 90 a^2 b^2 B^3 c^2 d^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] + 36 a^3 b B^3 c d^3 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] + \\
& 6 b^4 B^3 c^4 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x] - 24 a b^3 B^3 c^3 d n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x] + \\
& 36 a^2 b^2 B^3 c^2 d^2 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x] - 24 a^3 b B^3 c d^3 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x] - \\
& 12 a^4 B^3 d^4 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x] - 12 a^4 A B^2 d^4 n^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x] + \\
& 12 a^4 B^3 d^4 n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x] + 6 A b^4 B^2 c^4 n^2 \operatorname{Log}[c+d x]^2 - \\
& 24 a A b^3 B^2 c^3 d n^2 \operatorname{Log}[c+d x]^2 + 36 a^2 A b^2 B^2 c^2 d^2 n^2 \operatorname{Log}[c+d x]^2 - \\
& 24 a^3 A b B^2 c d^3 n^2 \operatorname{Log}[c+d x]^2 + 11 b^4 B^3 c^4 n^3 \operatorname{Log}[c+d x]^2 - 38 a b^3 B^3 c^3 d n^3 \operatorname{Log}[c+d x]^2 + \\
& 45 a^2 b^2 B^3 c^2 d^2 n^3 \operatorname{Log}[c+d x]^2 - 18 a^3 b B^3 c d^3 n^3 \operatorname{Log}[c+d x]^2 - \\
& 12 b^4 B^3 c^4 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2 + 48 a b^3 B^3 c^3 d n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2 - \\
& 72 a^2 b^2 B^3 c^2 d^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2 + 48 a^3 b B^3 c d^3 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2 + \\
& 6 a^4 B^3 d^4 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2 + 6 b^4 B^3 c^4 n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2 - \\
& 24 a b^3 B^3 c^3 d n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2 + 36 a^2 b^2 B^3 c^2 d^2 n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2 - \\
& 24 a^3 b B^3 c d^3 n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2 - 6 a^4 B^3 d^4 n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2 + \\
& 2 b^4 B^3 c^4 n^3 \operatorname{Log}[c+d x]^3 - 8 a b^3 B^3 c^3 d n^3 \operatorname{Log}[c+d x]^3 + 12 a^2 b^2 B^3 c^2 d^2 n^3 \operatorname{Log}[c+d x]^3 - \\
& 8 a^3 b B^3 c d^3 n^3 \operatorname{Log}[c+d x]^3 + 12 A b^4 B^2 c^4 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
& 48 a A b^3 B^2 c^3 d n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 72 a^2 A b^2 B^2 c^2 d^2 n^2 \\
& \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 48 a^3 A b B^2 c d^3 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
& 22 b^4 B^3 c^4 n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 88 a b^3 B^3 c^3 d n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
& 132 a^2 b^2 B^3 c^2 d^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 88 a^3 b B^3 c d^3 n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
& 22 a^4 B^3 d^4 n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 6 b^4 B^3 c^4 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
& 24 a b^3 B^3 c^3 d n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 36 a^2 b^2 B^3 c^2 d^2 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
& 24 a^3 b B^3 c d^3 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 6 a^4 B^3 d^4 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
& 12 b^4 B^3 c^4 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] -
\end{aligned}$$

$$\begin{aligned}
 & 48 a b^3 B^3 c^3 d n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 & 72 a^2 b^2 B^3 c^2 d^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
 & 48 a^3 b B^3 c d^3 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 & 12 a b^3 B^3 c^3 d n^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - 48 a^2 b^2 B^3 c^2 d^2 n^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 60 a^3 b B^3 c d^3 n^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - 48 a^4 B^3 d^4 n^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 24 a^3 A^2 b B d^4 x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - 12 A b^4 B^2 c^3 d n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 48 a A b^3 B^2 c^2 d^2 n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - 72 a^2 A b^2 B^2 c d^3 n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 36 a^3 A b B^2 d^4 n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - 10 b^4 B^3 c^3 d n^2 x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 34 a b^3 B^3 c^2 d^2 n^2 x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - 38 a^2 b^2 B^3 c d^3 n^2 x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 14 a^3 b B^3 d^4 n^2 x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + 36 a^2 A^2 b^2 B d^4 x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 6 A b^4 B^2 c^2 d^2 n x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - 24 a A b^3 B^2 c d^3 n x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 18 a^2 A b^2 B^2 d^4 n x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + 2 b^4 B^3 c^2 d^2 n^2 x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
 & 4 a b^3 B^3 c d^3 n^2 x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + 2 a^2 b^2 B^3 d^4 n^2 x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 24 a A^2 b^3 B d^4 x^3 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - 4 A b^4 B^2 c d^3 n x^3 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 4 a A b^3 B^2 d^4 n x^3 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + 6 A^2 b^4 B d^4 x^4 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 12 a^4 A B^2 d^4 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
 & 12 a b^3 B^3 c^3 d n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 42 a^2 b^2 B^3 c^2 d^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
 & 52 a^3 b B^3 c d^3 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 22 a^4 B^3 d^4 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
 & 6 a^4 B^3 d^4 n^2 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 12 A b^4 B^2 c^4 n \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
 & 48 a A b^3 B^2 c^3 d n \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 72 a^2 A b^2 B^2 c^2 d^2 n \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
 & 48 a^3 A b B^2 c d^3 n \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 22 b^4 B^3 c^4 n^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
 & 76 a b^3 B^3 c^3 d n^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 90 a^2 b^2 B^3 c^2 d^2 n^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
 & 36 a^3 b B^3 c d^3 n^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
 & 12 b^4 B^3 c^4 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 48 a b^3 B^3 c^3 d n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
 & 72 a^2 b^2 B^3 c^2 d^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 48 a^3 b B^3 c d^3 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 12 a^4 B^3 d^4 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
 & 12 a^4 B^3 d^4 n^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 6 b^4 B^3 c^4 n^2 \operatorname{Log}[c+d x]^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
 & 24 a b^3 B^3 c^3 d n^2 \operatorname{Log}[c+d x]^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 36 a^2 b^2 B^3 c^2 d^2 n^2 \operatorname{Log}[c+d x]^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
 & 24 a^3 b B^3 c d^3 n^2 \operatorname{Log}[c+d x]^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 12 b^4 B^3 c^4 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] -
 \end{aligned}$$

$$\begin{aligned}
 & 48 a b^3 B^3 c^3 d n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]+ \\
 & 72 a^2 b^2 B^3 c^2 d^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]- \\
 & 48 a^3 b B^3 c d^3 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]+ \\
 & 24 a^3 A b B^2 d^4 x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2-6 b^4 B^3 c^3 d n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2+ \\
 & 24 a b^3 B^3 c^2 d^2 n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2-36 a^2 b^2 B^3 c d^3 n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2+ \\
 & 18 a^3 b B^3 d^4 n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2+36 a^2 A b^2 B^2 d^4 x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2+ \\
 & 3 b^4 B^3 c^2 d^2 n x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2-12 a b^3 B^3 c d^3 n x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2+ \\
 & 9 a^2 b^2 B^3 d^4 n x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2+24 a A b^3 B^2 d^4 x^3 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2- \\
 & 2 b^4 B^3 c d^3 n x^3 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2+2 a b^3 B^3 d^4 n x^3 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2+ \\
 & 6 A b^4 B^2 d^4 x^4 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2+6 a^4 B^3 d^4 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2+ \\
 & 6 b^4 B^3 c^4 n \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2- \\
 & 24 a b^3 B^3 c^3 d n \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2+ \\
 & 36 a^2 b^2 B^3 c^2 d^2 n \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2- \\
 & 24 a^3 b B^3 c d^3 n \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2+ \\
 & 8 a^3 b B^3 d^4 x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^3+12 a^2 b^2 B^3 d^4 x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^3+ \\
 & 8 a b^3 B^3 d^4 x^3 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^3+2 b^4 B^3 d^4 x^4 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^3+ \\
 & 2 B^2 n^2\left(6 A b^4 c^4-24 a A b^3 c^3 d+36 a^2 A b^2 c^2 d^2-24 a^3 A b c d^3+11 b^4 B c^4 n-44 a b^3 B c^3 d n+\right. \\
 & \quad \left.66 a^2 b^2 B c^2 d^2 n-44 a^3 b B c d^3 n+11 a^4 B d^4 n+6 a^4 B d^4 n \operatorname{Log}[a+b x]+6 b B c\right. \\
 & \quad \left.\left(b^3 c^3-4 a b^2 c^2 d+6 a^2 b c d^2-4 a^3 d^3\right) n \operatorname{Log}[c+d x]+6 b^4 B c^4 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]-\right. \\
 & \quad \left.24 a b^3 B c^3 d \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]+36 a^2 b^2 B c^2 d^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]-\right. \\
 & \quad \left.24 a^3 b B c d^3 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]\right) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]+ \\
 & 12 B^2 n^2\left(a^4 B d^4 n \operatorname{Log}[a+b x]+b B c\left(b^3 c^3-4 a b^2 c^2 d+6 a^2 b c d^2-4 a^3 d^3\right) n \operatorname{Log}[c+d x]-\right. \\
 & \quad \left.a^4 d^4(A+B \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right])\right) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]- \\
 & 12 b^4 B^3 c^4 n^3 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]+48 a b^3 B^3 c^3 d n^3 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]- \\
 & 72 a^2 b^2 B^3 c^2 d^2 n^3 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]+48 a^3 b B^3 c d^3 n^3 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]- \\
 & 12 a^4 B^3 d^4 n^3 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]-12 b^4 B^3 c^4 n^3 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]+ \\
 & 48 a b^3 B^3 c^3 d n^3 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]-72 a^2 b^2 B^3 c^2 d^2 n^3 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]+ \\
 & 48 a^3 b B^3 c d^3 n^3 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]-12 a^4 B^3 d^4 n^3 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]
 \end{aligned}$$

Problem 165: Result more than twice size of optimal antiderivative.

$$\int (a+b x)^2 (A+B \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right])^3 dx$$

Optimal (type 4, 614 leaves, 17 steps):

$$\begin{aligned}
 & - \frac{B^3 (b c - a d)^3 n^3 \text{Log}[c + d x]}{b d^3} + \frac{B^2 (b c - a d)^2 n^2 (a + b x) (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])}{b d^2} + \\
 & \frac{4 B^2 (b c - a d)^3 n^2 \text{Log}\left[\frac{b c - a d}{b (c + d x)}\right] (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])}{b d^3} + \\
 & \frac{2 B (b c - a d)^2 n (a + b x) (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{b d^2} - \\
 & \frac{b B (b c - a d) n (c + d x)^2 (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{2 d^3} + \\
 & \frac{B (b c - a d)^3 n \text{Log}\left[\frac{b c - a d}{b (c + d x)}\right] (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{b d^3} + \\
 & \frac{(a + b x)^3 (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^3}{3 b} - \\
 & \frac{B^2 (b c - a d)^3 n^2 (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}]) \text{Log}\left[1 - \frac{b (c + d x)}{d (a + b x)}\right]}{b d^3} + \\
 & \frac{4 B^3 (b c - a d)^3 n^3 \text{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]}{b d^3} + \frac{1}{b d^3} \\
 & 2 B^2 (b c - a d)^3 n^2 (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}]) \text{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right] + \\
 & \frac{B^3 (b c - a d)^3 n^3 \text{PolyLog}\left[2, \frac{b (c + d x)}{d (a + b x)}\right]}{b d^3} - \frac{2 B^3 (b c - a d)^3 n^3 \text{PolyLog}\left[3, \frac{d (a + b x)}{b (c + d x)}\right]}{b d^3}
 \end{aligned}$$

Result (type 4, 4819 leaves):

$$\begin{aligned}
 & - \frac{6 a^3 A B^2 n^2}{b} - \frac{2 a A B B^2 c^2 n^2}{d^2} + \frac{4 a^2 A B^2 c n^2}{d} + \frac{2 a^3 B^3 n^3}{b} + \frac{2 b^2 B^3 c^3 n^3}{d^3} - \frac{7 a b B^3 c^2 n^3}{d^2} + \\
 & \frac{5 a^2 B^3 c n^3}{d} + a^2 A^3 x + 2 a^2 A^2 B n x + \frac{A^2 b^2 B c^2 n x}{d^2} - \frac{3 a A^2 b B c n x}{d} + a^2 A B^2 n^2 x + \frac{A b^2 B^2 c^2 n^2 x}{d^2} - \\
 & \frac{2 a A B B^2 c n^2 x}{d} + a A^3 b x^2 + \frac{1}{2} a A^2 b B n x^2 - \frac{A^2 b^2 B c n x^2}{2 d} + \frac{1}{3} A^3 b^2 x^3 + \frac{a^3 A^2 B n \text{Log}[a + b x]}{b} + \\
 & \frac{3 a^3 A B^2 n^2 \text{Log}[a + b x]}{b} + \frac{2 a A B B^2 c^2 n^2 \text{Log}[a + b x]}{d^2} - \frac{5 a^2 A B^2 c n^2 \text{Log}[a + b x]}{d} + \\
 & \frac{7 a^3 B^3 n^3 \text{Log}[a + b x]}{b} + \frac{3 a b B^3 c^2 n^3 \text{Log}[a + b x]}{d^2} - \frac{6 a^2 B^3 c n^3 \text{Log}[a + b x]}{d} - \\
 & \frac{a^3 A B^2 n^2 \text{Log}[a + b x]^2}{b} - \frac{3 a^3 B^3 n^3 \text{Log}[a + b x]^2}{2 b} - \frac{a b B^3 c^2 n^3 \text{Log}[a + b x]^2}{d^2} + \\
 & \frac{5 a^2 B^3 c n^3 \text{Log}[a + b x]^2}{2 d} + \frac{a^3 B^3 n^3 \text{Log}[a + b x]^3}{3 b} - \frac{A^2 b^2 B c^3 n \text{Log}[c + d x]}{d^3} + \\
 & \frac{3 a A^2 b B c^2 n \text{Log}[c + d x]}{d^2} - \frac{3 a^2 A^2 B c n \text{Log}[c + d x]}{d} - \frac{3 A b^2 B^2 c^3 n^2 \text{Log}[c + d x]}{d^3} +
 \end{aligned}$$

$$\begin{aligned}
& \frac{7 a A b B^2 c^2 n^2 \operatorname{Log}[c+d x]}{d^2} - \frac{4 a^2 A B^2 c n^2 \operatorname{Log}[c+d x]}{d} - \frac{6 a^3 B^3 n^3 \operatorname{Log}[c+d x]}{b} - \\
& \frac{b^2 B^3 c^3 n^3 \operatorname{Log}[c+d x]}{d^3} + \frac{3 a^2 B^3 c n^3 \operatorname{Log}[c+d x]}{d} + \frac{2 a^3 A B^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]}{b} + \\
& \frac{2 A b^2 B^2 c^3 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]}{d^3} - \frac{6 a A b B^2 c^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]}{d^2} + \\
& \frac{6 a^2 A B^2 c n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]}{d} + \frac{3 b^2 B^3 c^3 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]}{d^3} - \\
& \frac{7 a b B^3 c^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]}{d^2} + \frac{4 a^2 B^3 c n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]}{d} - \\
& \frac{2 a^3 B^3 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x]}{b} - \frac{b^2 B^3 c^3 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x]}{d^3} + \\
& \frac{3 a b B^3 c^2 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x]}{d^2} - \frac{3 a^2 B^3 c n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x]}{d} - \\
& \frac{2 a^3 A B^2 n^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]}{b} + \frac{2 a^2 B^3 n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]}{b} - \\
& \frac{A b^2 B^2 c^3 n^2 \operatorname{Log}[c+d x]^2}{d^3} + \frac{3 a A b B^2 c^2 n^2 \operatorname{Log}[c+d x]^2}{d^2} - \frac{3 a^2 A B^2 c n^2 \operatorname{Log}[c+d x]^2}{d} - \\
& \frac{3 b^2 B^3 c^3 n^3 \operatorname{Log}[c+d x]^2}{2 d^3} + \frac{7 a b B^3 c^2 n^3 \operatorname{Log}[c+d x]^2}{2 d^2} - \frac{2 a^2 B^3 c n^3 \operatorname{Log}[c+d x]^2}{d} + \\
& \frac{a^3 B^3 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2}{b} + \frac{2 b^2 B^3 c^3 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2}{d^3} - \\
& \frac{6 a b B^3 c^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2}{d^2} + \frac{6 a^2 B^3 c n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2}{d} - \\
& \frac{a^3 B^3 n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2}{b} - \frac{b^2 B^3 c^3 n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2}{d^3} + \\
& \frac{3 a b B^3 c^2 n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2}{d^2} - \frac{3 a^2 B^3 c n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2}{d} - \\
& \frac{b^2 B^3 c^3 n^3 \operatorname{Log}[c+d x]^3}{3 d^3} + \frac{a b B^3 c^2 n^3 \operatorname{Log}[c+d x]^3}{d^2} - \frac{a^2 B^3 c n^3 \operatorname{Log}[c+d x]^3}{d} - \\
& \frac{2 A b^2 B^2 c^3 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^3} + \frac{6 a A b B^2 c^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^2} - \\
& \frac{6 a^2 A B^2 c n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d} + \frac{3 a^3 B^3 n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{b} - \\
& \frac{3 b^2 B^3 c^3 n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^3} + \frac{9 a b B^3 c^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^2} - \\
& \frac{9 a^2 B^3 c n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d} + \frac{a^3 B^3 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{b} + \\
& \frac{b^2 B^3 c^3 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^3} - \frac{3 a b B^3 c^2 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^2} +
\end{aligned}$$

$$\begin{aligned}
 & \frac{3 a^2 B^3 c n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d} - \frac{2 b^2 B^3 c^3 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^3} + \\
 & \frac{6 a b B^3 c^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^2} - \\
 & \frac{6 a^2 B^3 c n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d} - \frac{6 a^3 B^3 n^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b} - \\
 & \frac{2 a b B^3 c^2 n^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^2} + \frac{4 a^2 B^3 c n^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d} + \\
 & \frac{3 a^2 A^2 B x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + 4 a^2 A B^2 n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] +}{d^2} \\
 & \frac{2 A b^2 B^2 c^2 n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^2} - \frac{6 a A b B^2 c n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d} + \\
 & a^2 B^3 n^2 x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \frac{b^2 B^3 c^2 n^2 x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^2} - \\
 & \frac{2 a b B^3 c n^2 x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d} + 3 a A^2 b B x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & a A b B^2 n x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \frac{A b^2 B^2 c n x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d} + \\
 & A^2 b^2 B x^3 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \frac{2 a^3 A B^2 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b} + \\
 & \frac{3 a^3 B^3 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b} + \\
 & \frac{2 a b B^3 c^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^2} - \\
 & \frac{5 a^2 B^3 c n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d} - \\
 & \frac{a^3 B^3 n^2 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b} - \\
 & \frac{2 A b^2 B^2 c^3 n \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^3} + \\
 & \frac{6 a A b B^2 c^2 n \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^2} - \\
 & \frac{6 a^2 A B^2 c n \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d} - \\
 & \frac{3 b^2 B^3 c^3 n^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^3} + \\
 & \frac{7 a b B^3 c^2 n^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^2} - \\
 & \frac{4 a^2 B^3 c n^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d} +
 \end{aligned}$$

$$\begin{aligned}
& \frac{2 a^3 B^3 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b} + \\
& \frac{2 b^2 B^3 c^3 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^3} - \\
& \frac{6 a b B^3 c^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^2} + \\
& \frac{6 a^2 B^3 c n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d} - \\
& \frac{2 a^3 B^3 n^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b} - \\
& \frac{b^2 B^3 c^3 n^2 \operatorname{Log}[c+d x]^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^3} + \\
& \frac{3 a b B^3 c^2 n^2 \operatorname{Log}[c+d x]^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^2} - \\
& \frac{3 a^2 B^3 c n^2 \operatorname{Log}[c+d x]^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d} - \\
& \frac{2 b^2 B^3 c^3 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^3} + \\
& \frac{6 a b B^3 c^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^2} - \\
& \frac{6 a^2 B^3 c n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d} + \\
& \frac{3 a^2 A B^2 x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2 + 2 a^2 B^3 n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2 +}{d^2} - \\
& \frac{b^2 B^3 c^2 n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2}{d} - \frac{3 a b B^3 c n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2}{d} + \\
& \frac{3 a A b B^2 x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2 + \frac{1}{2} a b B^3 n x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2 -}{2 d} - \\
& \frac{b^2 B^3 c n x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2}{2 d} + A b^2 B^2 x^3 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2 + \\
& \frac{a^3 B^3 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2}{b} - \\
& \frac{b^2 B^3 c^3 n \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2}{d^3} + \\
& \frac{3 a b B^3 c^2 n \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2}{d^2} - \\
& \frac{3 a^2 B^3 c n \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2}{d} + a^2 B^3 x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^3 + \\
& a b B^3 x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^3 + \frac{1}{3} b^2 B^3 x^3 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^3 -
\end{aligned}$$

$$\begin{aligned} & \frac{1}{b d^3} B^2 n^2 \left(2 A b^3 c^3 - 6 a A b^2 c^2 d + 6 a^2 A b c d^2 + 3 b^3 B c^3 n - 9 a b^2 B c^2 d n + 9 a^2 b B c d^2 n - \right. \\ & \quad \left. 3 a^3 B d^3 n - 2 a^3 B d^3 n \operatorname{Log}[a+b x] + 2 b B c \left(b^2 c^2 - 3 a b c d + 3 a^2 d^2 \right) n \operatorname{Log}[c+d x] + \right. \\ & \quad \left. 2 b^3 B c^3 \operatorname{Log}\left[e(a+b x)^n (c+d x)^{-n}\right] - 6 a b^2 B c^2 d \operatorname{Log}\left[e(a+b x)^n (c+d x)^{-n}\right] + \right. \\ & \quad \left. 6 a^2 b B c d^2 \operatorname{Log}\left[e(a+b x)^n (c+d x)^{-n}\right] \right) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] - \\ & \frac{1}{b d^3} 2 B^2 n^2 \left(-a^3 B d^3 n \operatorname{Log}[a+b x] + b B c \left(b^2 c^2 - 3 a b c d + 3 a^2 d^2 \right) n \operatorname{Log}[c+d x] + \right. \\ & \quad \left. a^3 d^3 \left(A+B \operatorname{Log}\left[e(a+b x)^n (c+d x)^{-n}\right] \right) \right) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] - \\ & \frac{2 a^3 B^3 n^3 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]}{b} + \frac{2 b^2 B^3 c^3 n^3 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]}{d^3} - \\ & \frac{6 a b B^3 c^2 n^3 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]}{d^2} + \frac{6 a^2 B^3 c n^3 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]}{d} - \\ & \frac{2 a^3 B^3 n^3 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]}{b} + \frac{2 b^2 B^3 c^3 n^3 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]}{d^3} - \\ & \frac{6 a b B^3 c^2 n^3 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]}{d^2} + \frac{6 a^2 B^3 c n^3 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]}{d} \end{aligned}$$

Problem 166: Result more than twice size of optimal antiderivative.

$$\int (a+b x) (A+B \operatorname{Log}[e(a+b x)^n (c+d x)^{-n}])^3 dx$$

Optimal (type 4, 376 leaves, 11 steps):

$$\begin{aligned} & \frac{3 B^2 (b c-a d)^2 n^2 \operatorname{Log}\left[\frac{b c-a d}{b(c+d x)}\right] (A+B \operatorname{Log}[e(a+b x)^n (c+d x)^{-n}])}{b d^2} - \\ & \frac{3 B (b c-a d) n (a+b x) (A+B \operatorname{Log}[e(a+b x)^n (c+d x)^{-n}])^2}{2 b d} - \\ & \frac{3 B (b c-a d)^2 n \operatorname{Log}\left[\frac{b c-a d}{b(c+d x)}\right] (A+B \operatorname{Log}[e(a+b x)^n (c+d x)^{-n}])^2}{2 b d^2} + \\ & \frac{(a+b x)^2 (A+B \operatorname{Log}[e(a+b x)^n (c+d x)^{-n}])^3}{2 b} - \frac{3 B^3 (b c-a d)^2 n^3 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{b d^2} - \\ & \frac{1}{b d^2} 3 B^2 (b c-a d)^2 n^2 (A+B \operatorname{Log}[e(a+b x)^n (c+d x)^{-n}]) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right] + \\ & \frac{3 B^3 (b c-a d)^2 n^3 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{b(c+d x)}\right]}{b d^2} \end{aligned}$$

Result (type 4, 2998 leaves):

$$\frac{1}{2 b d^2} \left(-12 a^2 A B^2 d^2 n^2 - 6 b^2 B^3 c^2 n^3 + 6 a b B^3 c d n^3 + 6 a^2 B^3 d^2 n^3 + 2 a A^3 b d^2 x - 3 A^2 b^2 B c d n x + \right.$$

$$\begin{aligned}
& 3 a A^2 b B d^2 n x + A^3 b^2 d^2 x^2 + 3 a^2 A^2 B d^2 n \operatorname{Log}[a+b x] - 6 a A b B^2 c d n^2 \operatorname{Log}[a+b x] + \\
& 6 a^2 A B^2 d^2 n^2 \operatorname{Log}[a+b x] + 12 a^2 B^3 d^2 n^3 \operatorname{Log}[a+b x] - 3 a^2 A B^2 d^2 n^2 \operatorname{Log}[a+b x]^2 + \\
& 3 a b B^3 c d n^3 \operatorname{Log}[a+b x]^2 - 3 a^2 B^3 d^2 n^3 \operatorname{Log}[a+b x]^2 + a^2 B^3 d^2 n^3 \operatorname{Log}[a+b x]^3 + \\
& 3 A^2 b^2 B c^2 n \operatorname{Log}[c+d x] - 6 a A^2 b B c d n \operatorname{Log}[c+d x] + 6 A b^2 B^2 c^2 n^2 \operatorname{Log}[c+d x] - \\
& 6 a A b B^2 c d n^2 \operatorname{Log}[c+d x] - 12 a^2 B^3 d^2 n^3 \operatorname{Log}[c+d x] - 6 A b^2 B^2 c^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] + \\
& 12 a A b B^2 c d n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] + 6 a^2 A B^2 d^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] - \\
& 6 b^2 B^3 c^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] + 6 a b B^3 c d n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] + \\
& 3 b^2 B^3 c^2 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x] - 6 a b B^3 c d n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x] - \\
& 6 a^2 B^3 d^2 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x] - 6 a^2 A B^2 d^2 n^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x] + \\
& 6 a^2 B^3 d^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x] + 3 A b^2 B^2 c^2 n^2 \operatorname{Log}[c+d x]^2 - \\
& 6 a A b B^2 c d n^2 \operatorname{Log}[c+d x]^2 + 3 b^2 B^3 c^2 n^3 \operatorname{Log}[c+d x]^2 - 3 a b B^3 c d n^3 \operatorname{Log}[c+d x]^2 - \\
& 6 b^2 B^3 c^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2 + 12 a b B^3 c d n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2 + \\
& 3 a^2 B^3 d^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2 + 3 b^2 B^3 c^2 n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2 - \\
& 6 a b B^3 c d n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2 - 3 a^2 B^3 d^2 n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2 + \\
& b^2 B^3 c^2 n^3 \operatorname{Log}[c+d x]^3 - 2 a b B^3 c d n^3 \operatorname{Log}[c+d x]^3 + \\
& 6 A b^2 B^2 c^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 12 a A b B^2 c d n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
& 6 b^2 B^3 c^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 12 a b B^3 c d n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
& 6 a^2 B^3 d^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 3 b^2 B^3 c^2 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
& 6 a b B^3 c d n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 3 a^2 B^3 d^2 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
& 6 b^2 B^3 c^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
& 12 a b B^3 c d n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
& 12 a^2 B^3 d^2 n^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + 6 a A^2 b B d^2 x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
& 6 A b^2 B^2 c d n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + 6 a A b B^2 d^2 n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
& 3 A^2 b^2 B d^2 x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + 6 a^2 A B^2 d^2 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
& 6 a b B^3 c d n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
& 6 a^2 B^3 d^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
& 3 a^2 B^3 d^2 n^2 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
& 6 A b^2 B^2 c^2 n \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
& 12 a A b B^2 c d n \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
& 6 b^2 B^3 c^2 n^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
& 6 a b B^3 c d n^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
& 6 b^2 B^3 c^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
& 12 a b B^3 c d n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
& 6 a^2 B^3 d^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
& 6 a^2 B^3 d^2 n^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] +
\end{aligned}$$

$$\begin{aligned}
 & 3 b^2 B^3 c^2 n^2 \text{Log}[c+d x]^2 \text{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
 & 6 a b B^3 c d n^2 \text{Log}[c+d x]^2 \text{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 6 b^2 B^3 c^2 n^2 \text{Log}[a+b x] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \text{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
 & 12 a b B^3 c d n^2 \text{Log}[a+b x] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \text{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 6 a A b B^2 d^2 x \text{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2 - 3 b^2 B^3 c d n x \text{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2 + \\
 & 3 a b B^3 d^2 n x \text{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2 + 3 A b^2 B^2 d^2 x^2 \text{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2 + \\
 & 3 a^2 B^3 d^2 n \text{Log}[a+b x] \text{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2 + 3 b^2 B^3 c^2 n \text{Log}[c+d x] \\
 & \text{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2 - 6 a b B^3 c d n \text{Log}[c+d x] \text{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2 + \\
 & 2 a b B^3 d^2 x \text{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^3 + b^2 B^3 d^2 x^2 \text{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^3 + 6 B^2 n^2 \\
 & (A b^2 c^2 - 2 a A b c d + b^2 B c^2 n - 2 a b B c d n + a^2 B d^2 n + a^2 B d^2 n \text{Log}[a+b x] + b B c (b c - 2 a d) n \\
 & \text{Log}[c+d x] + b^2 B c^2 \text{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - 2 a b B c d \text{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]) \\
 & \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] + 6 B^2 n^2 (a^2 B d^2 n \text{Log}[a+b x] + b B c (b c - 2 a d) n \text{Log}[c+d x] - \\
 & a^2 d^2 (A+B \text{Log}\left[e(a+b x)^n(c+d x)^{-n}\right])) \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] - \\
 & 6 b^2 B^3 c^2 n^3 \text{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] + 12 a b B^3 c d n^3 \text{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] - \\
 & 6 a^2 B^3 d^2 n^3 \text{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] - 6 b^2 B^3 c^2 n^3 \text{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right] + \\
 & 12 a b B^3 c d n^3 \text{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right] - 6 a^2 B^3 d^2 n^3 \text{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]
 \end{aligned}$$

Problem 167: Result more than twice size of optimal antiderivative.

$$\int \frac{(A+B \text{Log}\left[e(a+b x)^n(c+d x)^{-n}\right])^3}{a+b x} dx$$

Optimal (type 4, 186 leaves, 6 steps):

$$\begin{aligned}
 & \frac{(A+B \text{Log}\left[e(a+b x)^n(c+d x)^{-n}\right])^3 \text{Log}\left[1-\frac{b(c+d x)}{d(a+b x)}\right]}{b} + \\
 & \frac{3 B n (A+B \text{Log}\left[e(a+b x)^n(c+d x)^{-n}\right])^2 \text{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]}{b} + \\
 & \frac{6 B^2 n^2 (A+B \text{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]) \text{PolyLog}\left[3, \frac{b(c+d x)}{d(a+b x)}\right]}{b} + \frac{6 B^3 n^3 \text{PolyLog}\left[4, \frac{b(c+d x)}{d(a+b x)}\right]}{b}
 \end{aligned}$$

Result (type 4, 2513 leaves):

$$\begin{aligned}
 & \frac{1}{4 b} \left(4 A^3 \text{Log}[a+b x] - 6 A^2 B n \text{Log}[a+b x]^2 + \right. \\
 & \left. 4 A B^2 n^2 \text{Log}[a+b x]^3 - B^3 n^3 \text{Log}[a+b x]^4 + B^3 n^3 \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]^4 - \right.
 \end{aligned}$$

$$\begin{aligned}
& 4 B^3 n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]^3 \operatorname{Log}\left[-\frac{d(a+b x)}{b(c+d x)}\right] + 6 B^3 n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]^2 \operatorname{Log}\left[-\frac{d(a+b x)}{b(c+d x)}\right]^2 - \\
& 4 B^3 n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}\left[-\frac{d(a+b x)}{b(c+d x)}\right]^3 + B^3 n^3 \operatorname{Log}\left[-\frac{d(a+b x)}{b(c+d x)}\right]^4 - \\
& 12 A B^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2 + 12 B^3 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x]^2 + \\
& 12 A B^2 n^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2 - 12 B^3 n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2 - \\
& 8 B^3 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^3 + 8 B^3 n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^3 + \\
& 12 A^2 B n \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 12 A B^2 n^2 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
& 4 B^3 n^3 \operatorname{Log}[a+b x]^3 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 8 B^3 n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]^3 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
& 12 B^3 n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]^2 \operatorname{Log}\left[-\frac{d(a+b x)}{b(c+d x)}\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
& 24 A B^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
& 24 B^3 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
& 12 B^3 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 6 B^3 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]^2 + \\
& 12 B^3 n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]^2 - \\
& 18 B^3 n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]^2 + 12 A^2 B \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
& 12 A B^2 n \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
& 4 B^3 n^2 \operatorname{Log}[a+b x]^3 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
& 12 B^3 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
& 12 B^3 n^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
& 24 A B^2 n \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
& 12 B^3 n^2 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
& 24 B^3 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
& 12 A B^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2 - \\
& 6 B^3 n \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2 + \\
& 12 B^3 n \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2 + \\
& 4 B^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^3 - 4 B^3 n^3 \operatorname{Log}\left[-\frac{d(a+b x)}{b(c+d x)}\right]^3 \operatorname{Log}\left[\frac{b c-a d}{b c+b d x}\right] +
\end{aligned}$$

$$\begin{aligned}
 & 12 B n \left(A^2 + B^2 n^2 \operatorname{Log} \left[\frac{d(a+b x)}{-b c+a d} \right]^2 + B^2 n^2 \operatorname{Log}[c+d x]^2 + 2 B^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log} \left[\frac{b(c+d x)}{b c-a d} \right] - \right. \\
 & \quad 2 B^2 n^2 \operatorname{Log} \left[\frac{d(a+b x)}{-b c+a d} \right] \left(\operatorname{Log} \left[-\frac{d(a+b x)}{b(c+d x)} \right] + \operatorname{Log} \left[\frac{b(c+d x)}{b c-a d} \right] \right) + \\
 & \quad 2 A B \operatorname{Log} \left[e(a+b x)^n (c+d x)^{-n} \right] + B^2 \operatorname{Log} \left[e(a+b x)^n (c+d x)^{-n} \right]^2 + \\
 & \quad \left. 2 B n \operatorname{Log}[c+d x] \left(A - B n \operatorname{Log}[a+b x] + B \operatorname{Log} \left[e(a+b x)^n (c+d x)^{-n} \right] \right) \right) \\
 & \operatorname{PolyLog} \left[2, \frac{d(a+b x)}{-b c+a d} \right] - 12 B^3 n^3 \operatorname{Log} \left[-\frac{d(a+b x)}{b(c+d x)} \right]^2 \operatorname{PolyLog} \left[2, \frac{d(a+b x)}{b(c+d x)} \right] + \\
 & 12 B^3 n^3 \operatorname{Log} \left[\frac{d(a+b x)}{-b c+a d} \right]^2 \operatorname{PolyLog} \left[2, \frac{b(c+d x)}{b c-a d} \right] - \\
 & 24 B^3 n^3 \operatorname{Log} \left[\frac{d(a+b x)}{-b c+a d} \right] \operatorname{Log} \left[-\frac{d(a+b x)}{b(c+d x)} \right] \operatorname{PolyLog} \left[2, \frac{b(c+d x)}{b c-a d} \right] + \\
 & 12 B^3 n^3 \operatorname{Log} \left[-\frac{d(a+b x)}{b(c+d x)} \right]^2 \operatorname{PolyLog} \left[2, \frac{b(c+d x)}{b c-a d} \right] + \\
 & 24 A B^2 n^2 \operatorname{Log}[c+d x] \operatorname{PolyLog} \left[2, \frac{b(c+d x)}{b c-a d} \right] - \\
 & 24 B^3 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{PolyLog} \left[2, \frac{b(c+d x)}{b c-a d} \right] + \\
 & 12 B^3 n^3 \operatorname{Log}[c+d x]^2 \operatorname{PolyLog} \left[2, \frac{b(c+d x)}{b c-a d} \right] + \\
 & 24 B^3 n^3 \operatorname{Log}[a+b x] \operatorname{Log} \left[\frac{b(c+d x)}{b c-a d} \right] \operatorname{PolyLog} \left[2, \frac{b(c+d x)}{b c-a d} \right] - \\
 & 24 B^3 n^3 \operatorname{Log} \left[\frac{d(a+b x)}{-b c+a d} \right] \operatorname{Log} \left[\frac{b(c+d x)}{b c-a d} \right] \operatorname{PolyLog} \left[2, \frac{b(c+d x)}{b c-a d} \right] + \\
 & 24 B^3 n^2 \operatorname{Log}[c+d x] \operatorname{Log} \left[e(a+b x)^n (c+d x)^{-n} \right] \operatorname{PolyLog} \left[2, \frac{b(c+d x)}{b c-a d} \right] - \\
 & 24 A B^2 n^2 \operatorname{PolyLog} \left[3, \frac{d(a+b x)}{-b c+a d} \right] + 24 B^3 n^3 \operatorname{Log} \left[-\frac{d(a+b x)}{b(c+d x)} \right] \operatorname{PolyLog} \left[3, \frac{d(a+b x)}{-b c+a d} \right] - \\
 & 24 B^3 n^2 \operatorname{Log} \left[e(a+b x)^n (c+d x)^{-n} \right] \operatorname{PolyLog} \left[3, \frac{d(a+b x)}{-b c+a d} \right] + \\
 & 24 B^3 n^3 \operatorname{Log} \left[-\frac{d(a+b x)}{b(c+d x)} \right] \operatorname{PolyLog} \left[3, \frac{d(a+b x)}{b(c+d x)} \right] - \\
 & 24 A B^2 n^2 \operatorname{PolyLog} \left[3, \frac{b(c+d x)}{b c-a d} \right] + 24 B^3 n^3 \operatorname{Log} \left[-\frac{d(a+b x)}{b(c+d x)} \right] \operatorname{PolyLog} \left[3, \frac{b(c+d x)}{b c-a d} \right] - \\
 & 24 B^3 n^2 \operatorname{Log} \left[e(a+b x)^n (c+d x)^{-n} \right] \operatorname{PolyLog} \left[3, \frac{b(c+d x)}{b c-a d} \right] - 24 B^3 n^3 \operatorname{PolyLog} \left[4, \frac{d(a+b x)}{b(c+d x)} \right] \Big)
 \end{aligned}$$

Problem 168: Result more than twice size of optimal antiderivative.

$$\int \frac{(A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^3}{(a + b x)^2} dx$$

Optimal (type 3, 184 leaves, 5 steps):

$$\begin{aligned} & -\frac{6 B^3 n^3 (c + d x)}{(b c - a d) (a + b x)} - \frac{6 B^2 n^2 (c + d x) (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])}{(b c - a d) (a + b x)} - \\ & \frac{3 B n (c + d x) (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{(b c - a d) (a + b x)} - \frac{(c + d x) (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^3}{(b c - a d) (a + b x)} \end{aligned}$$

Result (type 3, 524 leaves):

$$\begin{aligned} & \frac{1}{b (b c - a d) (a + b x)} \left(-B^3 d n^3 (a + b x) \operatorname{Log}[a + b x]^3 + B^3 d n^3 (a + b x) \operatorname{Log}[c + d x]^3 + \right. \\ & 3 B^2 d n^2 (a + b x) \operatorname{Log}[c + d x]^2 (A + B n + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]) + \\ & 3 B^2 d n^2 (a + b x) \operatorname{Log}[a + b x]^2 (A + B n + B n \operatorname{Log}[c + d x] + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]) + \\ & 3 B d n (a + b x) \operatorname{Log}[c + d x] (A^2 + 2 A B n + 2 B^2 n^2 + \\ & 2 B (A + B n) \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}] + B^2 \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]^2) - \\ & (b c - a d) (A^3 + 3 A^2 B n + 6 A B^2 n^2 + 6 B^3 n^3 + 3 B (A^2 + 2 A B n + 2 B^2 n^2) \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}] + \\ & 3 B^2 (A + B n) \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]^2 + B^3 \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]^3) - 3 B d n (a + b x) \\ & \left. \operatorname{Log}[a + b x] (A^2 + 2 A B n + 2 B^2 n^2 + B^2 n^2 \operatorname{Log}[c + d x]^2 + 2 B (A + B n) \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}] + \right. \\ & \left. B^2 \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]^2 + 2 B n \operatorname{Log}[c + d x] (A + B n + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])) \right) \end{aligned}$$

Problem 172: Unable to integrate problem.

$$\int \frac{1}{(a g + b g x)^2 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])} dx$$

Optimal (type 4, 96 leaves, 4 steps):

$$\left(\frac{A}{e^{B n}} (c + d x) (e (a + b x)^n (c + d x)^{-n})^{\frac{1}{n}} \operatorname{ExpIntegralEi} \left[-\frac{A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]}{B n} \right] \right) / (B (b c - a d) g^2 n (a + b x))$$

Result (type 8, 38 leaves):

$$\int \frac{1}{(a g + b g x)^2 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])} dx$$

Problem 182: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^4 \left(A + B \operatorname{Log} \left[\frac{e (c + d x)}{a + b x} \right] \right)^2 dx$$

Optimal (type 4, 503 leaves, 19 steps):

$$\begin{aligned}
 & \frac{13 B^2 (b c - a d)^4 g^4 x}{30 d^4} - \frac{7 B^2 (b c - a d)^3 g^4 (a + b x)^2}{60 b d^3} + \\
 & \frac{B^2 (b c - a d)^2 g^4 (a + b x)^3}{30 b d^2} - \frac{5 B^2 (b c - a d)^5 g^4 \text{Log}[a + b x]}{6 b d^5} - \\
 & \frac{13 B^2 (b c - a d)^5 g^4 \text{Log}\left[\frac{c+d x}{a+b x}\right]}{30 b d^5} + \frac{B (b c - a d)^3 g^4 (a + b x)^2 (A + B \text{Log}\left[\frac{e(c+d x)}{a+b x}\right])}{5 b d^3} - \\
 & \frac{2 B (b c - a d)^2 g^4 (a + b x)^3 (A + B \text{Log}\left[\frac{e(c+d x)}{a+b x}\right])}{15 b d^2} + \frac{B (b c - a d) g^4 (a + b x)^4 (A + B \text{Log}\left[\frac{e(c+d x)}{a+b x}\right])}{10 b d} - \\
 & \frac{2 B (b c - a d)^4 g^4 (c + d x) (A + B \text{Log}\left[\frac{e(c+d x)}{a+b x}\right])}{5 d^5} + \frac{g^4 (a + b x)^5 (A + B \text{Log}\left[\frac{e(c+d x)}{a+b x}\right])^2}{5 b} - \\
 & \frac{2 B (b c - a d)^5 g^4 (A + B \text{Log}\left[\frac{e(c+d x)}{a+b x}\right]) \text{Log}\left[1 - \frac{d(a+b x)}{b(c+d x)}\right]}{5 b d^5} + \frac{2 B^2 (b c - a d)^5 g^4 \text{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{5 b d^5}
 \end{aligned}$$

Result (type 4, 2847 leaves):

$$\begin{aligned}
 & \frac{1}{60 b d^5} \\
 & g^4 \left(24 b^5 B^2 c^5 - 144 a b^4 B^2 c^4 d + 360 a^2 b^3 B^2 c^3 d^2 - 480 a^3 b^2 B^2 c^2 d^3 + 336 a^4 b B^2 c d^4 - 96 a^5 B^2 d^5 - \right. \\
 & 24 a b^5 B c^4 d x + 26 b^5 B^2 c^4 d x + 120 a A b^4 B c^3 d^2 x - 118 a b^4 B^2 c^3 d^2 x - 240 a^2 A b^3 B c^2 d^3 x + \\
 & 204 a^2 b^3 B^2 c^2 d^3 x + 240 a^3 A b^2 B c d^4 x - 158 a^3 b^2 B^2 c d^4 x + 60 a^4 A^2 b d^5 x - 96 a^4 A b B d^5 x + \\
 & 46 a^4 b B^2 d^5 x + 12 A b^5 B c^3 d^2 x^2 - 7 b^5 B^2 c^3 d^2 x^2 - 60 a A b^4 B c^2 d^3 x^2 + 27 a b^4 B^2 c^2 d^3 x^2 + \\
 & 120 a^2 A b^3 B c d^4 x^2 - 33 a^2 b^3 B^2 c d^4 x^2 + 120 a^3 A^2 b^2 d^5 x^2 - 72 a^3 A b^2 B d^5 x^2 + \\
 & 13 a^3 b^2 B^2 d^5 x^2 - 8 A b^5 B c^2 d^3 x^3 + 2 b^5 B^2 c^2 d^3 x^3 + 40 a A b^4 B c d^4 x^3 - 4 a b^4 B^2 c d^4 x^3 + \\
 & 120 a^2 A^2 b^3 d^5 x^3 - 32 a^2 A b^3 B d^5 x^3 + 2 a^2 b^3 B^2 d^5 x^3 + 6 A b^5 B c d^4 x^4 + 60 a A^2 b^4 d^5 x^4 - \\
 & 6 a A b^4 B d^5 x^4 + 12 A^2 b^5 d^5 x^5 + 24 a b^4 B^2 c^4 d \text{Log}\left[\frac{a}{b} + x\right] - 120 a^2 b^3 B^2 c^3 d^2 \text{Log}\left[\frac{a}{b} + x\right] + \\
 & 240 a^3 b^2 B^2 c^2 d^3 \text{Log}\left[\frac{a}{b} + x\right] - 240 a^4 b B^2 c d^4 \text{Log}\left[\frac{a}{b} + x\right] + 96 a^5 B^2 d^5 \text{Log}\left[\frac{a}{b} + x\right] + \\
 & 12 a^5 B^2 d^5 \text{Log}\left[\frac{a}{b} + x\right]^2 - 24 b^5 B^2 c^5 \text{Log}\left[\frac{c}{d} + x\right] + 120 a b^4 B^2 c^4 d \text{Log}\left[\frac{c}{d} + x\right] - \\
 & 240 a^2 b^3 B^2 c^3 d^2 \text{Log}\left[\frac{c}{d} + x\right] + 240 a^3 b^2 B^2 c^2 d^3 \text{Log}\left[\frac{c}{d} + x\right] - 96 a^4 b B^2 c d^4 \text{Log}\left[\frac{c}{d} + x\right] + \\
 & 12 b^5 B^2 c^5 \text{Log}\left[\frac{c}{d} + x\right]^2 - 60 a b^4 B^2 c^4 d \text{Log}\left[\frac{c}{d} + x\right]^2 + 120 a^2 b^3 B^2 c^3 d^2 \text{Log}\left[\frac{c}{d} + x\right]^2 - \\
 & 120 a^3 b^2 B^2 c^2 d^3 \text{Log}\left[\frac{c}{d} + x\right]^2 + 60 a^4 b B^2 c d^4 \text{Log}\left[\frac{c}{d} + x\right]^2 + 12 a^2 b^3 B^2 c^3 d^2 \text{Log}[a + b x] - \\
 & 52 a^3 b^2 B^2 c^2 d^3 \text{Log}[a + b x] + 86 a^4 b B^2 c d^4 \text{Log}[a + b x] - 24 a^5 A B d^5 \text{Log}[a + b x] - \\
 & 46 a^5 B^2 d^5 \text{Log}[a + b x] - 24 a^5 B^2 d^5 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] + 24 a^5 B^2 d^5 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] - \\
 & 24 a^5 B^2 d^5 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + 24 A b^5 B c^5 \text{Log}[c + d x] - 26 b^5 B^2 c^5 \text{Log}[c + d x] - \\
 & 120 a A b^4 B c^4 d \text{Log}[c + d x] + 106 a b^4 B^2 c^4 d \text{Log}[c + d x] + 240 a^2 A b^3 B c^3 d^2 \text{Log}[c + d x] - \\
 & 152 a^2 b^3 B^2 c^3 d^2 \text{Log}[c + d x] - 240 a^3 A b^2 B c^2 d^3 \text{Log}[c + d x] + 72 a^3 b^2 B^2 c^2 d^3 \text{Log}[c + d x] + \\
 & 120 a^4 A b B c d^4 \text{Log}[c + d x] + 24 b^5 B^2 c^5 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[c + d x] -
 \end{aligned}$$

$$\begin{aligned}
& 120 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]+240 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]- \\
& 240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]+120 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]- \\
& 24 b^5 B^2 c^5 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]+120 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]- \\
& 240 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]+240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]- \\
& 120 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]-24 b^5 B^2 c^5 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+ \\
& 120 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]-240 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+ \\
& 240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]-120 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]- \\
& 24 b^5 B^2 c^4 d x \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]+120 a b^4 B^2 c^3 d^2 x \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]- \\
& 240 a^2 b^3 B^2 c^2 d^3 x \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]+240 a^3 b^2 B^2 c d^4 x \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]+ \\
& 120 a^4 A b B d^5 x \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]-96 a^4 b B^2 d^5 x \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]+ \\
& 12 b^5 B^2 c^3 d^2 x^2 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]-60 a b^4 B^2 c^2 d^3 x^2 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]+ \\
& 120 a^2 b^3 B^2 c d^4 x^2 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]+240 a^3 A b^2 B d^5 x^2 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]- \\
& 72 a^3 b^2 B^2 d^5 x^2 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]-8 b^5 B^2 c^2 d^3 x^3 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]+ \\
& 40 a b^4 B^2 c d^4 x^3 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]+240 a^2 A b^3 B d^5 x^3 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]- \\
& 32 a^2 b^3 B^2 d^5 x^3 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]+6 b^5 B^2 c d^4 x^4 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]+ \\
& 120 a A b^4 B d^5 x^4 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]-6 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]+ \\
& 24 A b^5 B d^5 x^5 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]-24 a^5 B^2 d^5 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]+ \\
& 24 b^5 B^2 c^5 \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]-120 a b^4 B^2 c^4 d \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]+ \\
& 240 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]-240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]+ \\
& 120 a^4 b B^2 c d^4 \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]+60 a^4 b B^2 d^5 x \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]^2+ \\
& 120 a^3 b^2 B^2 d^5 x^2 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]^2+120 a^2 b^3 B^2 d^5 x^3 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]^2+ \\
& 60 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]^2+12 b^5 B^2 d^5 x^5 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]^2-
\end{aligned}$$

$$24 b B^2 c (b^4 c^4 - 5 a b^3 c^3 d + 10 a^2 b^2 c^2 d^2 - 10 a^3 b c d^3 + 5 a^4 d^4) \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] -$$

$$24 a^5 B^2 d^5 \text{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right]$$

Problem 183: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^3 \left(A + B \text{Log}\left[\frac{e(c+d x)}{a+b x}\right] \right)^2 dx$$

Optimal (type 4, 420 leaves, 15 steps):

$$-\frac{5 B^2 (b c - a d)^3 g^3 x}{12 d^3} + \frac{B^2 (b c - a d)^2 g^3 (a + b x)^2}{12 b d^2} +$$

$$\frac{11 B^2 (b c - a d)^4 g^3 \text{Log}[a + b x]}{12 b d^4} + \frac{5 B^2 (b c - a d)^4 g^3 \text{Log}\left[\frac{c+d x}{a+b x}\right]}{12 b d^4} -$$

$$\frac{B (b c - a d)^2 g^3 (a + b x)^2 \left(A + B \text{Log}\left[\frac{e(c+d x)}{a+b x}\right] \right)}{4 b d^2} + \frac{B (b c - a d) g^3 (a + b x)^3 \left(A + B \text{Log}\left[\frac{e(c+d x)}{a+b x}\right] \right)}{6 b d} +$$

$$\frac{B (b c - a d)^3 g^3 (c + d x) \left(A + B \text{Log}\left[\frac{e(c+d x)}{a+b x}\right] \right)}{2 d^4} + \frac{g^3 (a + b x)^4 \left(A + B \text{Log}\left[\frac{e(c+d x)}{a+b x}\right] \right)^2}{4 b} +$$

$$\frac{B (b c - a d)^4 g^3 \left(A + B \text{Log}\left[\frac{e(c+d x)}{a+b x}\right] \right) \text{Log}\left[1 - \frac{d(a+b x)}{b(c+d x)}\right]}{2 b d^4} - \frac{B^2 (b c - a d)^4 g^3 \text{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{2 b d^4}$$

Result (type 4, 2110 leaves):

$$\frac{1}{12 b d^4}$$

$$g^3 \left(-6 a^2 B^2 c^4 + 30 a b^3 B^2 c^3 d - 60 a^2 b^2 B^2 c^2 d^2 + 54 a^3 b B^2 c d^3 - 18 a^4 B^2 d^4 + 6 A b^4 B c^3 d x - 5 b^4 B^2 c^3 \right.$$

$$d x - 24 a A b^3 B c^2 d^2 x + 17 a b^3 B^2 c^2 d^2 x + 36 a^2 A b^2 B c d^3 x - 19 a^2 b^2 B^2 c d^3 x + 12 a^3 A^2 b d^4 x -$$

$$18 a^3 A b B d^4 x + 7 a^3 b B^2 d^4 x - 3 A b^4 B c^2 d^2 x^2 + b^4 B^2 c^2 d^2 x^2 + 12 a A b^3 B c d^3 x^2 - 2 a b^3 B^2 c d^3 x^2 +$$

$$18 a^2 A^2 b^2 d^4 x^2 - 9 a^2 A b^2 B d^4 x^2 + a^2 b^2 B^2 d^4 x^2 + 2 A b^4 B c d^3 x^3 + 12 a A^2 b^3 d^4 x^3 - 2 a A b^3 B d^4 x^3 +$$

$$3 A^2 b^4 d^4 x^4 - 6 a b^3 B^2 c^3 d \text{Log}\left[\frac{a}{b} + x\right] + 24 a^2 b^2 B^2 c^2 d^2 \text{Log}\left[\frac{a}{b} + x\right] - 36 a^3 b B^2 c d^3 \text{Log}\left[\frac{a}{b} + x\right] +$$

$$18 a^4 B^2 d^4 \text{Log}\left[\frac{a}{b} + x\right] + 3 a^4 B^2 d^4 \text{Log}\left[\frac{a}{b} + x\right]^2 + 6 b^4 B^2 c^4 \text{Log}\left[\frac{c}{d} + x\right] - 24 a b^3 B^2 c^3 d \text{Log}\left[\frac{c}{d} + x\right] +$$

$$36 a^2 b^2 B^2 c^2 d^2 \text{Log}\left[\frac{c}{d} + x\right] - 18 a^3 b B^2 c d^3 \text{Log}\left[\frac{c}{d} + x\right] - 3 b^4 B^2 c^4 \text{Log}\left[\frac{c}{d} + x\right]^2 +$$

$$12 a b^3 B^2 c^3 d \text{Log}\left[\frac{c}{d} + x\right]^2 - 18 a^2 b^2 B^2 c^2 d^2 \text{Log}\left[\frac{c}{d} + x\right]^2 + 12 a^3 b B^2 c d^3 \text{Log}\left[\frac{c}{d} + x\right]^2 -$$

$$3 a^2 b^2 B^2 c^2 d^2 \text{Log}[a + b x] + 10 a^3 b B^2 c d^3 \text{Log}[a + b x] - 6 a^4 A B d^4 \text{Log}[a + b x] -$$

$$7 a^4 B^2 d^4 \text{Log}[a + b x] - 6 a^4 B^2 d^4 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] + 6 a^4 B^2 d^4 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] -$$

$$6 a^4 B^2 d^4 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] - 6 A b^4 B c^4 \text{Log}[c + d x] + 5 b^4 B^2 c^4 \text{Log}[c + d x] +$$

$$24 a A b^3 B c^3 d \text{Log}[c + d x] - 14 a b^3 B^2 c^3 d \text{Log}[c + d x] - 36 a^2 A b^2 B c^2 d^2 \text{Log}[c + d x] +$$

$$\begin{aligned}
 & 9 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}[c+d x]+24 a^3 A b B c d^3 \operatorname{Log}[c+d x]-6 b^4 B^2 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]+ \\
 & 24 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]-36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]+ \\
 & 24 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]+6 b^4 B^2 c^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]- \\
 & 24 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]+36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]- \\
 & 24 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]+6 b^4 B^2 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]- \\
 & 24 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]- \\
 & 24 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+6 b^4 B^2 c^3 d x \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]- \\
 & 24 a b^3 B^2 c^2 d^2 x \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]+36 a^2 b^2 B^2 c d^3 x \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]+ \\
 & 24 a^3 A b B d^4 x \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]-18 a^3 b B^2 d^4 x \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]- \\
 & 3 b^4 B^2 c^2 d^2 x^2 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]+12 a b^3 B^2 c d^3 x^2 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]+ \\
 & 36 a^2 A b^2 B d^4 x^2 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]-9 a^2 b^2 B^2 d^4 x^2 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]+ \\
 & 2 b^4 B^2 c d^3 x^3 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]+24 a A b^3 B d^4 x^3 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]- \\
 & 2 a b^3 B^2 d^4 x^3 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]+6 A b^4 B d^4 x^4 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]- \\
 & 6 a^4 B^2 d^4 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]-6 b^4 B^2 c^4 \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]+ \\
 & 24 a b^3 B^2 c^3 d \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]-36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]+ \\
 & 24 a^3 b B^2 c d^3 \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]+12 a^3 b B^2 d^4 x \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]^2+ \\
 & 18 a^2 b^2 B^2 d^4 x^2 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]^2+12 a b^3 B^2 d^4 x^3 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]^2+ \\
 & 3 b^4 B^2 d^4 x^4 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]^2+6 b B^2 c\left(b^3 c^3-4 a b^2 c^2 d+6 a^2 b c d^2-4 a^3 d^3\right) \\
 & \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]-6 a^4 B^2 d^4 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]
 \end{aligned}$$

Problem 184: Result more than twice size of optimal antiderivative.

$$\int (a g+b g x)^2\left(A+B \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]\right)^2 d x$$

Optimal (type 4, 335 leaves, 11 steps):

$$\frac{B^2 (b c - a d)^2 g^2 x}{3 d^2} - \frac{B^2 (b c - a d)^3 g^2 \text{Log}[a + b x]}{b d^3} -$$

$$\frac{B^2 (b c - a d)^3 g^2 \text{Log}\left[\frac{c+d x}{a+b x}\right]}{3 b d^3} + \frac{B (b c - a d) g^2 (a + b x)^2 \left(A + B \text{Log}\left[\frac{e(c+d x)}{a+b x}\right]\right)}{3 b d} -$$

$$\frac{2 B (b c - a d)^2 g^2 (c + d x) \left(A + B \text{Log}\left[\frac{e(c+d x)}{a+b x}\right]\right)}{3 d^3} + \frac{g^2 (a + b x)^3 \left(A + B \text{Log}\left[\frac{e(c+d x)}{a+b x}\right]\right)^2}{3 b} -$$

$$\frac{2 B (b c - a d)^3 g^2 \left(A + B \text{Log}\left[\frac{e(c+d x)}{a+b x}\right]\right) \text{Log}\left[1 - \frac{d(a+b x)}{b(c+d x)}\right]}{3 b d^3} + \frac{2 B^2 (b c - a d)^3 g^2 \text{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{3 b d^3}$$

Result (type 4, 1398 leaves):

$$g^2 \left(a^2 A^2 x + a A^2 b x^2 + \frac{1}{3} A^2 b^2 x^3 + \right.$$

$$2 a^2 A B \left(\frac{(-b c + a d) (a d \text{Log}[a + b x] - b c \text{Log}[c + d x])}{b^2 c d - a b d^2} + x \text{Log}\left[\frac{c e + d e x}{a + b x}\right] \right) +$$

$$4 a A b B \left(-\frac{1}{2} (-b c + a d) \left(\frac{x}{b d} + \frac{a^2 \text{Log}[a + b x]}{b^2 (b c - a d)} - \frac{c^2 \text{Log}[c + d x]}{d^2 (b c - a d)} \right) + \frac{1}{2} x^2 \text{Log}\left[\frac{c e + d e x}{a + b x}\right] \right) +$$

$$2 A b^2 B \left(-\left((-b c + a d) (b d (b c - a d) x - 2 b c - 2 a d + b d x) - 2 a^3 d^3 \text{Log}[a + b x] + \right. \right.$$

$$\left. \left. 2 b^3 c^3 \text{Log}[c + d x] \right) / (6 b^3 d^3 (b c - a d)) + \frac{1}{3} x^3 \text{Log}\left[\frac{c e + d e x}{a + b x}\right] \right) +$$

$$a^2 B^2 \left(x \text{Log}\left[\frac{c e + d e x}{a + b x}\right]^2 - \frac{1}{b d (b c - a d)} (-b c + a d) \left(a d \text{Log}\left[\frac{a}{b} + x\right]^2 + b c \text{Log}\left[\frac{c}{d} + x\right]^2 - \right. \right.$$

$$2 a d \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] + 2 a d \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] - 2 a d \text{Log}\left[\frac{c}{d} + x\right]$$

$$\text{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + 2 b c \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[c + d x] - 2 b c \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[c + d x] -$$

$$2 b c \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c+d x)}{b c - a d}\right] - 2 a d \text{Log}[a + b x] \text{Log}\left[\frac{e(c+d x)}{a + b x}\right] + 2 b c \text{Log}[c + d x]$$

$$\left. \left. \text{Log}\left[\frac{e(c+d x)}{a + b x}\right] - 2 b c \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] - 2 a d \text{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] \right) \right) +$$

$$2 a b B^2 \left(\frac{1}{2} x^2 \text{Log}\left[\frac{c e + d e x}{a + b x}\right]^2 + \frac{1}{2 b^2 d^2} \left(2 d (-b c + a d) (a + b x) \left(-1 + \text{Log}\left[\frac{a}{b} + x\right] \right) - \right. \right.$$

$$a^2 d^2 \text{Log}\left[\frac{a}{b} + x\right]^2 + 2 b (b c - a d) (c + d x) \left(-1 + \text{Log}\left[\frac{c}{d} + x\right] \right) - b^2 c^2 \text{Log}\left[\frac{c}{d} + x\right]^2 +$$

$$2 (a^2 d^2 \text{Log}[a + b x] - b (d (-b c + a d) x + b c^2 \text{Log}[c + d x])) \left(\text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] + \right.$$

$$\left. \left. \text{Log}\left[\frac{e(c+d x)}{a + b x}\right] \right) + 2 b^2 c^2 \left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] \right) \right) +$$

$$2 a^2 d^2 \left(\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + \text{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] \right) \right) +$$

$$\begin{aligned}
 & b^2 B^2 \left(\frac{1}{3} x^3 \text{Log} \left[\frac{c e + d e x}{a + b x} \right]^2 + \frac{1}{6 b^3 d^3} \left(-4 d (-b c + a d) (b c + a d) (a + b x) \left(-1 + \text{Log} \left[\frac{a}{b} + x \right] \right) + \right. \right. \\
 & \quad 2 a^3 d^3 \text{Log} \left[\frac{a}{b} + x \right]^2 - 4 b (b c - a d) (b c + a d) (c + d x) \left(-1 + \text{Log} \left[\frac{c}{d} + x \right] \right) + \\
 & \quad 2 b^3 c^3 \text{Log} \left[\frac{c}{d} + x \right]^2 + d^2 (-b c + a d) \left(b x (2 a - b x) + 2 b^2 x^2 \text{Log} \left[\frac{a}{b} + x \right] - 2 a^2 \text{Log} [a + b x] \right) + \\
 & \quad b^2 (b c - a d) \left(d x (2 c - d x) + 2 d^2 x^2 \text{Log} \left[\frac{c}{d} + x \right] - 2 c^2 \text{Log} [c + d x] \right) + \\
 & \quad \left. 2 (b d (b c - a d) x (-2 b c - 2 a d + b d x) - 2 a^3 d^3 \text{Log} [a + b x] + 2 b^3 c^3 \text{Log} [c + d x]) \right. \\
 & \quad \left. \left(\text{Log} \left[\frac{a}{b} + x \right] - \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{e (c + d x)}{a + b x} \right] \right) - \right. \\
 & \quad \left. 4 b^3 c^3 \left(\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + \text{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) - \right. \\
 & \quad \left. 4 a^3 d^3 \left(\text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \text{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) \right)
 \end{aligned}$$

Problem 185: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x) \left(A + B \text{Log} \left[\frac{e (c + d x)}{a + b x} \right] \right)^2 dx$$

Optimal (type 4, 202 leaves, 7 steps):

$$\begin{aligned}
 & \frac{B^2 (b c - a d)^2 g \text{Log} [a + b x]}{b d^2} + \\
 & \frac{B (b c - a d) g (c + d x) \left(A + B \text{Log} \left[\frac{e (c + d x)}{a + b x} \right] \right)}{d^2} + \frac{g (a + b x)^2 \left(A + B \text{Log} \left[\frac{e (c + d x)}{a + b x} \right] \right)^2}{2 b} + \\
 & \frac{B (b c - a d)^2 g \left(A + B \text{Log} \left[\frac{e (c + d x)}{a + b x} \right] \right) \text{Log} \left[1 - \frac{d (a + b x)}{b (c + d x)} \right]}{b d^2} - \frac{B^2 (b c - a d)^2 g \text{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{b d^2}
 \end{aligned}$$

Result (type 4, 734 leaves):

$$\frac{1}{2 b d^2} g \left(2 a A^2 b d^2 x + A^2 b^2 d^2 x^2 - 4 a A B d \left(a d \operatorname{Log}[a+b x] - b \left(c \operatorname{Log}[c+d x] + d x \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right] \right) \right) \right) +$$

$$2 A B \left(a^2 d^2 \operatorname{Log}[a+b x] + b \left(-b c^2 \operatorname{Log}[c+d x] + d x \left(b c - a d + b d x \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right] \right) \right) \right) +$$

$$2 a B^2 d \left(a d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + b c \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 a d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a+b x] +$$

$$2 a d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a+b x] - 2 a d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + 2 b c \operatorname{Log}\left[\frac{a}{b} + x\right]$$

$$\operatorname{Log}[c+d x] - 2 b c \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c+d x] - 2 b c \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] -$$

$$2 a d \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right] + 2 b c \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right] +$$

$$b d x \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]^2 - 2 b c \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] - 2 a d \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] \right) +$$

$$B^2 \left(2 d (-b c + a d) (a+b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) - a^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 +$$

$$2 b (b c - a d) (c+d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) - b^2 c^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + b^2 d^2 x^2 \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right]^2 +$$

$$2 (a^2 d^2 \operatorname{Log}[a+b x] - b (d (-b c + a d) x + b c^2 \operatorname{Log}[c+d x])) \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] +$$

$$\operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right] \right) + 2 b^2 c^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] \right) +$$

$$2 a^2 d^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] \right) \right)$$

Problem 186: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right] \right)^2}{a g + b g x} dx$$

Optimal (type 4, 128 leaves, 4 steps):

$$\frac{\operatorname{Log}\left[-\frac{b c - a d}{d(a+b x)}\right] \left(A + B \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right] \right)^2}{b g} -$$

$$\frac{2 B \left(A + B \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right] \right) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]}{b g} + \frac{2 B^2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{d(a+b x)}\right]}{b g}$$

Result (type 4, 454 leaves):

$$\frac{1}{3 b g} \left(3 A^2 \operatorname{Log}[a+b x] - 3 A B \left(\operatorname{Log}\left[\frac{a}{b}+x\right]^2 - 2 \operatorname{Log}[a+b x] \left(\operatorname{Log}\left[\frac{a}{b}+x\right] - \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right] \right) - 2 \left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) \right) + B^2 \left(\operatorname{Log}\left[\frac{a}{b}+x\right]^3 + 3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + 3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \left(-\operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \right) + 3 \operatorname{Log}[a+b x] \left(\operatorname{Log}\left[\frac{a}{b}+x\right] - \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right] \right)^2 + 6 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] + 6 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] - 3 \left(\operatorname{Log}\left[\frac{a}{b}+x\right] - \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{e(c+d x)}{a+b x}\right] \right) \left(\operatorname{Log}\left[\frac{a}{b}+x\right]^2 - 2 \left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) \right) - 6 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] - 6 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right] \right)$$

Problem 210: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^4 \left(A + B \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] \right)^2 dx$$

Optimal (type 4, 515 leaves, 19 steps):

$$\frac{26 B^2 (b c - a d)^4 g^4 x}{15 d^4} - \frac{7 B^2 (b c - a d)^3 g^4 (a + b x)^2}{15 b d^3} + \frac{2 B^2 (b c - a d)^2 g^4 (a + b x)^3}{15 b d^2} - \frac{10 B^2 (b c - a d)^5 g^4 \operatorname{Log}[a + b x]}{3 b d^5} - \frac{26 B^2 (b c - a d)^5 g^4 \operatorname{Log}\left[\frac{c+d x}{a+b x}\right]}{15 b d^5} + \frac{2 B (b c - a d)^3 g^4 (a + b x)^2 \left(A + B \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] \right)}{5 b d^3} - \frac{4 B (b c - a d)^2 g^4 (a + b x)^3 \left(A + B \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] \right)}{15 b d^2} + \frac{B (b c - a d) g^4 (a + b x)^4 \left(A + B \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] \right)}{5 b d} + \frac{4 B (b c - a d)^4 g^4 (c + d x) \left(A + B \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] \right)}{5 d^5} + \frac{g^4 (a + b x)^5 \left(A + B \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] \right)^2}{5 b} - \frac{4 B (b c - a d)^5 g^4 \left(A + B \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] \right) \operatorname{Log}\left[1 - \frac{d(a+b x)}{b(c+d x)}\right]}{5 b d^5} + \frac{8 B^2 (b c - a d)^5 g^4 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{5 b d^5}$$

Result (type 4, 2907 leaves):

$$\frac{1}{15 b d^5}$$

$$\begin{aligned}
 & g^4 \left(24 b^5 B^2 c^5 - 144 a b^4 B^2 c^4 d + 360 a^2 b^3 B^2 c^3 d^2 - 480 a^3 b^2 B^2 c^2 d^3 + 336 a^4 b B^2 c d^4 - 96 a^5 B^2 d^5 - \right. \\
 & 12 A b^5 B c^4 d x + 26 b^5 B^2 c^4 d x + 60 a A b^4 B c^3 d^2 x - 118 a b^4 B^2 c^3 d^2 x - 120 a^2 A b^3 B c^2 d^3 x + \\
 & 204 a^2 b^3 B^2 c^2 d^3 x + 120 a^3 A b^2 B c d^4 x - 158 a^3 b^2 B^2 c d^4 x + 15 a^4 A^2 b d^5 x - 48 a^4 A b B d^5 x + \\
 & 46 a^4 b B^2 d^5 x + 6 A b^5 B c^3 d^2 x^2 - 7 b^5 B^2 c^3 d^2 x^2 - 30 a A b^4 B c^2 d^3 x^2 + 27 a b^4 B^2 c^2 d^3 x^2 + \\
 & 60 a^2 A b^3 B c d^4 x^2 - 33 a^2 b^3 B^2 c d^4 x^2 + 30 a^3 A^2 b^2 d^5 x^2 - 36 a^3 A b^2 B d^5 x^2 + \\
 & 13 a^3 b^2 B^2 d^5 x^2 - 4 A b^5 B c^2 d^3 x^3 + 2 b^5 B^2 c^2 d^3 x^3 + 20 a A b^4 B c d^4 x^3 - 4 a b^4 B^2 c d^4 x^3 + \\
 & 30 a^2 A^2 b^3 d^5 x^3 - 16 a^2 A b^3 B d^5 x^3 + 2 a^2 b^3 B^2 d^5 x^3 + 3 A b^5 B c d^4 x^4 + 15 a A^2 b^4 d^5 x^4 - \\
 & 3 a A b^4 B d^5 x^4 + 3 A^2 b^5 d^5 x^5 + 24 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b} + x\right] - 120 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \\
 & 240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] - 240 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] + 96 a^5 B^2 d^5 \operatorname{Log}\left[\frac{a}{b} + x\right] + \\
 & 12 a^5 B^2 d^5 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 24 b^5 B^2 c^5 \operatorname{Log}\left[\frac{c}{d} + x\right] + 120 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{c}{d} + x\right] - \\
 & 240 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] - 96 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] + \\
 & 12 b^5 B^2 c^5 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 60 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 120 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - \\
 & 120 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 60 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 12 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}[a + b x] - \\
 & 52 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}[a + b x] + 86 a^4 b B^2 c d^4 \operatorname{Log}[a + b x] - 12 a^5 A B d^5 \operatorname{Log}[a + b x] - \\
 & 46 a^5 B^2 d^5 \operatorname{Log}[a + b x] - 24 a^5 B^2 d^5 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 24 a^5 B^2 d^5 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - \\
 & 24 a^5 B^2 d^5 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 12 A b^5 B c^5 \operatorname{Log}[c + d x] - 26 b^5 B^2 c^5 \operatorname{Log}[c + d x] - \\
 & 60 a A b^4 B c^4 d \operatorname{Log}[c + d x] + 106 a b^4 B^2 c^4 d \operatorname{Log}[c + d x] + 120 a^2 A b^3 B c^3 d^2 \operatorname{Log}[c + d x] - \\
 & 152 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}[c + d x] - 120 a^3 A b^2 B c^2 d^3 \operatorname{Log}[c + d x] + 72 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}[c + d x] + \\
 & 60 a^4 A b B c d^4 \operatorname{Log}[c + d x] + 24 b^5 B^2 c^5 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - \\
 & 120 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + 240 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - \\
 & 240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + 120 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - \\
 & 24 b^5 B^2 c^5 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + 120 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - \\
 & 240 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + 240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - \\
 & 120 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 24 b^5 B^2 c^5 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + \\
 & 120 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - 240 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + \\
 & 240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - 120 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - \\
 & 12 b^5 B^2 c^4 d x \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] + 60 a b^4 B^2 c^3 d^2 x \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] -
 \end{aligned}$$

$$\begin{aligned}
 & 120 a^2 b^3 B^2 c^2 d^3 x \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] + 120 a^3 b^2 B^2 c d^4 x \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] + \\
 & 30 a^4 A b B d^5 x \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] - 48 a^4 b B^2 d^5 x \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] + \\
 & 6 b^5 B^2 c^3 d^2 x^2 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] - 30 a b^4 B^2 c^2 d^3 x^2 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] + \\
 & 60 a^2 b^3 B^2 c d^4 x^2 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] + 60 a^3 A b^2 B d^5 x^2 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] - \\
 & 36 a^3 b^2 B^2 d^5 x^2 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] - 4 b^5 B^2 c^2 d^3 x^3 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] + \\
 & 20 a b^4 B^2 c d^4 x^3 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] + 60 a^2 A b^3 B d^5 x^3 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] - \\
 & 16 a^2 b^3 B^2 d^5 x^3 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] + 3 b^5 B^2 c d^4 x^4 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] + \\
 & 30 a A b^4 B d^5 x^4 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] - 3 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] + \\
 & 6 A b^5 B d^5 x^5 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] - 12 a^5 B^2 d^5 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] + \\
 & 12 b^5 B^2 c^5 \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] - 60 a b^4 B^2 c^4 d \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] + \\
 & 120 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] - 120 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] + \\
 & 60 a^4 b B^2 c d^4 \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] + 15 a^4 b B^2 d^5 x \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]^2 + \\
 & 30 a^3 b^2 B^2 d^5 x^2 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]^2 + 30 a^2 b^3 B^2 d^5 x^3 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]^2 + \\
 & 15 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]^2 + 3 b^5 B^2 d^5 x^5 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]^2 - \\
 & 24 b B^2 c (b^4 c^4 - 5 a b^3 c^3 d + 10 a^2 b^2 c^2 d^2 - 10 a^3 b c d^3 + 5 a^4 d^4) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] - \\
 & 24 a^5 B^2 d^5 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]
 \end{aligned}$$

Problem 211: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^3 \left(A + B \operatorname{Log} \left[\frac{e (c + d x)^2}{(a + b x)^2} \right] \right)^2 dx$$

Optimal (type 4, 422 leaves, 15 steps):

$$\begin{aligned} & -\frac{5 B^2 (b c - a d)^3 g^3 x}{3 d^3} + \frac{B^2 (b c - a d)^2 g^3 (a + b x)^2}{3 b d^2} + \\ & \frac{11 B^2 (b c - a d)^4 g^3 \operatorname{Log}[a + b x]}{3 b d^4} + \frac{5 B^2 (b c - a d)^4 g^3 \operatorname{Log}\left[\frac{c+d x}{a+b x}\right]}{3 b d^4} - \\ & \frac{B (b c - a d)^2 g^3 (a + b x)^2 \left(A + B \operatorname{Log}\left[\frac{e (c+d x)^2}{(a+b x)^2}\right] \right)}{2 b d^2} + \frac{B (b c - a d) g^3 (a + b x)^3 \left(A + B \operatorname{Log}\left[\frac{e (c+d x)^2}{(a+b x)^2}\right] \right)}{3 b d} + \\ & \frac{B (b c - a d)^3 g^3 (c + d x) \left(A + B \operatorname{Log}\left[\frac{e (c+d x)^2}{(a+b x)^2}\right] \right)}{d^4} + \frac{g^3 (a + b x)^4 \left(A + B \operatorname{Log}\left[\frac{e (c+d x)^2}{(a+b x)^2}\right] \right)^2}{4 b} + \\ & \frac{B (b c - a d)^4 g^3 \left(A + B \operatorname{Log}\left[\frac{e (c+d x)^2}{(a+b x)^2}\right] \right) \operatorname{Log}\left[1 - \frac{d (a+b x)}{b (c+d x)}\right]}{b d^4} - \frac{2 B^2 (b c - a d)^4 g^3 \operatorname{PolyLog}\left[2, \frac{d (a+b x)}{b (c+d x)}\right]}{b d^4} \end{aligned}$$

Result (type 4, 2127 leaves):

$$\begin{aligned} g^3 \left(\right. & -\frac{6 a^4 B^2}{b} - \frac{2 b^3 B^2 c^4}{d^4} + \frac{10 a b^2 B^2 c^3}{d^3} - \frac{20 a^2 b B^2 c^2}{d^2} + \frac{18 a^3 B^2 c}{d} + a^3 A^2 x - 3 a^3 A B x + \\ & \frac{7}{3} a^3 B^2 x + \frac{A b^3 B c^3 x}{d^3} - \frac{5 b^3 B^2 c^3 x}{3 d^3} - \frac{4 a A b^2 B c^2 x}{d^2} + \frac{17 a b^2 B^2 c^2 x}{3 d^2} + \frac{6 a^2 A b B c x}{d} - \\ & \frac{19 a^2 b B^2 c x}{3 d} + \frac{3}{2} a^2 A^2 b x^2 - \frac{3}{2} a^2 A b B x^2 + \frac{1}{3} a^2 b B^2 x^2 - \frac{A b^3 B c^2 x^2}{2 d^2} + \frac{b^3 B^2 c^2 x^2}{3 d^2} + \\ & \frac{2 a A b^2 B c x^2}{d} - \frac{2 a b^2 B^2 c x^2}{3 d} + a A^2 b^2 x^3 - \frac{1}{3} a A b^2 B x^3 + \frac{A b^3 B c x^3}{3 d} + \frac{1}{4} A^2 b^3 x^4 + \\ & \frac{6 a^4 B^2 \operatorname{Log}\left[\frac{a}{b} + x\right]}{b} - \frac{2 a b^2 B^2 c^3 \operatorname{Log}\left[\frac{a}{b} + x\right]}{d^3} + \frac{8 a^2 b B^2 c^2 \operatorname{Log}\left[\frac{a}{b} + x\right]}{d^2} - \frac{12 a^3 B^2 c \operatorname{Log}\left[\frac{a}{b} + x\right]}{d} + \\ & \frac{a^4 B^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2}{b} + \frac{2 b^3 B^2 c^4 \operatorname{Log}\left[\frac{c}{d} + x\right]}{d^4} - \frac{8 a b^2 B^2 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]}{d^3} + \frac{12 a^2 b B^2 c^2 \operatorname{Log}\left[\frac{c}{d} + x\right]}{d^2} - \\ & \frac{6 a^3 B^2 c \operatorname{Log}\left[\frac{c}{d} + x\right]}{d} - \frac{b^3 B^2 c^4 \operatorname{Log}\left[\frac{c}{d} + x\right]^2}{d^4} + \frac{4 a b^2 B^2 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2}{d^3} - \frac{6 a^2 b B^2 c^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2}{d^2} + \\ & \frac{4 a^3 B^2 c \operatorname{Log}\left[\frac{c}{d} + x\right]^2}{d} - \frac{a^4 A B \operatorname{Log}[a + b x]}{b} - \frac{7 a^4 B^2 \operatorname{Log}[a + b x]}{3 b} - \frac{a^2 b B^2 c^2 \operatorname{Log}[a + b x]}{d^2} + \\ & \frac{10 a^3 B^2 c \operatorname{Log}[a + b x]}{3 d} - \frac{2 a^4 B^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x]}{b} + \frac{2 a^4 B^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x]}{b} - \\ & \frac{2 a^4 B^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a+b x)}{-b c + a d}\right]}{b} - \frac{A b^3 B c^4 \operatorname{Log}[c + d x]}{d^4} + \frac{5 b^3 B^2 c^4 \operatorname{Log}[c + d x]}{3 d^4} + \\ & \frac{4 a A b^2 B c^3 \operatorname{Log}[c + d x]}{d^3} - \frac{14 a b^2 B^2 c^3 \operatorname{Log}[c + d x]}{3 d^3} - \frac{6 a^2 A b B c^2 \operatorname{Log}[c + d x]}{d^2} + \end{aligned}$$

$$\begin{aligned}
 & \frac{3 a^2 b B^2 c^2 \operatorname{Log}[c+d x]}{d^2} + \frac{4 a^3 A B c \operatorname{Log}[c+d x]}{d} - \frac{2 b^3 B^2 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]}{d^4} + \\
 & \frac{8 a b^2 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]}{d^3} - \frac{12 a^2 b B^2 c^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]}{d^2} + \\
 & \frac{8 a^3 B^2 c \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]}{d} + \frac{2 b^3 B^2 c^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]}{d^4} - \\
 & \frac{8 a b^2 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]}{d^3} + \frac{12 a^2 b B^2 c^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]}{d^2} - \\
 & \frac{8 a^3 B^2 c \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]}{d} + \frac{2 b^3 B^2 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^4} - \\
 & \frac{8 a b^2 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^3} + \frac{12 a^2 b B^2 c^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^2} - \\
 & \frac{8 a^3 B^2 c \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d} + 2 a^3 A B x \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] - \\
 & 3 a^3 B^2 x \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] + \frac{b^3 B^2 c^3 x \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]}{d^3} - \frac{4 a b^2 B^2 c^2 x \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]}{d^2} + \\
 & \frac{6 a^2 b B^2 c x \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]}{d} + 3 a^2 A b B x^2 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] - \frac{3}{2} a^2 b B^2 x^2 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] - \\
 & \frac{b^3 B^2 c^2 x^2 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]}{2 d^2} + \frac{2 a b^2 B^2 c x^2 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]}{d} + 2 a A b^2 B x^3 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] - \\
 & \frac{1}{3} a b^2 B^2 x^3 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] + \frac{b^3 B^2 c x^3 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]}{3 d} + \frac{1}{2} A b^3 B x^4 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] - \\
 & \frac{a^4 B^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]}{b} - \frac{b^3 B^2 c^4 \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]}{d^4} + \\
 & \frac{4 a b^2 B^2 c^3 \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]}{d^3} - \frac{6 a^2 b B^2 c^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]}{d^2} + \\
 & \frac{4 a^3 B^2 c \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]}{d} + a^3 B^2 x \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]^2 + \\
 & \frac{3}{2} a^2 b B^2 x^2 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]^2 + a b^2 B^2 x^3 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]^2 + \frac{1}{4} b^3 B^2 x^4 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]^2 + \\
 & \frac{2 B^2 c\left(b^3 c^3-4 a b^2 c^2 d+6 a^2 b c d^2-4 a^3 d^3\right) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]}{d^4} - \frac{2 a^4 B^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]}{b}
 \end{aligned}$$

Problem 212: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^2 \left(A + B \operatorname{Log} \left[\frac{e (c + d x)^2}{(a + b x)^2} \right] \right)^2 dx$$

Optimal (type 4, 343 leaves, 11 steps):

$$\begin{aligned} & \frac{4 B^2 (b c - a d)^2 g^2 x}{3 d^2} - \frac{4 B^2 (b c - a d)^3 g^2 \operatorname{Log}[a + b x]}{b d^3} - \\ & \frac{4 B^2 (b c - a d)^3 g^2 \operatorname{Log}\left[\frac{c+d x}{a+b x}\right]}{3 b d^3} + \frac{2 B (b c - a d) g^2 (a + b x)^2 \left(A + B \operatorname{Log}\left[\frac{e (c+d x)^2}{(a+b x)^2}\right] \right)}{3 b d} - \\ & \frac{4 B (b c - a d)^2 g^2 (c + d x) \left(A + B \operatorname{Log}\left[\frac{e (c+d x)^2}{(a+b x)^2}\right] \right)}{3 d^3} + \frac{g^2 (a + b x)^3 \left(A + B \operatorname{Log}\left[\frac{e (c+d x)^2}{(a+b x)^2}\right] \right)^2}{3 b} - \\ & \frac{4 B (b c - a d)^3 g^2 \left(A + B \operatorname{Log}\left[\frac{e (c+d x)^2}{(a+b x)^2}\right] \right) \operatorname{Log}\left[1 - \frac{d (a+b x)}{b (c+d x)}\right]}{3 b d^3} + \frac{8 B^2 (b c - a d)^3 g^2 \operatorname{PolyLog}\left[2, \frac{d (a+b x)}{b (c+d x)}\right]}{3 b d^3} \end{aligned}$$

Result (type 4, 1458 leaves):

$$\begin{aligned} & g^2 \left(a^2 A^2 x + a A^2 b x^2 + \frac{1}{3} A^2 b^2 x^3 + 2 a^2 A B \right. \\ & \left. \left(\frac{2 (-b c + a d) (a d \operatorname{Log}[a + b x] - b c \operatorname{Log}[c + d x])}{b^2 c d - a b d^2} + x \operatorname{Log}\left[\frac{c^2 e + 2 c d e x + d^2 e x^2}{(a + b x)^2}\right] \right) + 4 a A b B \right. \\ & \left. \left(-(-b c + a d) \left(\frac{x}{b d} + \frac{a^2 \operatorname{Log}[a + b x]}{b^2 (b c - a d)} - \frac{c^2 \operatorname{Log}[c + d x]}{d^2 (b c - a d)} \right) + \frac{1}{2} x^2 \operatorname{Log}\left[\frac{c^2 e + 2 c d e x + d^2 e x^2}{(a + b x)^2}\right] \right) + \right. \\ & \left. 2 A b^2 B \left(- \left((-b c + a d) (b d (b c - a d) x (-2 b c - 2 a d + b d x) - 2 a^3 d^3 \operatorname{Log}[a + b x] + \right. \right. \right. \\ & \left. \left. \left. 2 b^3 c^3 \operatorname{Log}[c + d x] \right) \right) / (3 b^3 d^3 (b c - a d)) \right) + \frac{1}{3} x^3 \operatorname{Log}\left[\frac{c^2 e + 2 c d e x + d^2 e x^2}{(a + b x)^2}\right] \right) + \\ & a^2 B^2 \left(x \operatorname{Log}\left[\frac{c^2 e + 2 c d e x + d^2 e x^2}{(a + b x)^2}\right]^2 + \frac{1}{b d} 4 \left(a d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + b c \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - \right. \right. \\ & \left. \left. 2 a d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 2 a d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 2 a d \operatorname{Log}\left[\frac{c}{d} + x\right] \right. \right. \\ & \left. \left. \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + 2 b c \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - 2 b c \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - \right. \right. \\ & \left. \left. 2 b c \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] - a d \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e (c + d x)^2}{(a + b x)^2}\right] + b c \operatorname{Log}[c + d x] \right. \right. \\ & \left. \left. \operatorname{Log}\left[\frac{e (c + d x)^2}{(a + b x)^2}\right] - 2 b c \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] - 2 a d \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) + \\ & 2 a b B^2 \left(\frac{1}{2} x^2 \operatorname{Log}\left[\frac{c^2 e + 2 c d e x + d^2 e x^2}{(a + b x)^2}\right]^2 + \frac{1}{b^2 d^2} 2 \left(2 d (-b c + a d) (a + b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) - \right. \right. \end{aligned}$$

$$\begin{aligned}
 & a^2 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2+2 b(b c-a d)(c+d x)\left(-1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)- \\
 & b^2 c^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2+\left(a^2 d^2 \operatorname{Log}[a+b x]-b(d(-b c+a d) x+b c^2 \operatorname{Log}[c+d x])\right) \\
 & \left(2 \operatorname{Log}\left[\frac{a}{b}+x\right]-2 \operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]\right)+ \\
 & 2 b^2 c^2\left(\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+\operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)+ \\
 & 2 a^2 d^2\left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+\operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right)\left.\right)\left.\right)+ \\
 & b^2 B^2\left(\frac{1}{3} x^3 \operatorname{Log}\left[\frac{c^2 e+2 c d e x+d^2 e x^2}{(a+b x)^2}\right]^2+\frac{1}{3 b^3 d^3}\right. \\
 & 2\left(-4 d(-b c+a d)(b c+a d)(a+b x)\left(-1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)+2 a^3 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2- \right. \\
 & 4 b(b c-a d)(b c+a d)(c+d x)\left(-1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)+2 b^3 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2+ \\
 & d^2(-b c+a d)\left(b x(2 a-b x)+2 b^2 x^2 \operatorname{Log}\left[\frac{a}{b}+x\right]-2 a^2 \operatorname{Log}[a+b x]\right)+ \\
 & b^2(b c-a d)\left(d x(2 c-d x)+2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d}+x\right]-2 c^2 \operatorname{Log}[c+d x]\right)+ \\
 & (b d(b c-a d) x(-2 b c-2 a d+b d x)-2 a^3 d^3 \operatorname{Log}[a+b x]+2 b^3 c^3 \operatorname{Log}[c+d x]) \\
 & \left.\left(2 \operatorname{Log}\left[\frac{a}{b}+x\right]-2 \operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]\right)- \right. \\
 & 4 b^3 c^3\left(\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+\operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)- \\
 & \left.\left.4 a^3 d^3\left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+\operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right)\right)\right)\left.\right)\left.\right)
 \end{aligned}$$

Problem 213: Result more than twice size of optimal antiderivative.

$$\int(a g+b g x)\left(A+B \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]\right)^2 d x$$

Optimal (type 4, 211 leaves, 7 steps):

$$\begin{aligned}
 & \frac{4 B^2(b c-a d)^2 g \operatorname{Log}[a+b x]}{b d^2}+ \\
 & \frac{2 B(b c-a d) g(c+d x)\left(A+B \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]\right)}{d^2}+\frac{g(a+b x)^2\left(A+B \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]\right)^2}{2 b}+ \\
 & \frac{2 B(b c-a d)^2 g\left(A+B \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]\right) \operatorname{Log}\left[1-\frac{d(a+b x)}{b(c+d x)}\right]}{b d^2}-\frac{4 B^2(b c-a d)^2 g \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{b d^2}
 \end{aligned}$$

Result (type 4, 754 leaves):

$$\begin{aligned}
 & g \left(a A^2 x + \frac{1}{2} A^2 b x^2 + \frac{2 a A B (-2 a d \operatorname{Log}[a+b x] + 2 b c \operatorname{Log}[c+d x] + b d x \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right])}{b d} \right) + \\
 & A B \left(\frac{2 a^2 \operatorname{Log}[a+b x]}{b} + \frac{-2 b c^2 \operatorname{Log}[c+d x] + d x (2 b c - 2 a d + b d x \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right])}{d^2} \right) + \\
 & \frac{1}{b d} a B^2 \left(4 a d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 4 b c \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 8 a d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a+b x] + \right. \\
 & 8 a d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a+b x] - 8 a d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + 8 b c \operatorname{Log}\left[\frac{a}{b} + x\right] \\
 & \operatorname{Log}[c+d x] - 8 b c \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c+d x] - 8 b c \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] - \\
 & 4 a d \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] + 4 b c \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] + \\
 & \left. b d x \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]^2 - 8 b c \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] - 8 a d \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] \right) + \\
 & b B^2 \left(\frac{1}{2} x^2 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]^2 + \frac{1}{b^2 d^2} 2 \left(2 d (-b c + a d) (a+b x) (-1 + \operatorname{Log}\left[\frac{a}{b} + x\right]) - \right. \right. \\
 & a^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 b (b c - a d) (c+d x) (-1 + \operatorname{Log}\left[\frac{c}{d} + x\right]) - \\
 & \left. b^2 c^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + (a^2 d^2 \operatorname{Log}[a+b x] - b (d (-b c + a d) x + b c^2 \operatorname{Log}[c+d x])) \right) \\
 & \left(2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] \right) + \\
 & 2 b^2 c^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] \right) + \\
 & \left. 2 a^2 d^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] \right) \right)
 \end{aligned}$$

Problem 214: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] \right)^2}{a g + b g x} dx$$

Optimal (type 4, 132 leaves, 4 steps):

$$\frac{\text{Log}\left[-\frac{bc-ad}{d(a+bx)}\right] \left(A + B \text{Log}\left[\frac{e(c+dx)^2}{(a+bx)^2}\right]\right)^2}{bg} - \frac{4B \left(A + B \text{Log}\left[\frac{e(c+dx)^2}{(a+bx)^2}\right]\right) \text{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right]}{bg} + \frac{8B^2 \text{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right]}{bg}$$

Result (type 4, 624 leaves):

$$\frac{A^2 \text{Log}[a+bx]}{bg} + \frac{1}{g} 2AB \left(-\frac{\text{Log}\left[\frac{a}{b} + x\right]^2}{b} + \frac{1}{b} \right. \\ \left. \text{Log}[a+bx] \left(2 \text{Log}\left[\frac{a}{b} + x\right] - 2 \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{c^2 e}{(a+bx)^2} + \frac{2cdex}{(a+bx)^2} + \frac{d^2 ex^2}{(a+bx)^2}\right] \right) + \right. \\ \left. \frac{2 \left(\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[1 - \frac{b\left(\frac{c}{d} + x\right)}{-a + \frac{bc}{d}}\right] + \text{PolyLog}\left[2, \frac{b\left(\frac{c}{d} + x\right)}{-a + \frac{bc}{d}}\right] \right)}{b} \right) + \frac{1}{g} B^2 \left(\frac{4 \text{Log}\left[\frac{a}{b} + x\right]^3}{3b} + \frac{1}{b} \right. \\ \left. \text{Log}[a+bx] \left(2 \text{Log}\left[\frac{a}{b} + x\right] - 2 \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{c^2 e}{(a+bx)^2} + \frac{2cdex}{(a+bx)^2} + \frac{d^2 ex^2}{(a+bx)^2}\right] \right)^2 + \right. \\ \left. 2 \left(2 \text{Log}\left[\frac{a}{b} + x\right] - 2 \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{c^2 e}{(a+bx)^2} + \frac{2cdex}{(a+bx)^2} + \frac{d^2 ex^2}{(a+bx)^2}\right] \right) \right. \\ \left. \left(-\frac{\text{Log}\left[\frac{a}{b} + x\right]^2}{b} + \frac{2 \left(\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[1 - \frac{b\left(\frac{c}{d} + x\right)}{-a + \frac{bc}{d}}\right] + \text{PolyLog}\left[2, \frac{b\left(\frac{c}{d} + x\right)}{-a + \frac{bc}{d}}\right] \right)}{b} \right) + \right. \\ \left. \frac{1}{b} 8 \left(\frac{1}{2} \text{Log}\left[\frac{c}{d} + x\right]^2 \text{Log}\left[1 - \frac{b\left(\frac{c}{d} + x\right)}{-a + \frac{bc}{d}}\right] + \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b\left(\frac{c}{d} + x\right)}{-a + \frac{bc}{d}}\right] - \right. \right. \\ \left. \left. \text{PolyLog}\left[3, \frac{b\left(\frac{c}{d} + x\right)}{-a + \frac{bc}{d}}\right] \right) - \frac{1}{b} 8 \left(\frac{1}{2} \text{Log}\left[\frac{a}{b} + x\right]^2 \left(\text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{bd\left(\frac{c}{d} + x\right)}{bc-ad}\right] \right) - \right. \\ \left. \left. \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, -\frac{d(a+bx)}{bc-ad}\right] + \text{PolyLog}\left[3, -\frac{d(a+bx)}{bc-ad}\right] \right) \right)$$

Problem 222: Unable to integrate problem.

$$\int \frac{1}{(a g + b g x)^2 \left(A + B \operatorname{Log} \left[\frac{e (c+d x)^2}{(a+b x)^2} \right] \right)} dx$$

Optimal (type 4, 91 leaves, 3 steps):

$$\frac{e^{-\frac{A}{2B}} (c+d x) \operatorname{ExpIntegralEi} \left[\frac{A+B \operatorname{Log} \left[\frac{e (c+d x)^2}{(a+b x)^2} \right]}{2B} \right]}{2B (b c - a d) g^2 (a+b x) \sqrt{\frac{e (c+d x)^2}{(a+b x)^2}}}$$

Result (type 8, 36 leaves):

$$\int \frac{1}{(a g + b g x)^2 \left(A + B \operatorname{Log} \left[\frac{e (c+d x)^2}{(a+b x)^2} \right] \right)} dx$$

Problem 223: Unable to integrate problem.

$$\int \frac{1}{(a g + b g x)^3 \left(A + B \operatorname{Log} \left[\frac{e (c+d x)^2}{(a+b x)^2} \right] \right)} dx$$

Optimal (type 4, 151 leaves, 7 steps):

$$\frac{d e^{-\frac{A}{2B}} (c+d x) \operatorname{ExpIntegralEi} \left[\frac{A+B \operatorname{Log} \left[\frac{e (c+d x)^2}{(a+b x)^2} \right]}{2B} \right]}{2B (b c - a d)^2 g^3 (a+b x) \sqrt{\frac{e (c+d x)^2}{(a+b x)^2}}} - \frac{b e^{-\frac{A}{B}} \operatorname{ExpIntegralEi} \left[\frac{A+B \operatorname{Log} \left[\frac{e (c+d x)^2}{(a+b x)^2} \right]}{B} \right]}{2B (b c - a d)^2 e g^3}$$

Result (type 8, 36 leaves):

$$\int \frac{1}{(a g + b g x)^3 \left(A + B \operatorname{Log} \left[\frac{e (c+d x)^2}{(a+b x)^2} \right] \right)} dx$$

Problem 227: Unable to integrate problem.

$$\int \frac{1}{(a g + b g x)^2 \left(A + B \operatorname{Log} \left[\frac{e (c+d x)^2}{(a+b x)^2} \right] \right)^2} dx$$

Optimal (type 4, 147 leaves, 4 steps):

$$\frac{e^{-\frac{A}{2B}} (c+d x) \operatorname{ExpIntegralEi} \left[\frac{A+B \operatorname{Log} \left[\frac{e (c+d x)^2}{(a+b x)^2} \right]}{2B} \right]}{4B^2 (b c - a d) g^2 (a+b x) \sqrt{\frac{e (c+d x)^2}{(a+b x)^2}}} + \frac{c+d x}{2B (b c - a d) g^2 (a+b x) \left(A + B \operatorname{Log} \left[\frac{e (c+d x)^2}{(a+b x)^2} \right] \right)}$$

Result (type 8, 36 leaves):

$$\int \frac{1}{(a g + b g x)^2 \left(A + B \text{Log} \left[\frac{e (c+d x)^2}{(a+b x)^2} \right] \right)^2} dx$$

Problem 228: Unable to integrate problem.

$$\int \frac{1}{(a g + b g x)^3 \left(A + B \text{Log} \left[\frac{e (c+d x)^2}{(a+b x)^2} \right] \right)^2} dx$$

Optimal (type 4, 206 leaves, 10 steps):

$$\frac{d e^{-\frac{A}{2B}} (c+d x) \text{ExpIntegralEi} \left[\frac{A+B \text{Log} \left[\frac{e (c+d x)^2}{(a+b x)^2} \right]}{2B} \right]}{4 B^2 (b c - a d)^2 g^3 (a+b x) \sqrt{\frac{e (c+d x)^2}{(a+b x)^2}}} - \frac{b e^{-\frac{A}{B}} \text{ExpIntegralEi} \left[\frac{A+B \text{Log} \left[\frac{e (c+d x)^2}{(a+b x)^2} \right]}{B} \right]}{2 B^2 (b c - a d)^2 e g^3} + \frac{c+d x}{2 B (b c - a d) g^3 (a+b x)^2 \left(A + B \text{Log} \left[\frac{e (c+d x)^2}{(a+b x)^2} \right] \right)}$$

Result (type 8, 36 leaves):

$$\int \frac{1}{(a g + b g x)^3 \left(A + B \text{Log} \left[\frac{e (c+d x)^2}{(a+b x)^2} \right] \right)^2} dx$$

Problem 229: Unable to integrate problem.

$$\int \frac{1}{(a g + b g x)^2 \left(A + B \text{Log} \left[e (a+b x)^n (c+d x)^{-n} \right] \right)} dx$$

Optimal (type 4, 96 leaves, 4 steps):

$$\left(e^{\frac{A}{Bn}} (c+d x) \left(e (a+b x)^n (c+d x)^{-n} \right)^{\frac{1}{n}} \text{ExpIntegralEi} \left[-\frac{A+B \text{Log} \left[e (a+b x)^n (c+d x)^{-n} \right]}{B n} \right] \right) / (B (b c - a d) g^2 n (a+b x))$$

Result (type 8, 38 leaves):

$$\int \frac{1}{(a g + b g x)^2 \left(A + B \text{Log} \left[e (a+b x)^n (c+d x)^{-n} \right] \right)} dx$$

Problem 240: Result more than twice size of optimal antiderivative.

$$\int (f + g x)^3 \left(A + B \text{Log} \left[\frac{e (a+b x)}{c+d x} \right] \right)^2 dx$$

Optimal (type 4, 874 leaves, 15 steps):

$$\begin{aligned}
 & \frac{B^2 (b c - a d)^3 g^3 x}{6 b^3 d^3} + \frac{B^2 (b c - a d)^2 g^2 (4 b d f - 3 b c g - a d g) x}{4 b^3 d^3} + \frac{B^2 (b c - a d)^2 g^3 (c + d x)^2}{12 b^2 d^4} + \\
 & \frac{B^2 (b c - a d)^4 g^3 \text{Log}\left[\frac{a+b x}{c+d x}\right]}{6 b^4 d^4} + \frac{B^2 (b c - a d)^3 g^2 (4 b d f - 3 b c g - a d g) \text{Log}\left[\frac{a+b x}{c+d x}\right]}{4 b^4 d^4} - \frac{1}{2 b^4 d^3} \\
 & B (b c - a d) g (a^2 d^2 g^2 - 2 a b d g (2 d f - c g) + b^2 (6 d^2 f^2 - 8 c d f g + 3 c^2 g^2)) (a + b x) \\
 & \left(A + B \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) - \frac{B (b c - a d) g^2 (4 b d f - 3 b c g - a d g) (c + d x)^2 \left(A + B \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)}{4 b^2 d^4} - \\
 & \frac{B (b c - a d) g^3 (c + d x)^3 \left(A + B \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)}{6 b d^4} - \frac{1}{2 b^4 d^4} B (b c - a d) (2 b d f - b c g - a d g) \\
 & (2 a b d^2 f g - a^2 d^2 g^2 - b^2 (2 d^2 f^2 - 2 c d f g + c^2 g^2)) \text{Log}\left[\frac{b c - a d}{b (c + d x)}\right] \left(A + B \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) - \\
 & \frac{(b f - a g)^4 \left(A + B \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)^2}{4 b^4 g} + \frac{(f + g x)^4 \left(A + B \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)^2}{4 g} + \\
 & \frac{B^2 (b c - a d)^4 g^3 \text{Log}[c + d x]}{6 b^4 d^4} + \frac{B^2 (b c - a d)^3 g^2 (4 b d f - 3 b c g - a d g) \text{Log}[c + d x]}{4 b^4 d^4} + \frac{1}{2 b^4 d^4} \\
 & B^2 (b c - a d)^2 g (a^2 d^2 g^2 - 2 a b d g (2 d f - c g) + b^2 (6 d^2 f^2 - 8 c d f g + 3 c^2 g^2)) \text{Log}[c + d x] - \\
 & \frac{1}{2 b^4 d^4} B^2 (b c - a d) (2 b d f - b c g - a d g) \\
 & (2 a b d^2 f g - a^2 d^2 g^2 - b^2 (2 d^2 f^2 - 2 c d f g + c^2 g^2)) \text{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]
 \end{aligned}$$

Result (type 4, 2229 leaves):

$$\begin{aligned}
 & A^2 f^3 x + \frac{3}{2} A^2 f^2 g x^2 + A^2 f g^2 x^3 + \frac{1}{4} A^2 g^3 x^4 + \\
 & \frac{2 A B f^3 \left(a d \text{Log}[a + b x] + b d x \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] - b c \text{Log}[c + d x] \right)}{b d} + \\
 & \frac{1}{12} A B g^3 \left(\frac{6 a^3 x}{b^3} - \frac{6 c^3 x}{d^3} - \frac{3 a^2 x^2}{b^2} + \frac{3 c^2 x^2}{d^2} + \frac{2 a x^3}{b} - \right. \\
 & \left. \frac{2 c x^3}{d} - \frac{6 a^4 \text{Log}[a + b x]}{b^4} + 6 x^4 \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] + \frac{6 c^4 \text{Log}[c + d x]}{d^4} \right) + \\
 & A B f g^2 \left(\frac{(b c - a d) x (2 b c + 2 a d - b d x)}{b^2 d^2} + \frac{2 a^3 \text{Log}[a + b x]}{b^3} + \right. \\
 & \left. 2 x^3 \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] - \frac{2 c^3 \text{Log}[c + d x]}{d^3} \right) + \frac{1}{b^2 d^2} \\
 & 3 A B f^2 g \left(-a^2 d^2 \text{Log}[a + b x] + b \left(d (-b c + a d) x + b d^2 x^2 \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] + b c^2 \text{Log}[c + d x] \right) \right) + \\
 & \frac{1}{b d} B^2 f^3 \left(a d \text{Log}\left[\frac{a}{b} + x\right]^2 + b c \text{Log}\left[\frac{c}{d} + x\right]^2 - 2 a d \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 a d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x]-2 a d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+ \\
 & 2 a d \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+b d x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2+2 b c \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]- \\
 & 2 b c \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]-2 b c \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]-2 b c \operatorname{Log}\left[\frac{a}{b}+x\right] \\
 & \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]-2 b c \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]-2 a d \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]+ \\
 & \frac{1}{12} B^2 g^3\left(3 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2+\frac{1}{b^4 d^4}\left(-6 b^4 c^4+6 a b^3 c^3 d+6 a^3 b c d^3-6 a^4 d^4-5 b^4 c^3 d x+\right.\right. \\
 & 5 a b^3 c^2 d^2 x+5 a^2 b^2 c d^3 x-5 a^3 b d^4 x+b^4 c^2 d^2 x^2-2 a b^3 c d^3 x^2+a^2 b^2 d^4 x^2- \\
 & 6 a b^3 c^3 d \operatorname{Log}\left[\frac{a}{b}+x\right]+6 a^4 d^4 \operatorname{Log}\left[\frac{a}{b}+x\right]-3 a^4 d^4 \operatorname{Log}\left[\frac{a}{b}+x\right]^2+6 b^4 c^4 \operatorname{Log}\left[\frac{c}{d}+x\right]- \\
 & 6 a^3 b c d^3 \operatorname{Log}\left[\frac{c}{d}+x\right]-3 b^4 c^4 \operatorname{Log}\left[\frac{c}{d}+x\right]^2-3 a^2 b^2 c^2 d^2 \operatorname{Log}[a+b x]-2 a^3 b c d^3 \operatorname{Log}[a+b x]+ \\
 & 5 a^4 d^4 \operatorname{Log}[a+b x]+6 a^4 d^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x]-6 a^4 d^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x]+6 a^4 d^4 \\
 & \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]-6 b^4 c^3 d x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+6 a^3 b d^4 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & 3 b^4 c^2 d^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-3 a^2 b^2 d^4 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-2 b^4 c d^3 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & 2 a b^3 d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-6 a^4 d^4 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+5 b^4 c^4 \operatorname{Log}[c+d x]- \\
 & 2 a b^3 c^3 d \operatorname{Log}[c+d x]-3 a^2 b^2 c^2 d^2 \operatorname{Log}[c+d x]-6 b^4 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]+ \\
 & 6 b^4 c^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]+6 b^4 c^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]+6 b^4 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \\
 & \left.\left.\operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+6 b^4 c^4 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]+6 a^4 d^4 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right)\right)+ \\
 & \frac{3}{2} B^2 f^2 g\left(x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2-\frac{1}{b^2 d^2}\left(-2 d(-b c+a d)(a+b x)\left(-1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)+\right.\right. \\
 & a^2 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2-2 b(b c-a d)(c+d x)\left(-1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)+ \\
 & b^2 c^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2-2\left(\operatorname{Log}\left[\frac{a}{b}+x\right]-\operatorname{Log}\left[\frac{c}{d}+x\right]-\operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right) \\
 & \left.\left.\left(a^2 d^2 \operatorname{Log}[a+b x]-b(d(-b c+a d)x+b c^2 \operatorname{Log}[c+d x])\right)\right)-\right. \\
 & 2 b^2 c^2\left(\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+\operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)- \\
 & \left.\left.2 a^2 d^2\left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+\operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right)\right)\right)+ \\
 & 3 B^2 f g^2\left(\frac{1}{3} x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2-\frac{1}{6 b^3 d^3}\left(4 d(-b c+a d)(b c+a d)(a+b x)\left(-1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)-\right.\right. \\
 & \left.\left.2 a^3 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2+4 b(b c-a d)(b c+a d)(c+d x)\left(-1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)\right)-\right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 b^3 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2+d^2(b c-a d)\left(b x(2 a-b x)+2 b^2 x^2 \operatorname{Log}\left[\frac{a}{b}+x\right]-2 a^2 \operatorname{Log}[a+b x]\right)+ \\
 & b^2(b c-a d)\left(d x(-2 c+d x)-2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d}+x\right]+2 c^2 \operatorname{Log}[c+d x]\right)- \\
 & 2\left(\operatorname{Log}\left[\frac{a}{b}+x\right]-\operatorname{Log}\left[\frac{c}{d}+x\right]-\operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right) \\
 & (b d(b c-a d) x(-2 b c-2 a d+b d x)-2 a^3 d^3 \operatorname{Log}[a+b x]+2 b^3 c^3 \operatorname{Log}[c+d x])+ \\
 & 4 b^3 c^3\left(\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+\operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)+ \\
 & 4 a^3 d^3\left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+\operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right)
 \end{aligned}$$

Problem 241: Result more than twice size of optimal antiderivative.

$$\int(f+g x)^2\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2 d x$$

Optimal (type 4, 532 leaves, 12 steps):

$$\begin{aligned}
 & \frac{B^2(b c-a d)^2 g^2 x}{3 b^2 d^2}+\frac{B^2(b c-a d)^3 g^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]}{3 b^3 d^3}- \\
 & \frac{2 B(b c-a d) g(3 b d f-2 b c g-a d g)(a+b x)\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{3 b^3 d^2}- \\
 & \frac{B(b c-a d) g^2(c+d x)^2\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{3 b d^3}+\frac{1}{3 b^3 d^3} \\
 & 2 B(b c-a d)\left(a^2 d^2 g^2-a b d g(3 d f-c g)+b^2\left(3 d^2 f^2-3 c d f g+c^2 g^2\right)\right) \operatorname{Log}\left[\frac{b c-a d}{b(c+d x)}\right] \\
 & \left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)-\frac{(b f-a g)^3\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{3 b^3 g}+\frac{(f+g x)^3\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{3 g} \\
 & \frac{B^2(b c-a d)^3 g^2 \operatorname{Log}[c+d x]}{3 b^3 d^3}+\frac{2 B^2(b c-a d)^2 g(3 b d f-2 b c g-a d g) \operatorname{Log}[c+d x]}{3 b^3 d^3}+\frac{1}{3 b^3 d^3} \\
 & 2 B^2(b c-a d)\left(a^2 d^2 g^2-a b d g(3 d f-c g)+b^2\left(3 d^2 f^2-3 c d f g+c^2 g^2\right)\right) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]
 \end{aligned}$$

Result (type 4, 1294 leaves):

$$\begin{aligned}
 & A^2 f^2 x+A^2 f g x^2+\frac{1}{3} A^2 g^2 x^3+ \\
 & \frac{2 A B f^2\left(a d \operatorname{Log}[a+b x]+b d x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-b c \operatorname{Log}[c+d x]\right)}{b d}+\frac{1}{3} A B g^2 \\
 & \left(\frac{(b c-a d) x(2 b c+2 a d-b d x)}{b^2 d^2}+\frac{2 a^3 \operatorname{Log}[a+b x]}{b^3}+2 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-\frac{2 c^3 \operatorname{Log}[c+d x]}{d^3}\right)+
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{b^2 d^2} 2 A B f g \left(-a^2 d^2 \text{Log}[a+b x] + b \left(d(-b c+a d) x + b d^2 x^2 \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] + b c^2 \text{Log}[c+d x] \right) \right) + \\
 & \frac{1}{b d} B^2 f^2 \left(a d \text{Log}\left[\frac{a}{b}+x\right]^2 + b c \text{Log}\left[\frac{c}{d}+x\right]^2 - 2 a d \text{Log}\left[\frac{a}{b}+x\right] \text{Log}[a+b x] + 2 a d \text{Log}\left[\frac{c}{d}+x\right] \right. \\
 & \quad \text{Log}[a+b x] - 2 a d \text{Log}\left[\frac{c}{d}+x\right] \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + 2 a d \text{Log}[a+b x] \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & \quad b d x \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 2 b c \text{Log}\left[\frac{a}{b}+x\right] \text{Log}[c+d x] - 2 b c \text{Log}\left[\frac{c}{d}+x\right] \text{Log}[c+d x] - \\
 & \quad 2 b c \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] \text{Log}[c+d x] - 2 b c \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
 & \quad \left. 2 b c \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] - 2 a d \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) + B^2 f g \\
 & \left(x^2 \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 - \frac{1}{b^2 d^2} \left(-2 d(-b c+a d)(a+b x) \left(-1 + \text{Log}\left[\frac{a}{b}+x\right] \right) + a^2 d^2 \text{Log}\left[\frac{a}{b}+x\right]^2 - \right. \right. \\
 & \quad \left. \left. 2 b(b c-a d)(c+d x) \left(-1 + \text{Log}\left[\frac{c}{d}+x\right] \right) + b^2 c^2 \text{Log}\left[\frac{c}{d}+x\right]^2 - 2 \left(\text{Log}\left[\frac{a}{b}+x\right] - \text{Log}\left[\frac{c}{d}+x\right] - \right. \right. \right. \\
 & \quad \left. \left. \left. \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right) \right) \left(a^2 d^2 \text{Log}[a+b x] - b(d(-b c+a d) x + b c^2 \text{Log}[c+d x]) \right) - \right. \\
 & \quad \left. 2 b^2 c^2 \left(\text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) - \right. \\
 & \quad \left. \left. 2 a^2 d^2 \left(\text{Log}\left[\frac{c}{d}+x\right] \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) \right) \right) + \\
 & B^2 g^2 \left(\frac{1}{3} x^3 \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 - \frac{1}{6 b^3 d^3} \left(4 d(-b c+a d)(b c+a d)(a+b x) \left(-1 + \text{Log}\left[\frac{a}{b}+x\right] \right) - \right. \right. \\
 & \quad \left. \left. 2 a^3 d^3 \text{Log}\left[\frac{a}{b}+x\right]^2 + 4 b(b c-a d)(b c+a d)(c+d x) \left(-1 + \text{Log}\left[\frac{c}{d}+x\right] \right) - \right. \right. \\
 & \quad \left. \left. 2 b^3 c^3 \text{Log}\left[\frac{c}{d}+x\right]^2 + d^2(b c-a d) \left(b x(2 a-b x) + 2 b^2 x^2 \text{Log}\left[\frac{a}{b}+x\right] - 2 a^2 \text{Log}[a+b x] \right) + \right. \right. \\
 & \quad \left. \left. b^2(b c-a d) \left(d x(-2 c+d x) - 2 d^2 x^2 \text{Log}\left[\frac{c}{d}+x\right] + 2 c^2 \text{Log}[c+d x] \right) - \right. \right. \\
 & \quad \left. \left. 2 \left(\text{Log}\left[\frac{a}{b}+x\right] - \text{Log}\left[\frac{c}{d}+x\right] - \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right) \right) \right. \\
 & \quad \left. (b d(b c-a d) x(-2 b c-2 a d+b d x) - 2 a^3 d^3 \text{Log}[a+b x] + 2 b^3 c^3 \text{Log}[c+d x]) + \right. \\
 & \quad \left. 4 b^3 c^3 \left(\text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) + \right. \\
 & \quad \left. \left. 4 a^3 d^3 \left(\text{Log}\left[\frac{c}{d}+x\right] \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) \right) \right)
 \end{aligned}$$

Problem 242: Result more than twice size of optimal antiderivative.

$$\int (f+g x) \left(A+B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)^2 dx$$

Optimal (type 4, 270 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{B (b c - a d) g (a + b x) \left(A + B \operatorname{Log} \left[\frac{e (a+b x)}{c+d x} \right] \right)}{b^2 d} + \\
 & \frac{B (b c - a d) (2 b d f - b c g - a d g) \operatorname{Log} \left[\frac{b c - a d}{b (c+d x)} \right] \left(A + B \operatorname{Log} \left[\frac{e (a+b x)}{c+d x} \right] \right)}{b^2 d^2} - \\
 & \frac{(b f - a g)^2 \left(A + B \operatorname{Log} \left[\frac{e (a+b x)}{c+d x} \right] \right)^2}{2 b^2 g} + \frac{(f + g x)^2 \left(A + B \operatorname{Log} \left[\frac{e (a+b x)}{c+d x} \right] \right)^2}{2 g} + \\
 & \frac{B^2 (b c - a d)^2 g \operatorname{Log} [c + d x]}{b^2 d^2} + \frac{B^2 (b c - a d) (2 b d f - b c g - a d g) \operatorname{PolyLog} \left[2, \frac{d (a+b x)}{b (c+d x)} \right]}{b^2 d^2}
 \end{aligned}$$

Result (type 4, 745 leaves):

$$\begin{aligned}
 & \frac{1}{2 b^2 d^2} \\
 & \left(2 A^2 b^2 d^2 f x + A^2 b^2 d^2 g x^2 + 4 A b B d f \left(a d \operatorname{Log} [a + b x] + b d x \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] - b c \operatorname{Log} [c + d x] \right) - \right. \\
 & \left. 2 A B g \left(a^2 d^2 \operatorname{Log} [a + b x] - b \left(d (-b c + a d) x + b d^2 x^2 \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] + b c^2 \operatorname{Log} [c + d x] \right) \right) + \right. \\
 & \left. 2 b B^2 d f \left(a d \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + b c \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 2 a d \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + b x] + \right. \right. \\
 & \left. \left. 2 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + b x] - 2 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \right. \right. \\
 & \left. \left. 2 a d \operatorname{Log} [a + b x] \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] + b d x \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right]^2 + 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [c + d x] - \right. \right. \\
 & \left. \left. 2 b c \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [c + d x] - 2 b c \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \operatorname{Log} [c + d x] - 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \right. \right. \\
 & \left. \left. \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] - 2 b c \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] - 2 a d \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) + \\
 & B^2 g \left(2 d (-b c + a d) (a + b x) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) - a^2 d^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + \right. \\
 & \left. 2 b (b c - a d) (c + d x) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) - b^2 c^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + \right. \\
 & \left. b^2 d^2 x^2 \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right]^2 + 2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right) \right. \\
 & \left. \left(a^2 d^2 \operatorname{Log} [a + b x] - b \left(d (-b c + a d) x + b c^2 \operatorname{Log} [c + d x] \right) \right) + \right. \\
 & \left. 2 b^2 c^2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) + \right. \\
 & \left. 2 a^2 d^2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right)
 \end{aligned}$$

Problem 243: Result more than twice size of optimal antiderivative.

$$\int \left(A + B \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \right)^2 dx$$

Optimal (type 4, 125 leaves, 6 steps):

$$\frac{2 B (b c - a d) \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right] \left(A + B \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \right)}{b d} + \frac{(a+bx) \left(A + B \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \right)^2}{b} + \frac{2 B^2 (b c - a d) \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{b(c+dx)} \right]}{b d}$$

Result (type 4, 338 leaves):

$$\frac{1}{b d} \left(A^2 b d x + 2 A B \left(a d \operatorname{Log}[a+bx] + b d x \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] - b c \operatorname{Log}[c+dx] \right) + B^2 \left(a d \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + b c \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 2 a d \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log}[a+bx] + 2 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log}[a+bx] - 2 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(a+bx)}{-b c + a d} \right] + 2 a d \operatorname{Log}[a+bx] \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] + b d x \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right]^2 + 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log}[c+dx] - 2 b c \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log}[c+dx] - 2 b c \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \operatorname{Log}[c+dx] - 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(c+dx)}{b c - a d} \right] - 2 b c \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{-b c + a d} \right] - 2 a d \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{b c - a d} \right] \right)$$

Problem 244: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \right)^2}{f+g x} dx$$

Optimal (type 4, 277 leaves, 9 steps):

$$-\frac{\operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right] \left(A + B \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \right)^2}{g} + \frac{\left(A + B \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \right)^2 \operatorname{Log} \left[1 - \frac{(d f - c g)(a+bx)}{(b f - a g)(c+dx)} \right]}{g} - \frac{2 B \left(A + B \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \right) \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{b(c+dx)} \right]}{g} + \frac{2 B \left(A + B \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \right) \operatorname{PolyLog} \left[2, \frac{(d f - c g)(a+bx)}{(b f - a g)(c+dx)} \right]}{g} + \frac{2 B^2 \operatorname{PolyLog} \left[3, \frac{d(a+bx)}{b(c+dx)} \right]}{g} - \frac{2 B^2 \operatorname{PolyLog} \left[3, \frac{(d f - c g)(a+bx)}{(b f - a g)(c+dx)} \right]}{g}$$

Result (type 4, 1348 leaves):

$$\begin{aligned}
 & \frac{1}{g} \left(-B^2 \operatorname{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right]^2 + \right. \\
 & A^2 \operatorname{Log}[f+gx] - 2AB \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[f+gx] + B^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}[f+gx] + \\
 & 2AB \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[f+gx] - 2B^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[f+gx] + \\
 & B^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}[f+gx] + 2AB \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[f+gx] - \\
 & 2B^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[f+gx] + 2B^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[f+gx] + \\
 & B^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 \operatorname{Log}[f+gx] + 2AB \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - \\
 & B^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + 2B^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + \\
 & 2B^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right] \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - B^2 \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right]^2 \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + \\
 & 2B^2 \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right] \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - \\
 & B^2 \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right]^2 \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - 2AB \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] + \\
 & 2B^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] - B^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] - \\
 & 2B^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] - \\
 & 2B^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right] \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] + B^2 \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right]^2 \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] - \\
 & 2B^2 \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right] \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] + \\
 & B^2 \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right]^2 \operatorname{Log}\left[\frac{(-bc+ad)(f+gx)}{(df-cg)(a+bx)}\right] + \\
 & 2B \left(A+B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + B \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] \right) \operatorname{PolyLog}\left[2, \frac{g(a+bx)}{-bf+ag}\right] - \\
 & 2B \left(A+B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + B \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] \right) \operatorname{PolyLog}\left[2, \frac{g(c+dx)}{-df+cg}\right] - \\
 & 2B^2 \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right] + \\
 & 2B^2 \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] \operatorname{PolyLog}\left[2, \frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] + \\
 & 2B^2 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right] - 2B^2 \operatorname{PolyLog}\left[3, \frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] \Big)
 \end{aligned}$$

Problem 245: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{(f+gx)^2} dx$$

Optimal (type 4, 196 leaves, 4 steps):

$$\frac{(a+bx) \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{(bf-ag)(f+gx)} + \frac{2B(bc-ad) \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right) \operatorname{Log}\left[1 - \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)}\right]}{(bf-ag)(df-cg)} + \frac{2B^2(bc-ad) \operatorname{PolyLog}\left[2, \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)}\right]}{(bf-ag)(df-cg)}$$

Result (type 4, 3258 leaves):

$$\frac{1}{g(-bf+ag)(-df+cg)(f+gx)} \left(-A^2bd f^2 + A^2bc f g + aA^2df g - aA^2c g^2 + 2ABd f^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 2ABc f g \operatorname{Log}\left[\frac{a}{b} + x\right] + 2ABd f g x \operatorname{Log}\left[\frac{a}{b} + x\right] - 2ABc g^2 x \operatorname{Log}\left[\frac{a}{b} + x\right] - bB^2d f^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + bB^2c f g \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - bB^2d f g x \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + bB^2c g^2 x \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2ABd f^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 2aABd f g \operatorname{Log}\left[\frac{c}{d} + x\right] - 2ABd f g x \operatorname{Log}\left[\frac{c}{d} + x\right] + 2aABd g^2 x \operatorname{Log}\left[\frac{c}{d} + x\right] + 2bB^2d f^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] - 2aB^2d f g \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] + 2bB^2d f g x \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] - 2aB^2d g^2 x \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] - bB^2d f^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + aB^2d f g \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - bB^2d f g x \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + aB^2d g^2 x \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2ABd f^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 2ABc f g \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 2aABd f g \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 2aABc g^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 2bB^2d f^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 2bB^2c f g \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 2bB^2c g^2 x \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 2bB^2d f^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 2aB^2d f g \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 2bB^2d f g x \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 2aB^2d g^2 x \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - bB^2d f^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + bB^2c f g \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + aB^2d f g \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 - aB^2c g^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 -$$

$$\begin{aligned}
 & 2 b B^2 c f g \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right]+2 a B^2 d f g \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right]- \\
 & 2 b B^2 c g^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right]+2 a B^2 d g^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right]+ \\
 & b B^2 c f g \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right]^2-a B^2 d f g \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right]^2+b B^2 c g^2 x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right]^2- \\
 & a B^2 d g^2 x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right]^2-2 b B^2 c f g \operatorname{Log}\left[\frac{-b c+a d}{d(a+b x)}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]+ \\
 & 2 a B^2 d f g \operatorname{Log}\left[\frac{-b c+a d}{d(a+b x)}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]- \\
 & 2 b B^2 c g^2 x \operatorname{Log}\left[\frac{-b c+a d}{d(a+b x)}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]+ \\
 & 2 a B^2 d g^2 x \operatorname{Log}\left[\frac{-b c+a d}{d(a+b x)}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]- \\
 & 2 b B^2 c f g \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]+ \\
 & 2 a B^2 d f g \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]- \\
 & 2 b B^2 c g^2 x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]+ \\
 & 2 a B^2 d g^2 x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]+b B^2 c f g \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]^2- \\
 & a B^2 d f g \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]^2+b B^2 c g^2 x \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]^2- \\
 & a B^2 d g^2 x \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]^2-2 A b B d f^2 \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+ \\
 & 2 A b B c f g \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]-2 A b B d f g x \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+2 A b B c g^2 x \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+ \\
 & 2 b B^2 d f^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]-2 a B^2 d f g \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+ \\
 & 2 b B^2 d f g x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]-2 a B^2 d g^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]- \\
 & 2 b B^2 d f^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+2 b B^2 c f g \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]- \\
 & 2 b B^2 d f g x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+2 b B^2 c g^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]- \\
 & 2 b B^2 d f^2 \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+2 b B^2 c f g \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]-
 \end{aligned}$$

$$\begin{aligned}
 & 2 b B^2 d f g x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+2 b B^2 c g^2 x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+ \\
 & 2 A b B d f^2 \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]-2 a A B d f g \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+2 A b B d f g x \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]- \\
 & 2 a A B d g^2 x \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]-2 b B^2 d f^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+ \\
 & 2 a B^2 d f g \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]-2 b B^2 d f g x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+ \\
 & 2 a B^2 d g^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+2 b B^2 d f^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]- \\
 & 2 a B^2 d f g \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+2 b B^2 d f g x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]- \\
 & 2 a B^2 d g^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+2 b B^2 d f^2 \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]- \\
 & 2 b B^2 c f g \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+2 b B^2 d f g x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]- \\
 & 2 b B^2 c g^2 x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+2 B^2(b c-a d) g(f+g x) \\
 & \operatorname{PolyLog}\left[2, \frac{g(a+b x)}{-b f+a g}\right]-2 B^2(b c-a d) g(f+g x) \operatorname{PolyLog}\left[2, \frac{g(c+d x)}{-d f+c g}\right]- \\
 & 2 b B^2 c f g \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]+2 a B^2 d f g \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]- \\
 & 2 b B^2 c g^2 x \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]+2 a B^2 d g^2 x \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]
 \end{aligned}$$

Problem 246: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{(f+g x)^3} d x$$

Optimal (type 4, 369 leaves, 9 steps):

$$\begin{aligned}
 & \frac{B(b c-a d) g(a+b x)\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{(b f-a g)^2(d f-c g)(f+g x)}+ \\
 & \frac{b^2\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{2 g(b f-a g)^2}-\frac{\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{2 g(f+g x)^2}+\frac{B^2(b c-a d)^2 g \operatorname{Log}\left[\frac{f+g x}{c+d x}\right]}{(b f-a g)^2(d f-c g)^2}+ \\
 & \left(B(b c-a d)(2 b d f-b c g-a d g)\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right) \operatorname{Log}\left[1-\frac{(d f-c g)(a+b x)}{(b f-a g)(c+d x)}\right]\right) / \\
 & \left((b f-a g)^2(d f-c g)^2\right)+\frac{B^2(b c-a d)(2 b d f-b c g-a d g) \operatorname{PolyLog}\left[2, \frac{(d f-c g)(a+b x)}{(b f-a g)(c+d x)}\right]}{(b f-a g)^2(d f-c g)^2}
 \end{aligned}$$

Result (type 4, 18 235 leaves):

$$\begin{aligned}
 & -\frac{A^2}{2 g (f+g x)^2} + 2 A B \\
 & \left(\frac{1}{2 g} \left(\frac{g \left(\frac{a}{b} + x \right)}{\left(-f + \frac{a g}{b} \right)^3 \left(1 - \frac{g \left(\frac{a+x}{b} \right)}{-f + \frac{a g}{b}} \right)} - \left(\frac{g^2 \left(\frac{a}{b} + x \right)^2}{\left(-f + \frac{a g}{b} \right)^4 \left(1 - \frac{g \left(\frac{a+x}{b} \right)}{-f + \frac{a g}{b}} \right)^2} + \frac{2 g \left(\frac{a}{b} + x \right)}{\left(-f + \frac{a g}{b} \right)^3 \left(1 - \frac{g \left(\frac{a+x}{b} \right)}{-f + \frac{a g}{b}} \right)} \right) \text{Log} \left[\frac{a}{b} + x \right] - \right. \\
 & \left. \frac{\text{Log} \left[1 - \frac{g \left(\frac{a+x}{b} \right)}{-f + \frac{a g}{b}} \right]}{\left(-f + \frac{a g}{b} \right)^2} \right) - \frac{1}{2 g} \left(\frac{g \left(\frac{c}{d} + x \right)}{\left(-f + \frac{c g}{d} \right)^3 \left(1 - \frac{g \left(\frac{c+x}{d} \right)}{-f + \frac{c g}{d}} \right)} - \right. \\
 & \left. \left(\frac{g^2 \left(\frac{c}{d} + x \right)^2}{\left(-f + \frac{c g}{d} \right)^4 \left(1 - \frac{g \left(\frac{c+x}{d} \right)}{-f + \frac{c g}{d}} \right)^2} + \frac{2 g \left(\frac{c}{d} + x \right)}{\left(-f + \frac{c g}{d} \right)^3 \left(1 - \frac{g \left(\frac{c+x}{d} \right)}{-f + \frac{c g}{d}} \right)} \right) \text{Log} \left[\frac{c}{d} + x \right] - \frac{\text{Log} \left[1 - \frac{g \left(\frac{c+x}{d} \right)}{-f + \frac{c g}{d}} \right]}{\left(-f + \frac{c g}{d} \right)^2} \right) - \\
 & \left. \frac{-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a e}{c+d x} + \frac{b e x}{c+d x} \right]}{2 g (f+g x)^2} \right) + \\
 & B^2 \left(2 \left(\frac{1}{2 g} \left(\frac{g \left(\frac{a}{b} + x \right)}{\left(-f + \frac{a g}{b} \right)^3 \left(1 - \frac{g \left(\frac{a+x}{b} \right)}{-f + \frac{a g}{b}} \right)} - \left(\frac{g^2 \left(\frac{a}{b} + x \right)^2}{\left(-f + \frac{a g}{b} \right)^4 \left(1 - \frac{g \left(\frac{a+x}{b} \right)}{-f + \frac{a g}{b}} \right)^2} + \frac{2 g \left(\frac{a}{b} + x \right)}{\left(-f + \frac{a g}{b} \right)^3 \left(1 - \frac{g \left(\frac{a+x}{b} \right)}{-f + \frac{a g}{b}} \right)} \right) \right. \right. \\
 & \left. \left. \text{Log} \left[\frac{a}{b} + x \right] - \frac{\text{Log} \left[1 - \frac{g \left(\frac{a+x}{b} \right)}{-f + \frac{a g}{b}} \right]}{\left(-f + \frac{a g}{b} \right)^2} \right) - \frac{1}{2 g} \left(\frac{g \left(\frac{c}{d} + x \right)}{\left(-f + \frac{c g}{d} \right)^3 \left(1 - \frac{g \left(\frac{c+x}{d} \right)}{-f + \frac{c g}{d}} \right)} - \right. \right. \\
 & \left. \left. \left(\frac{g^2 \left(\frac{c}{d} + x \right)^2}{\left(-f + \frac{c g}{d} \right)^4 \left(1 - \frac{g \left(\frac{c+x}{d} \right)}{-f + \frac{c g}{d}} \right)^2} + \frac{2 g \left(\frac{c}{d} + x \right)}{\left(-f + \frac{c g}{d} \right)^3 \left(1 - \frac{g \left(\frac{c+x}{d} \right)}{-f + \frac{c g}{d}} \right)} \right) \text{Log} \left[\frac{c}{d} + x \right] - \frac{\text{Log} \left[1 - \frac{g \left(\frac{c+x}{d} \right)}{-f + \frac{c g}{d}} \right]}{\left(-f + \frac{c g}{d} \right)^2} \right) \right) \\
 & \left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a e}{c+d x} + \frac{b e x}{c+d x} \right] \right) - \\
 & \left. \frac{\left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a e}{c+d x} + \frac{b e x}{c+d x} \right] \right)^2}{2 g (f+g x)^2} + \frac{1}{g} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(-\frac{1}{2} \left(\frac{g^2 \left(\frac{a}{b} + x\right)^2}{\left(-f + \frac{ag}{b}\right)^4 \left(1 - \frac{g\left(\frac{a}{b} + x\right)}{-f + \frac{ag}{b}}\right)^2} + \frac{2g\left(\frac{a}{b} + x\right)}{\left(-f + \frac{ag}{b}\right)^3 \left(1 - \frac{g\left(\frac{a}{b} + x\right)}{-f + \frac{ag}{b}}\right)} \right) \text{Log}\left[\frac{a}{b} + x\right]^2 + \frac{\text{Log}\left[1 - \frac{g\left(\frac{a}{b} + x\right)}{-f + \frac{ag}{b}}\right]}{\left(-f + \frac{ag}{b}\right)^2} + \right. \\
 & \text{Log}\left[\frac{a}{b} + x\right] \left(\frac{g\left(\frac{a}{b} + x\right)}{\left(-f + \frac{ag}{b}\right)^3 \left(1 - \frac{g\left(\frac{a}{b} + x\right)}{-f + \frac{ag}{b}}\right)} - \frac{\text{Log}\left[1 - \frac{g\left(\frac{a}{b} + x\right)}{-f + \frac{ag}{b}}\right]}{\left(-f + \frac{ag}{b}\right)^2} - \frac{\text{PolyLog}\left[2, \frac{g\left(\frac{a}{b} + x\right)}{-f + \frac{ag}{b}}\right]}{\left(-f + \frac{ag}{b}\right)^2} \right) + \frac{1}{g} \\
 & \left(-\frac{1}{2} \left(\frac{g^2 \left(\frac{c}{d} + x\right)^2}{\left(-f + \frac{cg}{d}\right)^4 \left(1 - \frac{g\left(\frac{c}{d} + x\right)}{-f + \frac{cg}{d}}\right)^2} + \frac{2g\left(\frac{c}{d} + x\right)}{\left(-f + \frac{cg}{d}\right)^3 \left(1 - \frac{g\left(\frac{c}{d} + x\right)}{-f + \frac{cg}{d}}\right)} \right) \text{Log}\left[\frac{c}{d} + x\right]^2 + \frac{\text{Log}\left[1 - \frac{g\left(\frac{c}{d} + x\right)}{-f + \frac{cg}{d}}\right]}{\left(-f + \frac{cg}{d}\right)^2} + \right. \\
 & \left. \text{Log}\left[\frac{c}{d} + x\right] \left(\frac{g\left(\frac{c}{d} + x\right)}{\left(-f + \frac{cg}{d}\right)^3 \left(1 - \frac{g\left(\frac{c}{d} + x\right)}{-f + \frac{cg}{d}}\right)} - \frac{\text{Log}\left[1 - \frac{g\left(\frac{c}{d} + x\right)}{-f + \frac{cg}{d}}\right]}{\left(-f + \frac{cg}{d}\right)^2} - \frac{\text{PolyLog}\left[2, \frac{g\left(\frac{c}{d} + x\right)}{-f + \frac{cg}{d}}\right]}{\left(-f + \frac{cg}{d}\right)^2} \right) - \right. \\
 & \left. \frac{1}{f^2} \left(\frac{1}{g} 2 \left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + \frac{1}{2} \text{Log}\left[\frac{dg\left(\frac{c}{d} + x\right)}{-df+cg}\right] \right) \right. \\
 & \left. \left(-2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{dg\left(\frac{c}{d} + x\right)}{-df+cg}\right] \right) \left(\text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - \text{Log}\left[-\frac{d(f+gx)}{-df+cg}\right] \right) + \text{Log}\left[\right. \right. \\
 & \left. \left. \frac{dg\left(\frac{c}{d} + x\right)}{-df+cg} \right] \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d} + x\right)}{b(-df+cg)\left(\frac{a}{b} + x\right)}\right] \left(-\text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + \text{Log}\left[-\frac{d(f+gx)}{-df+cg}\right] \right) \right) + \\
 & \frac{1}{2} \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d} + x\right)}{b(-df+cg)\left(\frac{a}{b} + x\right)}\right]^2 \left(\text{Log}\left[\frac{-bc+ad}{bd\left(\frac{a}{b} + x\right)}\right] + \text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - \right. \\
 & \left. \text{Log}\left[-\frac{(-bc+ad)(f+gx)}{b(-df+cg)\left(\frac{a}{b} + x\right)}\right] \right) + \left(\text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d} + x\right)}{b(-df+cg)\left(\frac{a}{b} + x\right)}\right] \right) \\
 & \text{PolyLog}\left[2, -\frac{bg\left(\frac{a}{b} + x\right)}{bf-ag}\right] + \left(\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d} + x\right)}{b(-df+cg)\left(\frac{a}{b} + x\right)}\right] \right) \\
 & \text{PolyLog}\left[2, \frac{dg\left(\frac{c}{d} + x\right)}{-df+cg}\right] + \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d} + x\right)}{b(-df+cg)\left(\frac{a}{b} + x\right)}\right] \left(\text{PolyLog}\left[2, \frac{c}{\frac{a}{b} + x}\right] - \right.
 \end{aligned}$$

$$\begin{aligned}
 & \text{PolyLog}\left[2, -\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right] - \text{PolyLog}\left[3, -\frac{bg\left(\frac{a}{b}+x\right)}{bf-ag}\right] - \\
 & \text{PolyLog}\left[3, \frac{dg\left(\frac{c}{d}+x\right)}{-df+cg}\right] - \text{PolyLog}\left[3, \frac{\frac{c}{d}+x}{\frac{a}{b}+x}\right] + \text{PolyLog}\left[3, -\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right] + \\
 & g^2 \left(\left(\frac{(bf-ag)\left(\frac{-2abx}{(bf-ag)^2} + \frac{2a^2b(f+gx)}{(bf-ag)^3}\right)}{b(f+gx)} - \frac{(bf-ag)x\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)^2} - \right. \right. \\
 & \left. \frac{a\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)} \right) \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{c}{d}+x\right] - \left(2b(-df+cg)\left(\frac{a}{b}+x\right) \right. \\
 & \left. \left(\frac{cd(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)} + \frac{ad\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right) \left(\frac{(bf-ag)\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)} + \right. \right. \\
 & \left. \left. \left(b(-df+cg)\left(\frac{a}{b}+x\right)\left(-\frac{(-bc+ad)x}{b(-df+cg)\left(\frac{a}{b}+x\right)} + \frac{c(-bc+ad)(f+gx)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)}\right)\right) \right) / \\
 & \left. \left((-bc+ad)(f+gx)\right) \right) \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right] / \left(d(bf-ag)\left(\frac{c}{d}+ \right. \right. \\
 & \left. \left. x\right)\right) + \left(-\frac{(bf-ag)\left(\frac{-2abx}{(bf-ag)^2} + \frac{2a^2b(f+gx)}{(bf-ag)^3}\right)}{b(f+gx)} + \frac{(bf-ag)x\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)^2} + \right. \\
 & \left. \frac{a\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)} - \frac{(-df+cg)\left(\frac{-2cdx}{(-df+cg)^2} - \frac{2c^2d(f+gx)}{(-df+cg)^3}\right)}{d(f+gx)} + \right. \\
 & \left. \frac{(-df+cg)x\left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2}\right)}{d(f+gx)^2} - \frac{c\left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2}\right)}{d(f+gx)} \right) \text{Log}\left[\frac{dg\left(\frac{c}{d}+x\right)}{-df+cg}\right] \\
 & \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right] + \frac{1}{2} \left(\frac{(bf-ag)\left(\frac{-2abx}{(bf-ag)^2} + \frac{2a^2b(f+gx)}{(bf-ag)^3}\right)}{b(f+gx)} - \right. \\
 & \left. \frac{(bf-ag)x\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)^2} - \frac{a\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)} + \right. \\
 & \left. \left(b(-df+cg)\left(\frac{a}{b}+x\right)\left(\frac{2c(-bc+ad)x}{b(-df+cg)^2\left(\frac{a}{b}+x\right)} - \frac{2c^2(-bc+ad)(f+gx)}{b(-df+cg)^3\left(\frac{a}{b}+x\right)}\right)\right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left((-bc+ad)(f+gx) \right) - \left(b(-df+cg)x \left(\frac{a}{b} + x \right) \left(-\frac{(-bc+ad)x}{b(-df+cg)\left(\frac{a}{b}+x\right)} + \right. \right. \\
 & \left. \left. \frac{c(-bc+ad)(f+gx)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)} \right) \right) / \left((-bc+ad)(f+gx)^2 \right) + \\
 & \frac{bc\left(\frac{a}{b}+x\right)\left(-\frac{(-bc+ad)x}{b(-df+cg)\left(\frac{a}{b}+x\right)} + \frac{c(-bc+ad)(f+gx)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)}\right)}{(-bc+ad)(f+gx)} \left. \right) \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right]^2 + \\
 & 2 \left(-\frac{(bf-ag)\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)} - \frac{(-df+cg)\left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2}\right)}{d(f+gx)} \right) \\
 & \left(-\left(\left(b(-df+cg)\left(\frac{a}{b}+x\right) \left(\frac{cd(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)} + \frac{ad\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)} \right) \right. \right. \right. \\
 & \left. \left. \text{Log}\left[\frac{dg\left(\frac{c}{d}+x\right)}{-df+cg}\right] \right) / \left(d(bf-ag)\left(\frac{c}{d}+x\right) \right) \right) + \frac{1}{dg\left(\frac{c}{d}+x\right)} \\
 & (-df+cg) \left(-\frac{cdg\left(\frac{c}{d}+x\right)}{(-df+cg)^2} + \frac{d\left(\frac{c}{d}+x\right)}{-df+cg} \right) \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right] + \\
 & \frac{1}{dg\left(\frac{c}{d}+x\right)} (-df+cg) \left(-\frac{cdg\left(\frac{c}{d}+x\right)}{(-df+cg)^2} + \frac{d\left(\frac{c}{d}+x\right)}{-df+cg} \right) \\
 & \left(\left(\frac{(bf-ag)\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)} + \frac{(-df+cg)\left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2}\right)}{d(f+gx)} \right) \right. \\
 & \left. \left(-2 \text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{dg\left(\frac{c}{d}+x\right)}{-df+cg}\right] \right) + \frac{1}{dg\left(\frac{c}{d}+x\right)} (-df+cg) \right. \\
 & \left. \left(-\frac{cdg\left(\frac{c}{d}+x\right)}{(-df+cg)^2} + \frac{d\left(\frac{c}{d}+x\right)}{-df+cg} \right) \left(\text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - \text{Log}\left[-\frac{d(f+gx)}{-df+cg}\right] \right) \right) + \\
 & \frac{1}{2} \text{Log}\left[\frac{dg\left(\frac{c}{d}+x\right)}{-df+cg}\right] \left(\frac{1}{dg\left(\frac{c}{d}+x\right)} 2(-df+cg) \left(-\frac{cdg\left(\frac{c}{d}+x\right)}{(-df+cg)^2} + \frac{d\left(\frac{c}{d}+x\right)}{-df+cg} \right) \right. \\
 & \left. \left(\frac{(bf-ag)\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)} + \frac{(-df+cg)\left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2}\right)}{d(f+gx)} \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left(\frac{(b f - a g) \left(\frac{2 a b x}{(b f - a g)^2} + \frac{2 a^2 b (f + g x)}{(b f - a g)^3} \right)}{b (f + g x)} - \frac{(b f - a g) x \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right)}{b (f + g x)^2} \right. \\
 & \frac{a \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right)}{b (f + g x)} + \frac{(-d f + c g) \left(\frac{2 c d x}{(-d f + c g)^2} - \frac{2 c^2 d (f + g x)}{(-d f + c g)^3} \right)}{d (f + g x)} - \\
 & \frac{(-d f + c g) x \left(-\frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2} \right)}{d (f + g x)^2} + \\
 & \left. \frac{c \left(-\frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2} \right)}{d (f + g x)} \right) \left(-2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right) + \\
 & \left(\frac{(-d f + c g) \left(\frac{2 c^2 d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^3} - \frac{2 c d \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} \right)}{d g \left(\frac{c}{d} + x \right)} + \frac{c \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right)}{d g \left(\frac{c}{d} + x \right)} \right. \\
 & \left. \frac{(-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right)}{d g^2 \left(\frac{c}{d} + x \right)} \right) \left(\operatorname{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \operatorname{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) + \\
 & \frac{1}{2} \left(\frac{(-d f + c g) \left(\frac{2 c^2 d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^3} - \frac{2 c d \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} \right)}{d g \left(\frac{c}{d} + x \right)} + \frac{c \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right)}{d g \left(\frac{c}{d} + x \right)} \right. \\
 & \left. \frac{(-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right)}{d g^2 \left(\frac{c}{d} + x \right)} \right) \\
 & \left(-2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right) \left(\operatorname{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \operatorname{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) + \\
 & \left(- \left(\left(2 b (-d f + c g)^2 \left(\frac{a}{b} + x \right) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right) \right) / \left(d^2 g (b f - a g) \left(\frac{c}{d} + x \right)^2 \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left(- \left(\left(b (-d f + c g) \left(\frac{a}{b} + x \right) \left(- \frac{2 c^2 d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^3 \left(\frac{a}{b} + x \right)} - \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{2 a c d \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right) \right) / \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) \right) - \\
 & \frac{b c \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right)}{d (b f - a g) \left(\frac{c}{d} + x \right)} - \left(a b (-d f + c g) \left(\frac{a}{b} + x \right) \right. \\
 & \quad \left. \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right) / \left(d (b f - a g)^2 \right. \\
 & \quad \left. \left(\frac{c}{d} + x \right) \right) \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] + \left(\frac{(-d f + c g) \left(\frac{2 c^2 d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^3} - \frac{2 c d \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} \right)}{d g \left(\frac{c}{d} + x \right)} \right) + \\
 & \quad \left. \frac{c \left(- \frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right)}{d g \left(\frac{c}{d} + x \right)} - \frac{(-d f + c g) \left(- \frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right)}{d g^2 \left(\frac{c}{d} + x \right)} \right) \\
 & \quad \left. \text{Log} \left[- \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) \left(- \text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] + \text{Log} \left[- \frac{d (f + g x)}{-d f + c g} \right] \right) + \\
 & \frac{1}{2} \left(\left(2 b^2 (-d f + c g)^2 \left(\frac{a}{b} + x \right)^2 \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right) / \right. \\
 & \quad \left(d^2 (b f - a g)^2 \left(\frac{c}{d} + x \right)^2 \right) - \left(2 b (-d f + c g) \left(\frac{a}{b} + x \right) \left(- \frac{2 c^2 d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^3 \left(\frac{a}{b} + x \right)} - \right. \right. \\
 & \quad \left. \left. \frac{2 a c d \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[- \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) / \left(d (b f - a g) \right. \\
 & \quad \left. \left(\frac{c}{d} + x \right) \right) - \left(2 b c \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right. \\
 & \quad \left. \text{Log} \left[- \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left(2 a b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right. \\
 & \quad \left. \text{Log} \left[- \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) / \left(d (b f - a g)^2 \left(\frac{c}{d} + x \right) \right) \\
 & \left(\text{Log} \left[\frac{-b c + a d}{b d \left(\frac{a}{b} + x \right)} \right] + \text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \text{Log} \left[- \frac{(-b c + a d) (f + g x)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) + \\
 & \frac{(b f - a g)^2 \left(- \frac{a b g \left(\frac{a}{b} + x \right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x \right)}{b f - a g} \right)^2 \text{Log} \left[1 + \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right]}{b^2 g^2 \left(\frac{a}{b} + x \right)^2} + \frac{1}{d g \left(\frac{c}{d} + x \right)} 2 (-d f + c g) \\
 & \left(- \frac{a b g \left(\frac{a}{b} + x \right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x \right)}{b f - a g} \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \\
 & \text{Log} \left[1 + \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right] + \left(\text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[- \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) \\
 & \left(\frac{(b f - a g) \left(- \frac{a b g \left(\frac{a}{b} + x \right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x \right)}{b f - a g} \right) \left(\frac{a b g \left(\frac{a}{b} + x \right)}{(b f - a g)^2} + \frac{b \left(\frac{a}{b} + x \right)}{b f - a g} \right)}{b g \left(\frac{a}{b} + x \right) \left(1 + \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right)} + \frac{1}{b g \left(\frac{a}{b} + x \right)} \right) \\
 & (b f - a g) \left(- \frac{2 a^2 b g \left(\frac{a}{b} + x \right)}{(b f - a g)^3} - \frac{2 a b \left(\frac{a}{b} + x \right)}{(b f - a g)^2} \right) \text{Log} \left[1 + \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right] - \\
 & \frac{a \left(- \frac{a b g \left(\frac{a}{b} + x \right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x \right)}{b f - a g} \right) \text{Log} \left[1 + \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right]}{b g \left(\frac{a}{b} + x \right)} - \\
 & \left. \frac{(b f - a g) \left(- \frac{a b g \left(\frac{a}{b} + x \right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x \right)}{b f - a g} \right) \text{Log} \left[1 + \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right]}{b g^2 \left(\frac{a}{b} + x \right)} \right) + \\
 & \frac{(-d f + c g)^2 \left(- \frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right)^2 \text{Log} \left[1 - \frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right]}{d^2 g^2 \left(\frac{c}{d} + x \right)^2} + \\
 & \left(2 b (-d f + c g)^2 \left(\frac{a}{b} + x \right) \left(- \frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \right)
 \end{aligned}$$

$$\left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \text{Log} \left[1 - \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right] /$$

$$\left(d^2 g (b f - a g) \left(\frac{c}{d} + x\right)^2 \right) + \left(\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \right)$$

$$\left(- \left(\left((-d f + c g) \left(\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} - \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g} \right) \left(-\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g} \right) \right) / \right.$$

$$\left. \left(d g \left(\frac{c}{d} + x\right) \left(1 - \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right) \right) \right) - \frac{1}{d g \left(\frac{c}{d} + x\right)}$$

$$(-d f + c g) \left(\frac{2 c^2 d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^3} - \frac{2 c d \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} \right) \text{Log} \left[1 - \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right] -$$

$$\frac{c \left(-\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g} \right) \text{Log} \left[1 - \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right]}{d g \left(\frac{c}{d} + x\right)} +$$

$$\left. \frac{(-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g} \right) \text{Log} \left[1 - \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right]}{d g^2 \left(\frac{c}{d} + x\right)} \right) +$$

$$\left(b^2 (-d f + c g)^2 \left(\frac{a}{b} + x\right)^2 \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right)^2 \right.$$

$$\left. \text{Log} \left[1 + \frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \right) /$$

$$\left(d^2 (b f - a g)^2 \left(\frac{c}{d} + x\right)^2 \right) + \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right]$$

$$\left(- \left(\left(b (-d f + c g) \left(\frac{a}{b} + x\right) \left(-\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} - \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \right) / \right.$$

$$\left. \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \right) /$$

$$\left(d (b f - a g) \left(\frac{c}{d} + x\right) \left(1 + \frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \right) -$$

$$\begin{aligned}
 & \left(b (-d f + c g) \left(\frac{a}{b} + x \right) \left(- \frac{2 c^2 d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^3 \left(\frac{a}{b} + x \right)} - \frac{2 a c d \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right) \right. \\
 & \quad \left. \text{Log} \left[1 + \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) - \\
 & \left(b c \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right. \\
 & \quad \left. \text{Log} \left[1 + \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) - \\
 & \left(a b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right. \\
 & \quad \left. \text{Log} \left[1 + \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) / \left(d (b f - a g)^2 \left(\frac{c}{d} + x \right) \right) + \frac{1}{b g \left(\frac{a}{b} + x \right)} \\
 & (b f - a g) \left(- \frac{2 a^2 b g \left(\frac{a}{b} + x \right)}{(b f - a g)^3} - \frac{2 a b \left(\frac{a}{b} + x \right)}{(b f - a g)^2} \right) \text{PolyLog} \left[2, - \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right] - \\
 & a \left(- \frac{a b g \left(\frac{a}{b} + x \right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x \right)}{b f - a g} \right) \text{PolyLog} \left[2, - \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right] \\
 & \quad \quad \quad \frac{b g \left(\frac{a}{b} + x \right)}{b g \left(\frac{a}{b} + x \right)} - \\
 & \frac{(b f - a g) \left(- \frac{a b g \left(\frac{a}{b} + x \right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x \right)}{b f - a g} \right) \text{PolyLog} \left[2, - \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right]}{b g^2 \left(\frac{a}{b} + x \right)} + \\
 & \left(\left(b (-d f + c g) \left(\frac{a}{b} + x \right) \left(- \frac{2 c^2 d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^3 \left(\frac{a}{b} + x \right)} - \frac{2 a c d \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right) \right) / \right. \\
 & \quad \left. \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) + \frac{b c \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right)}{d (b f - a g) \left(\frac{c}{d} + x \right)} + \right. \\
 & \quad \left. \left(a b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right) / \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(d (b f - a g)^2 \left(\frac{c}{d} + x \right) \right) \text{PolyLog}\left[2, -\frac{b g \left(\frac{a}{b} + x \right)}{b f - a g}\right] - \frac{1}{d g \left(\frac{c}{d} + x \right)} \\
 & (-d f + c g) \left(\frac{2 c^2 d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^3} - \frac{2 c d \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} \right) \text{PolyLog}\left[2, \frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g}\right] - \\
 & \frac{c \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \text{PolyLog}\left[2, \frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g}\right]}{d g \left(\frac{c}{d} + x \right)} + \\
 & \frac{(-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \text{PolyLog}\left[2, \frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g}\right]}{d g^2 \left(\frac{c}{d} + x \right)} + \\
 & \left(-\left(\left(b (-d f + c g) \left(\frac{a}{b} + x \right) \left(-\frac{2 c^2 d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^3 \left(\frac{a}{b} + x \right)} - \frac{2 a c d \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right) \right) \right) / \\
 & \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) - \frac{b c \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right)}{d (b f - a g) \left(\frac{c}{d} + x \right)} - \\
 & \left(a b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right) / \\
 & \left(d (b f - a g)^2 \left(\frac{c}{d} + x \right) \right) \text{PolyLog}\left[2, \frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g}\right] + \\
 & \left(-\left(\left(b (-d f + c g) \left(\frac{a}{b} + x \right) \left(-\frac{2 c^2 d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^3 \left(\frac{a}{b} + x \right)} - \frac{2 a c d \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right) \right) \right) / \\
 & \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) - \frac{b c \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right)}{d (b f - a g) \left(\frac{c}{d} + x \right)} - \\
 & \left(a b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left(d (b f - a g)^2 \left(\frac{c}{d} + x \right) \right) \right) \\
 & \left(\text{PolyLog}\left[2, \frac{\frac{c}{d} + x}{\frac{a}{b} + x}\right] - \text{PolyLog}\left[2, -\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \right) - \\
 & \left(b (-d f + c g) \left(\frac{a}{b} + x\right) \left(-\frac{2 c^2 d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^3 \left(\frac{a}{b} + x\right)} - \frac{2 a c d \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} \right) \right. \\
 & \left. \text{PolyLog}\left[2, -\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x\right) \right) - \\
 & \left(b c \left(\frac{a}{b} + x\right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \right. \\
 & \left. \text{PolyLog}\left[2, -\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x\right) \right) - \\
 & \left(a b (-d f + c g) \left(\frac{a}{b} + x\right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \right. \\
 & \left. \text{PolyLog}\left[2, -\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \right) / \left(d (b f - a g)^2 \left(\frac{c}{d} + x\right) \right) \right) - \\
 & \frac{1}{g^2} 2 \left(\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2}\right) \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right]}{b (f + g x)} + \right. \\
 & \left. \frac{1}{2} \left(\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2}\right)}{b (f + g x)} + \frac{(-d f + c g) \left(-\frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2}\right)}{d (f + g x)} \right) \right. \\
 & \left. \text{Log}\left[\frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g}\right] \left(-2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g}\right] \right) \right) + \\
 & \left(-\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2}\right)}{b (f + g x)} - \frac{(-d f + c g) \left(-\frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2}\right)}{d (f + g x)} \right) \text{Log}\left[\right. \\
 & \left. \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right] \text{Log}\left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] + \frac{1}{2} \left(\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2}\right)}{b (f + g x)} + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(b(-df+cg) \left(\frac{a}{b} + x \right) \left(-\frac{(-bc+ad)x}{b(-df+cg) \left(\frac{a}{b} + x \right)} + \frac{c(-bc+ad)(f+gx)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} \right) \right) / \\
 & \left((-bc+ad)(f+gx) \right) \left. \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right]^2 + \right. \\
 & \frac{1}{2dg \left(\frac{c}{d} + x \right)} (-df+cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df+cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df+cg} \right) \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \\
 & \left(\text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - \text{Log} \left[-\frac{d(f+gx)}{-df+cg} \right] \right) + \frac{1}{2dg \left(\frac{c}{d} + x \right)} \\
 & (-df+cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df+cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df+cg} \right) \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \right) \\
 & \left(\text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - \text{Log} \left[-\frac{d(f+gx)}{-df+cg} \right] \right) - \left(b(-df+cg) \left(\frac{a}{b} + x \right) \right. \\
 & \left. \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \right. \\
 & \left. \left(-\text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] + \text{Log} \left[-\frac{d(f+gx)}{-df+cg} \right] \right) \right) / \left(d(bf-ag) \left(\frac{c}{d} + x \right) \right) + \frac{1}{dg \left(\frac{c}{d} + x \right)} \\
 & (-df+cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df+cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df+cg} \right) \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \\
 & \left(-\text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] + \text{Log} \left[-\frac{d(f+gx)}{-df+cg} \right] \right) - \left(b(-df+cg) \left(\frac{a}{b} + x \right) \right. \\
 & \left. \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right. \\
 & \left. \left(\text{Log} \left[\frac{-bc+ad}{bd \left(\frac{a}{b} + x \right)} \right] + \text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - \text{Log} \left[-\frac{(-bc+ad)(f+gx)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) \right) / \\
 & \left(d(bf-ag) \left(\frac{c}{d} + x \right) \right) + \frac{1}{bg \left(\frac{a}{b} + x \right)} (bf-ag) \left(-\frac{abg \left(\frac{a}{b} + x \right)}{(bf-ag)^2} - \frac{b \left(\frac{a}{b} + x \right)}{bf-ag} \right) \\
 & \left(\text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) \text{Log} \left[1 + \frac{bg \left(\frac{a}{b} + x \right)}{bf-ag} \right] -
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{d g \left(\frac{c}{d} + x\right)} (-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g} \right) \left(\text{Log} \left[\frac{a}{b} + x \right] + \right. \\
 & \left. \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \right) \text{Log} \left[1 - \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right] - \left(b (-d f + c g) \left(\frac{a}{b} + x\right) \right. \\
 & \left. \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \right. \\
 & \left. \text{Log} \left[1 + \frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x\right) \right) + \frac{1}{b g \left(\frac{a}{b} + x\right)} \\
 & (b f - a g) \left(-\frac{a b g \left(\frac{a}{b} + x\right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x\right)}{b f - a g} \right) \text{PolyLog} \left[2, -\frac{b g \left(\frac{a}{b} + x\right)}{b f - a g} \right] + \\
 & \left(b (-d f + c g) \left(\frac{a}{b} + x\right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \right. \\
 & \left. \text{PolyLog} \left[2, -\frac{b g \left(\frac{a}{b} + x\right)}{b f - a g} \right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x\right) \right) - \frac{1}{d g \left(\frac{c}{d} + x\right)} \\
 & (-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g} \right) \text{PolyLog} \left[2, \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right] - \\
 & \left(b (-d f + c g) \left(\frac{a}{b} + x\right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \right. \\
 & \left. \text{PolyLog} \left[2, \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x\right) \right) - \left(b (-d f + c g) \left(\frac{a}{b} + x\right) \right. \\
 & \left. \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \right) \left(\text{PolyLog} \left[2, \frac{c}{b} + x \right] - \right. \\
 & \left. \text{PolyLog} \left[2, -\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x\right) \right) - \\
 & \left(b (-d f + c g) \left(\frac{a}{b} + x\right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \right. \\
 & \left. \text{PolyLog} \left[2, -\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x\right) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{g^3} 2 \left(\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{b(f+g x)}{b f - a g} \right] + \frac{1}{2} \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right. \\
 & \quad \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right) \left(\text{Log} \left[\frac{b(f+g x)}{b f - a g} \right] - \text{Log} \left[-\frac{d(f+g x)}{-d f + c g} \right] \right) + \\
 & \quad \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \text{Log} \left[-\frac{d(b f - a g) \left(\frac{c}{d} + x \right)}{b(-d f + c g) \left(\frac{a}{b} + x \right)} \right] \left(-\text{Log} \left[\frac{b(f+g x)}{b f - a g} \right] + \right. \\
 & \quad \left. \text{Log} \left[-\frac{d(f+g x)}{-d f + c g} \right] \right) + \frac{1}{2} \text{Log} \left[-\frac{d(b f - a g) \left(\frac{c}{d} + x \right)}{b(-d f + c g) \left(\frac{a}{b} + x \right)} \right]^2 \\
 & \quad \left(\text{Log} \left[\frac{-b c + a d}{b d \left(\frac{a}{b} + x \right)} \right] + \text{Log} \left[\frac{b(f+g x)}{b f - a g} \right] - \text{Log} \left[-\frac{(-b c + a d)(f+g x)}{b(-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) + \\
 & \quad \left(\text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[-\frac{d(b f - a g) \left(\frac{c}{d} + x \right)}{b(-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) \text{PolyLog} \left[2, -\frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right] + \\
 & \quad \left(\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[-\frac{d(b f - a g) \left(\frac{c}{d} + x \right)}{b(-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) \text{PolyLog} \left[2, \frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] + \\
 & \quad \text{Log} \left[-\frac{d(b f - a g) \left(\frac{c}{d} + x \right)}{b(-d f + c g) \left(\frac{a}{b} + x \right)} \right] \left(\text{PolyLog} \left[2, \frac{\frac{c}{d} + x}{\frac{a}{b} + x} \right] - \right. \\
 & \quad \left. \text{PolyLog} \left[2, -\frac{d(b f - a g) \left(\frac{c}{d} + x \right)}{b(-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) - \text{PolyLog} \left[3, -\frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right] - \text{PolyLog} \left[3, \right. \\
 & \quad \left. \frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] - \text{PolyLog} \left[3, \frac{\frac{c}{d} + x}{\frac{a}{b} + x} \right] + \text{PolyLog} \left[3, -\frac{d(b f - a g) \left(\frac{c}{d} + x \right)}{b(-d f + c g) \left(\frac{a}{b} + x \right)} \right] \left. \right) + \\
 & 4 g \left(\frac{1}{g} \left(\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f+g x)}{(b f - a g)^2} \right) \text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{c}{d} + x \right]}{b(f+g x)} + \right. \right. \\
 & \quad \left. \frac{1}{2} \left(\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f+g x)}{(b f - a g)^2} \right)}{b(f+g x)} + \frac{(-d f + c g) \left(-\frac{d x}{-d f + c g} + \frac{c d (f+g x)}{(-d f + c g)^2} \right)}{d(f+g x)} \right) \right. \\
 & \quad \left. \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right) + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(-\frac{(b f - a g) \left(\frac{-b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right)}{b (f + g x)} - \frac{(-d f + c g) \left(-\frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2} \right)}{d (f + g x)} \right) \\
 & \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] + \frac{1}{2} \left(\frac{(b f - a g) \left(\frac{-b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right)}{b (f + g x)} \right. \\
 & \left. \left(b (-d f + c g) \left(\frac{a}{b} + x \right) \left(-\frac{(-b c + a d) x}{b (-d f + c g) \left(\frac{a}{b} + x \right)} + \frac{c (-b c + a d) (f + g x)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right) \right) \right) / \\
 & \left((-b c + a d) (f + g x) \right) \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right]^2 + \\
 & \frac{1}{2 d g \left(\frac{c}{d} + x \right)} (-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \\
 & \left(\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) + \frac{1}{2 d g \left(\frac{c}{d} + x \right)} \\
 & (-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right) \\
 & \left(\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) - \left(b (-d f + c g) \left(\frac{a}{b} + x \right) \right. \\
 & \left. \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right. \\
 & \left. \left(-\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] + \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) \right) / \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) + \frac{1}{d g \left(\frac{c}{d} + x \right)} \\
 & (-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \\
 & \left(-\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] + \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) - \left(b (-d f + c g) \left(\frac{a}{b} + x \right) \right. \\
 & \left. \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right. \\
 & \left. \left(\text{Log} \left[\frac{-b c + a d}{b d \left(\frac{a}{b} + x \right)} \right] + \text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \text{Log} \left[-\frac{(-b c + a d) (f + g x)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) + \frac{1}{b g \left(\frac{a}{b} + x \right)} (b f - a g) \left(- \frac{a b g \left(\frac{a}{b} + x \right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x \right)}{b f - a g} \right) \\
 & \left(\text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[- \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) \text{Log} \left[1 + \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right] - \\
 & \frac{1}{d g \left(\frac{c}{d} + x \right)} (-d f + c g) \left(- \frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \\
 & \left(\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[- \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) \text{Log} \left[1 - \frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] - \\
 & \left(b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right. \\
 & \left. \text{Log} \left[- \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \text{Log} \left[1 + \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) / \\
 & \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) + \frac{(b f - a g) \left(- \frac{a b g \left(\frac{a}{b} + x \right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x \right)}{b f - a g} \right) \text{PolyLog} \left[2, - \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right]}{b g \left(\frac{a}{b} + x \right)} + \\
 & \left(b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right. \\
 & \left. \text{PolyLog} \left[2, - \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) - \\
 & \frac{(-d f + c g) \left(- \frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \text{PolyLog} \left[2, \frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right]}{d g \left(\frac{c}{d} + x \right)} - \\
 & \left(b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right. \\
 & \left. \text{PolyLog} \left[2, \frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) - \\
 & \left(b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \left(\text{PolyLog} \left[\right. \right. \\
 & \left. \left. 2, \frac{c}{d} + x \right] - \text{PolyLog} \left[2, - \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) \right) / \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left(b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right. \\
 & \quad \left. \text{PolyLog}\left[2, -\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)}\right] / \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) \right] - \\
 & \frac{1}{g^2} \left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{b (f + g x)}{b f - a g}\right] + \frac{1}{2} \text{Log}\left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g}\right] \right. \\
 & \quad \left. \left(-2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g}\right] \right) \left(\text{Log}\left[\frac{b (f + g x)}{b f - a g}\right] - \text{Log}\left[-\frac{d (f + g x)}{-d f + c g}\right] \right) + \right. \\
 & \quad \left. \text{Log}\left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g}\right] \text{Log}\left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)}\right] \right. \\
 & \quad \left. \left(-\text{Log}\left[\frac{b (f + g x)}{b f - a g}\right] + \text{Log}\left[-\frac{d (f + g x)}{-d f + c g}\right] \right) + \frac{1}{2} \text{Log}\left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)}\right]^2 \right. \\
 & \quad \left. \left(\text{Log}\left[\frac{-b c + a d}{b d \left(\frac{a}{b} + x \right)}\right] + \text{Log}\left[\frac{b (f + g x)}{b f - a g}\right] - \text{Log}\left[-\frac{(-b c + a d) (f + g x)}{b (-d f + c g) \left(\frac{a}{b} + x \right)}\right] \right) + \right. \\
 & \quad \left. \left(\text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)}\right] \right) \text{PolyLog}\left[2, -\frac{b g \left(\frac{a}{b} + x \right)}{b f - a g}\right] + \right. \\
 & \quad \left. \left(\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)}\right] \right) \text{PolyLog}\left[2, \frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g}\right] + \right. \\
 & \quad \left. \text{Log}\left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)}\right] \right. \\
 & \quad \left. \left(\text{PolyLog}\left[2, \frac{c}{d} + x\right] - \text{PolyLog}\left[2, -\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)}\right] \right) - \right. \\
 & \quad \left. \text{PolyLog}\left[3, -\frac{b g \left(\frac{a}{b} + x \right)}{b f - a g}\right] - \text{PolyLog}\left[3, \frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g}\right] - \right. \\
 & \quad \left. \left. \left. \left. \text{PolyLog}\left[3, \frac{c}{d} + x\right] + \text{PolyLog}\left[3, -\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)}\right] \right) \right) \right) \right) \right)
 \end{aligned}$$

Problem 247: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]\right)^2}{(f+gx)^4} dx$$

Optimal (type 4, 714 leaves, 12 steps):

$$\begin{aligned} & \frac{B^2 (bc - ad)^2 g^2 (c + dx)}{3 (bf - ag)^2 (df - cg)^3 (f + gx)} + \\ & \frac{B^2 (bc - ad)^3 g^2 \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]}{3 (bf - ag)^3 (df - cg)^3} - \frac{B (bc - ad) g^2 (c + dx)^2 \left(A + B \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]\right)}{3 (bf - ag) (df - cg)^3 (f + gx)^2} + \\ & \frac{2B (bc - ad) g (3 bdf - bcg - 2adg) (a + bx) \left(A + B \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]\right)}{3 (bf - ag)^3 (df - cg)^2 (f + gx)} + \\ & \frac{b^3 \left(A + B \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]\right)^2}{3g (bf - ag)^3} - \frac{\left(A + B \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]\right)^2}{3g (f + gx)^3} - \frac{B^2 (bc - ad)^3 g^2 \operatorname{Log}\left[\frac{f+gx}{c+dx}\right]}{3 (bf - ag)^3 (df - cg)^3} + \\ & \frac{2B^2 (bc - ad)^2 g (3 bdf - bcg - 2adg) \operatorname{Log}\left[\frac{f+gx}{c+dx}\right]}{3 (bf - ag)^3 (df - cg)^3} + \\ & \left(2B (bc - ad) (a^2 d^2 g^2 - abdg (3df - cg) + b^2 (3d^2 f^2 - 3cdfg + c^2 g^2))\right. \\ & \quad \left.\left(A + B \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]\right) \operatorname{Log}\left[1 - \frac{(df - cg)(a + bx)}{(bf - ag)(c + dx)}\right]\right) / (3 (bf - ag)^3 (df - cg)^3) + \\ & \left(2B^2 (bc - ad) (a^2 d^2 g^2 - abdg (3df - cg) + b^2 (3d^2 f^2 - 3cdfg + c^2 g^2))\right. \\ & \quad \left.\operatorname{PolyLog}\left[2, \frac{(df - cg)(a + bx)}{(bf - ag)(c + dx)}\right]\right) / (3 (bf - ag)^3 (df - cg)^3) \end{aligned}$$

Result (type 4, 55110 leaves): Display of huge result suppressed!

Problem 248: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]\right)^2}{(f+gx)^5} dx$$

Optimal (type 4, 1159 leaves, 15 steps):

$$\begin{aligned}
 & - \frac{B^2 (bc - ad)^2 g^3 (c + dx)^2}{12 (bf - ag)^2 (df - cg)^4 (f + gx)^2} - \frac{B^2 (bc - ad)^3 g^3 (c + dx)}{6 (bf - ag)^3 (df - cg)^4 (f + gx)} + \\
 & \frac{B^2 (bc - ad)^2 g^2 (4 bdf - bcg - 3 adg) (c + dx)}{4 (bf - ag)^3 (df - cg)^4 (f + gx)} - \frac{B^2 (bc - ad)^4 g^3 \text{Log}\left[\frac{a+bx}{c+dx}\right]}{6 (bf - ag)^4 (df - cg)^4} + \\
 & \frac{B^2 (bc - ad)^3 g^2 (4 bdf - bcg - 3 adg) \text{Log}\left[\frac{a+bx}{c+dx}\right]}{4 (bf - ag)^4 (df - cg)^4} + \\
 & \frac{B (bc - ad) g^3 (c + dx)^3 \left(A + B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{6 (bf - ag) (df - cg)^4 (f + gx)^3} - \\
 & \frac{B (bc - ad) g^2 (4 bdf - bcg - 3 adg) (c + dx)^2 \left(A + B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{4 (bf - ag)^2 (df - cg)^4 (f + gx)^2} + \\
 & \left(B (bc - ad) g (3 a^2 d^2 g^2 - 2 abdg (4 df - cg) + b^2 (6 d^2 f^2 - 4 cdfg + c^2 g^2)) \right. \\
 & \quad \left. (a + bx) \left(A + B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right) \right) / \left(2 (bf - ag)^4 (df - cg)^3 (f + gx) \right) + \\
 & \frac{b^4 \left(A + B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{4 g (bf - ag)^4} - \frac{\left(A + B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{4 g (f + gx)^4} + \frac{B^2 (bc - ad)^4 g^3 \text{Log}\left[\frac{f+gx}{c+dx}\right]}{6 (bf - ag)^4 (df - cg)^4} - \\
 & \frac{B^2 (bc - ad)^3 g^2 (4 bdf - bcg - 3 adg) \text{Log}\left[\frac{f+gx}{c+dx}\right]}{4 (bf - ag)^4 (df - cg)^4} + \\
 & \left(B^2 (bc - ad)^2 g (3 a^2 d^2 g^2 - 2 abdg (4 df - cg) + b^2 (6 d^2 f^2 - 4 cdfg + c^2 g^2)) \text{Log}\left[\frac{f+gx}{c+dx}\right] \right) / \\
 & \left(2 (bf - ag)^4 (df - cg)^4 \right) - \\
 & \left(B (bc - ad) (2 bdf - bcg - adg) (2 abd^2 fg - a^2 d^2 g^2 - b^2 (2 d^2 f^2 - 2 cdfg + c^2 g^2)) \right. \\
 & \quad \left. \left(A + B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right) \text{Log}\left[1 - \frac{(df - cg)(a + bx)}{(bf - ag)(c + dx)}\right] \right) / \left(2 (bf - ag)^4 (df - cg)^4 \right) - \\
 & \left(B^2 (bc - ad) (2 bdf - bcg - adg) (2 abd^2 fg - a^2 d^2 g^2 - b^2 (2 d^2 f^2 - 2 cdfg + c^2 g^2)) \right. \\
 & \quad \left. \text{PolyLog}\left[2, \frac{(df - cg)(a + bx)}{(bf - ag)(c + dx)}\right] \right) / \left(2 (bf - ag)^4 (df - cg)^4 \right)
 \end{aligned}$$

Result (type 4, 142893 leaves): Display of huge result suppressed!

Problem 272: Result more than twice size of optimal antiderivative.

$$\int (f + gx)^3 \left(A + B \text{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right] \right)^2 dx$$

Optimal (type 4, 869 leaves, 15 steps):

$$\begin{aligned} & \frac{2 B^2 (b c - a d)^3 g^3 x}{3 b^3 d^3} + \frac{B^2 (b c - a d)^2 g^2 (4 b d f - 3 b c g - a d g) x}{b^3 d^3} + \\ & \frac{B^2 (b c - a d)^2 g^3 (c + d x)^2}{3 b^2 d^4} - \frac{1}{b^4 d^3} B (b c - a d) g \\ & (a^2 d^2 g^2 - 2 a b d g (2 d f - c g) + b^2 (6 d^2 f^2 - 8 c d f g + 3 c^2 g^2)) (a + b x) \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right) - \\ & \frac{1}{2 b^2 d^4} B (b c - a d) g^2 (4 b d f - 3 b c g - a d g) (c + d x)^2 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right) - \\ & \frac{B (b c - a d) g^3 (c + d x)^3 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right)}{3 b d^4} - \frac{(b f - a g)^4 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right)^2}{4 b^4 g} + \\ & \frac{(f + g x)^4 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right)^2}{4 g} - \frac{1}{b^4 d^4} B (b c - a d) (2 b d f - b c g - a d g) \\ & (2 a b d^2 f g - a^2 d^2 g^2 - b^2 (2 d^2 f^2 - 2 c d f g + c^2 g^2)) \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right) \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right] + \\ & \frac{2 B^2 (b c - a d)^4 g^3 \operatorname{Log} \left[\frac{a + b x}{c + d x} \right]}{3 b^4 d^4} + \frac{B^2 (b c - a d)^3 g^2 (4 b d f - 3 b c g - a d g) \operatorname{Log} \left[\frac{a + b x}{c + d x} \right]}{b^4 d^4} + \\ & \frac{2 B^2 (b c - a d)^4 g^3 \operatorname{Log} [c + d x]}{3 b^4 d^4} + \frac{B^2 (b c - a d)^3 g^2 (4 b d f - 3 b c g - a d g) \operatorname{Log} [c + d x]}{b^4 d^4} + \frac{1}{b^4 d^4} \\ & 2 B^2 (b c - a d)^2 g (a^2 d^2 g^2 - 2 a b d g (2 d f - c g) + b^2 (6 d^2 f^2 - 8 c d f g + 3 c^2 g^2)) \operatorname{Log} [c + d x] - \\ & \frac{1}{b^4 d^4} 2 B^2 (b c - a d) (2 b d f - b c g - a d g) \\ & (2 a b d^2 f g - a^2 d^2 g^2 - b^2 (2 d^2 f^2 - 2 c d f g + c^2 g^2)) \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right] \end{aligned}$$

Result (type 4, 2279 leaves):

$$\begin{aligned} & A^2 f^3 x + \frac{3}{2} A^2 f^2 g x^2 + A^2 f g^2 x^3 + \frac{1}{4} A^2 g^3 x^4 + \\ & \frac{2 A B f^3 \left(2 a d \operatorname{Log} [a + b x] + b d x \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] - 2 b c \operatorname{Log} [c + d x] \right)}{b d} + \\ & \frac{1}{6} A B g^3 \left(\frac{6 a^3 x}{b^3} - \frac{6 c^3 x}{d^3} - \frac{3 a^2 x^2}{b^2} + \frac{3 c^2 x^2}{d^2} + \frac{2 a x^3}{b} - \right. \\ & \left. \frac{2 c x^3}{d} - \frac{6 a^4 \operatorname{Log} [a + b x]}{b^4} + 3 x^4 \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] + \frac{6 c^4 \operatorname{Log} [c + d x]}{d^4} \right) + \\ & 2 A B f g^2 \left(\frac{(b c - a d) x (2 b c + 2 a d - b d x)}{b^2 d^2} + \frac{2 a^3 \operatorname{Log} [a + b x]}{b^3} + \right. \\ & \left. x^3 \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] - \frac{2 c^3 \operatorname{Log} [c + d x]}{d^3} \right) + \frac{1}{b^2 d^2} 3 A B f^2 g \end{aligned}$$

$$\begin{aligned}
 & \left(-2 a^2 d^2 \operatorname{Log}[a+b x] + b \left(2 d (-b c+a d) x + b d^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + 2 b c^2 \operatorname{Log}[c+d x] \right) \right) + \\
 & \frac{1}{b d} B^2 f^3 \left(4 a d \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + 4 b c \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 8 a d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x] + \right. \\
 & \quad 8 a d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] - 8 a d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \\
 & \quad 4 a d \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + b d x \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]^2 + 8 b c \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] - \\
 & \quad 8 b c \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - 4 b c \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \operatorname{Log}[c+d x] - 8 b c \operatorname{Log}\left[\frac{a}{b}+x\right] \\
 & \quad \left. \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 8 b c \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] - 8 a d \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) + \\
 & \frac{1}{12 b^4 d^4} B^2 g^3 \left(-24 b^4 c^4 + 24 a b^3 c^3 d + 24 a^3 b c d^3 - 24 a^4 d^4 - 20 b^4 c^3 d x + 20 a b^3 c^2 d^2 x + \right. \\
 & \quad 20 a^2 b^2 c d^3 x - 20 a^3 b d^4 x + 4 b^4 c^2 d^2 x^2 - 8 a b^3 c d^3 x^2 + 4 a^2 b^2 d^4 x^2 - \\
 & \quad 24 a b^3 c^3 d \operatorname{Log}\left[\frac{a}{b}+x\right] + 24 a^4 d^4 \operatorname{Log}\left[\frac{a}{b}+x\right] - 12 a^4 d^4 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + 24 b^4 c^4 \operatorname{Log}\left[\frac{c}{d}+x\right] - \\
 & \quad 24 a^3 b c d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] - 12 b^4 c^4 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 12 a^2 b^2 c^2 d^2 \operatorname{Log}[a+b x] - \\
 & \quad 8 a^3 b c d^3 \operatorname{Log}[a+b x] + 20 a^4 d^4 \operatorname{Log}[a+b x] + 24 a^4 d^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x] - \\
 & \quad 24 a^4 d^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] + 24 a^4 d^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] - \\
 & \quad 12 b^4 c^3 d x \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + 12 a^3 b d^4 x \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + 6 b^4 c^2 d^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] - \\
 & \quad 6 a^2 b^2 d^4 x^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] - 4 b^4 c d^3 x^3 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + 4 a b^3 d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] - \\
 & \quad 12 a^4 d^4 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + 3 b^4 d^4 x^4 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]^2 + 20 b^4 c^4 \operatorname{Log}[c+d x] - \\
 & \quad 8 a b^3 c^3 d \operatorname{Log}[c+d x] - 12 a^2 b^2 c^2 d^2 \operatorname{Log}[c+d x] - 24 b^4 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + \\
 & \quad 24 b^4 c^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] + 12 b^4 c^4 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \operatorname{Log}[c+d x] + \\
 & \quad 24 b^4 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 24 b^4 c^4 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] + \\
 & \quad \left. 24 a^4 d^4 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) + 3 B^2 f^2 g \left(\frac{1}{2} x^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]^2 - \right. \\
 & \quad \left. \frac{1}{b^2 d^2} 2 \left(-2 d (-b c+a d) (a+b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b}+x\right] \right) + a^2 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 - 2 b (b c-a d) (c+d x) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(-1 + \text{Log}\left[\frac{c}{d} + x\right] \right) + b^2 c^2 \text{Log}\left[\frac{c}{d} + x\right]^2 - \left(2 \text{Log}\left[\frac{a}{b} + x\right] - 2 \text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{e (a + b x)^2}{(c + d x)^2}\right] \right) \\
 & \left(a^2 d^2 \text{Log}[a + b x] - b (d (-b c + a d) x + b c^2 \text{Log}[c + d x]) \right) - \\
 & 2 b^2 c^2 \left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) - \\
 & 2 a^2 d^2 \left(\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \text{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \Bigg) + \\
 B^2 f g^2 & \left(x^3 \text{Log}\left[\frac{e (a + b x)^2}{(c + d x)^2}\right]^2 - \frac{1}{b^3 d^3} 2 \left(4 d (-b c + a d) (b c + a d) (a + b x) \left(-1 + \text{Log}\left[\frac{a}{b} + x\right] \right) - \right. \right. \\
 & 2 a^3 d^3 \text{Log}\left[\frac{a}{b} + x\right]^2 + 4 b (b c - a d) (b c + a d) (c + d x) \left(-1 + \text{Log}\left[\frac{c}{d} + x\right] \right) - \\
 & 2 b^3 c^3 \text{Log}\left[\frac{c}{d} + x\right]^2 + d^2 (b c - a d) \left(b x (2 a - b x) + 2 b^2 x^2 \text{Log}\left[\frac{a}{b} + x\right] - 2 a^2 \text{Log}[a + b x] \right) + \\
 & b^2 (b c - a d) \left(d x (-2 c + d x) - 2 d^2 x^2 \text{Log}\left[\frac{c}{d} + x\right] + 2 c^2 \text{Log}[c + d x] \right) - \\
 & \left. \left(2 \text{Log}\left[\frac{a}{b} + x\right] - 2 \text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{e (a + b x)^2}{(c + d x)^2}\right] \right) \right) \\
 & \left(b d (b c - a d) x (-2 b c - 2 a d + b d x) - 2 a^3 d^3 \text{Log}[a + b x] + 2 b^3 c^3 \text{Log}[c + d x] \right) + \\
 & 4 b^3 c^3 \left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) + \\
 & 4 a^3 d^3 \left(\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \text{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \Bigg) \Bigg)
 \end{aligned}$$

Problem 273: Result more than twice size of optimal antiderivative.

$$\int (f + g x)^2 \left(A + B \text{Log}\left[\frac{e (a + b x)^2}{(c + d x)^2}\right] \right)^2 dx$$

Optimal (type 4, 542 leaves, 12 steps):

$$\begin{aligned}
 & \frac{4 B^2 (b c - a d)^2 g^2 x}{3 b^2 d^2} - \frac{4 B (b c - a d) g (3 b d f - 2 b c g - a d g) (a + b x) \left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)}{3 b^3 d^2} - \\
 & \frac{2 B (b c - a d) g^2 (c + d x)^2 \left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)}{3 b d^3} - \\
 & \frac{(b f - a g)^3 \left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)^2}{3 b^3 g} + \frac{(f + g x)^3 \left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)^2}{3 g} + \frac{1}{3 b^3 d^3} \\
 & 4 B (b c - a d) (a^2 d^2 g^2 - a b d g (3 d f - c g) + b^2 (3 d^2 f^2 - 3 c d f g + c^2 g^2)) \\
 & \left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right) \operatorname{Log} \left[\frac{b c - a d}{b (c+d x)} \right] + \frac{4 B^2 (b c - a d)^3 g^2 \operatorname{Log} \left[\frac{a+b x}{c+d x} \right]}{3 b^3 d^3} + \\
 & \frac{4 B^2 (b c - a d)^3 g^2 \operatorname{Log} [c + d x]}{3 b^3 d^3} + \frac{8 B^2 (b c - a d)^2 g (3 b d f - 2 b c g - a d g) \operatorname{Log} [c + d x]}{3 b^3 d^3} + \frac{1}{3 b^3 d^3} \\
 & 8 B^2 (b c - a d) (a^2 d^2 g^2 - a b d g (3 d f - c g) + b^2 (3 d^2 f^2 - 3 c d f g + c^2 g^2)) \operatorname{PolyLog} \left[2, \frac{d (a+b x)}{b (c+d x)} \right]
 \end{aligned}$$

Result (type 4, 1323 leaves):

$$\begin{aligned}
 & \frac{1}{3} \\
 & \left(3 A^2 f^2 x + 3 A^2 f g x^2 + A^2 g^2 x^3 + \frac{6 A B f^2 (2 a d \operatorname{Log} [a + b x] + b d x \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] - 2 b c \operatorname{Log} [c + d x])}{b d} + \right. \\
 & 2 A B g^2 \left(\frac{(b c - a d) x (2 b c + 2 a d - b d x)}{b^2 d^2} + \frac{2 a^3 \operatorname{Log} [a + b x]}{b^3} + \right. \\
 & \left. \left. x^3 \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] - \frac{2 c^3 \operatorname{Log} [c + d x]}{d^3} \right) + \frac{1}{b^2 d^2} 6 A B f g \right. \\
 & \left. \left(-2 a^2 d^2 \operatorname{Log} [a + b x] + b \left(2 d (-b c + a d) x + b d^2 x^2 \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] + 2 b c^2 \operatorname{Log} [c + d x] \right) \right) + \right. \\
 & \frac{1}{b d} 3 B^2 f^2 \left(4 a d \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 4 b c \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 8 a d \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + b x] + \right. \\
 & 8 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + b x] - 8 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a+b x)}{-b c + a d} \right] + \\
 & 4 a d \operatorname{Log} [a + b x] \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] + b d x \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right]^2 + 8 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [c + d x] - \\
 & 8 b c \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [c + d x] - 4 b c \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \operatorname{Log} [c + d x] - 8 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \\
 & \left. \left. \operatorname{Log} \left[\frac{b (c+d x)}{b c - a d} \right] - 8 b c \operatorname{PolyLog} \left[2, \frac{d (a+b x)}{-b c + a d} \right] - 8 a d \operatorname{PolyLog} \left[2, \frac{b (c+d x)}{b c - a d} \right] \right) +
 \end{aligned}$$

$$\begin{aligned}
 & 6 B^2 f g \left(\frac{1}{2} x^2 \text{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right]^2 - \frac{1}{b^2 d^2} 2 \left(-2 d (-b c+a d) (a+b x) \left(-1+\text{Log} \left[\frac{a}{b}+x \right] \right) + \right. \right. \\
 & \quad a^2 d^2 \text{Log} \left[\frac{a}{b}+x \right]^2 - 2 b (b c-a d) (c+d x) \left(-1+\text{Log} \left[\frac{c}{d}+x \right] \right) + \\
 & \quad \left. \left. b^2 c^2 \text{Log} \left[\frac{c}{d}+x \right]^2 - \left(2 \text{Log} \left[\frac{a}{b}+x \right] - 2 \text{Log} \left[\frac{c}{d}+x \right] - \text{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right) \right) \right. \\
 & \quad \left(a^2 d^2 \text{Log} [a+b x] - b (d (-b c+a d) x+b c^2 \text{Log} [c+d x]) \right) - \\
 & \quad 2 b^2 c^2 \left(\text{Log} \left[\frac{a}{b}+x \right] \text{Log} \left[\frac{b (c+d x)}{b c-a d} \right] + \text{PolyLog} \left[2, \frac{d (a+b x)}{-b c+a d} \right] \right) - \\
 & \quad \left. \left. 2 a^2 d^2 \left(\text{Log} \left[\frac{c}{d}+x \right] \text{Log} \left[\frac{d (a+b x)}{-b c+a d} \right] + \text{PolyLog} \left[2, \frac{b (c+d x)}{b c-a d} \right] \right) \right) \right) + \\
 & B^2 g^2 \left(x^3 \text{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right]^2 - \frac{1}{b^3 d^3} 2 \left(4 d (-b c+a d) (b c+a d) (a+b x) \left(-1+\text{Log} \left[\frac{a}{b}+x \right] \right) - \right. \right. \\
 & \quad 2 a^3 d^3 \text{Log} \left[\frac{a}{b}+x \right]^2 + 4 b (b c-a d) (b c+a d) (c+d x) \left(-1+\text{Log} \left[\frac{c}{d}+x \right] \right) - \\
 & \quad 2 b^3 c^3 \text{Log} \left[\frac{c}{d}+x \right]^2 + d^2 (b c-a d) \left(b x (2 a-b x) + 2 b^2 x^2 \text{Log} \left[\frac{a}{b}+x \right] - 2 a^2 \text{Log} [a+b x] \right) + \\
 & \quad \left. \left. b^2 (b c-a d) \left(d x (-2 c+d x) - 2 d^2 x^2 \text{Log} \left[\frac{c}{d}+x \right] + 2 c^2 \text{Log} [c+d x] \right) - \right. \right. \\
 & \quad \left. \left(2 \text{Log} \left[\frac{a}{b}+x \right] - 2 \text{Log} \left[\frac{c}{d}+x \right] - \text{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right) \right) \right. \\
 & \quad \left(b d (b c-a d) x (-2 b c-2 a d+b d x) - 2 a^3 d^3 \text{Log} [a+b x] + 2 b^3 c^3 \text{Log} [c+d x] \right) + \\
 & \quad 4 b^3 c^3 \left(\text{Log} \left[\frac{a}{b}+x \right] \text{Log} \left[\frac{b (c+d x)}{b c-a d} \right] + \text{PolyLog} \left[2, \frac{d (a+b x)}{-b c+a d} \right] \right) + \\
 & \quad \left. \left. 4 a^3 d^3 \left(\text{Log} \left[\frac{c}{d}+x \right] \text{Log} \left[\frac{d (a+b x)}{-b c+a d} \right] + \text{PolyLog} \left[2, \frac{b (c+d x)}{b c-a d} \right] \right) \right) \right) \right)
 \end{aligned}$$

Problem 274: Result more than twice size of optimal antiderivative.

$$\int (f+g x) \left(A+B \text{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)^2 dx$$

Optimal (type 4, 281 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{2 B (b c - a d) g (a + b x) \left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)}{b^2 d} - \\
 & \frac{(b f - a g)^2 \left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)^2}{2 b^2 g} + \frac{(f + g x)^2 \left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)^2}{2 g} + \frac{1}{b^2 d^2} \\
 & 2 B (b c - a d) (2 b d f - b c g - a d g) \left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right) \operatorname{Log} \left[\frac{b c - a d}{b (c+d x)} \right] + \\
 & \frac{4 B^2 (b c - a d)^2 g \operatorname{Log}[c+d x]}{b^2 d^2} + \frac{4 B^2 (b c - a d) (2 b d f - b c g - a d g) \operatorname{PolyLog} \left[2, \frac{d (a+b x)}{b (c+d x)} \right]}{b^2 d^2}
 \end{aligned}$$

Result (type 4, 767 leaves):

$$\begin{aligned}
 & \frac{1}{2 b^2 d^2} \left(2 A^2 b^2 d^2 f x + A^2 b^2 d^2 g x^2 + \right. \\
 & 4 A b B d f \left(2 a d \operatorname{Log}[a+b x] + b d x \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] - 2 b c \operatorname{Log}[c+d x] \right) - \\
 & 2 A B g \left(2 a^2 d^2 \operatorname{Log}[a+b x] - b \left(2 d (-b c + a d) x + b d^2 x^2 \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] + 2 b c^2 \operatorname{Log}[c+d x] \right) \right) + \\
 & 2 b B^2 d f \left(4 a d \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 4 b c \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 8 a d \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log}[a+b x] + \right. \\
 & 8 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log}[a+b x] - 8 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a+b x)}{-b c + a d} \right] + \\
 & 4 a d \operatorname{Log}[a+b x] \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] + b d x \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right]^2 + 8 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log}[c+d x] - \\
 & 8 b c \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log}[c+d x] - 4 b c \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \operatorname{Log}[c+d x] - 8 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \\
 & \left. \operatorname{Log} \left[\frac{b (c+d x)}{b c - a d} \right] - 8 b c \operatorname{PolyLog} \left[2, \frac{d (a+b x)}{-b c + a d} \right] - 8 a d \operatorname{PolyLog} \left[2, \frac{b (c+d x)}{b c - a d} \right] \right) + \\
 & B^2 g \left(8 d (-b c + a d) (a+b x) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) - 4 a^2 d^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + \right. \\
 & 8 b (b c - a d) (c+d x) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) - 4 b^2 c^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + \\
 & b^2 d^2 x^2 \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right]^2 + 4 \left(2 \operatorname{Log} \left[\frac{a}{b} + x \right] - 2 \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right) \\
 & \left(a^2 d^2 \operatorname{Log}[a+b x] - b (d (-b c + a d) x + b c^2 \operatorname{Log}[c+d x]) \right) + \\
 & 8 b^2 c^2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c+d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d (a+b x)}{-b c + a d} \right] \right) + \\
 & \left. 8 a^2 d^2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a+b x)}{-b c + a d} \right] + \operatorname{PolyLog} \left[2, \frac{b (c+d x)}{b c - a d} \right] \right) \right)
 \end{aligned}$$

Problem 275: Result more than twice size of optimal antiderivative.

$$\int \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right)^2 dx$$

Optimal (type 4, 129 leaves, 6 steps):

$$\frac{(a + b x) \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right)^2}{b} + \frac{4 B (b c - a d) \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right) \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right]}{b d} + \frac{8 B^2 (b c - a d) \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{b d}$$

Result (type 4, 385 leaves):

$$\begin{aligned} & \frac{1}{b d} \left(A^2 b d x + 4 a B^2 d \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 4 b B^2 c \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + \right. \\ & 4 a A B d \operatorname{Log} [a + b x] - 8 a B^2 d \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + b x] + 8 a B^2 d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + b x] - \\ & 8 a B^2 d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + 2 A b B d x \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] + \\ & 4 a B^2 d \operatorname{Log} [a + b x] \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] + b B^2 d x \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right]^2 - \\ & 4 A b B c \operatorname{Log} [c + d x] + 8 b B^2 c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [c + d x] - 8 b B^2 c \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [c + d x] - \\ & 4 b B^2 c \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \operatorname{Log} [c + d x] - 8 b B^2 c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] - \\ & \left. 8 b B^2 c \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] - 8 a B^2 d \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \end{aligned}$$

Problem 276: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right)^2}{f + g x} dx$$

Optimal (type 4, 285 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{\left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)^2 \operatorname{Log} \left[\frac{b c - a d}{b (c+d x)} \right]}{g} + \\
 & \frac{\left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)^2 \operatorname{Log} \left[1 - \frac{(d f - c g) (a+b x)}{(b f - a g) (c+d x)} \right]}{g} - \frac{4 B \left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right) \operatorname{PolyLog} \left[2, \frac{d (a+b x)}{b (c+d x)} \right]}{g} + \\
 & \frac{4 B \left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right) \operatorname{PolyLog} \left[2, \frac{(d f - c g) (a+b x)}{(b f - a g) (c+d x)} \right]}{g} + \\
 & \frac{8 B^2 \operatorname{PolyLog} \left[3, \frac{d (a+b x)}{b (c+d x)} \right]}{g} - \frac{8 B^2 \operatorname{PolyLog} \left[3, \frac{(d f - c g) (a+b x)}{(b f - a g) (c+d x)} \right]}{g}
 \end{aligned}$$

Result (type 4, 1370 leaves):

$$\begin{aligned}
 & \frac{1}{g} \left(-4 B^2 \operatorname{Log} \left[\frac{-b c + a d}{d (a+b x)} \right] \operatorname{Log} \left[\frac{(b f - a g) (c+d x)}{(d f - c g) (a+b x)} \right]^2 + \right. \\
 & A^2 \operatorname{Log} [f+g x] - 4 A B \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [f+g x] + 4 B^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} [f+g x] + \\
 & 4 A B \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [f+g x] - 8 B^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [f+g x] + \\
 & 4 B^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \operatorname{Log} [f+g x] + 2 A B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \operatorname{Log} [f+g x] - \\
 & 4 B^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \operatorname{Log} [f+g x] + 4 B^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \operatorname{Log} [f+g x] + \\
 & B^2 \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right]^2 \operatorname{Log} [f+g x] + 4 A B \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (f+g x)}{b f - a g} \right] - \\
 & 4 B^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} \left[\frac{b (f+g x)}{b f - a g} \right] + 4 B^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \operatorname{Log} \left[\frac{b (f+g x)}{b f - a g} \right] + \\
 & 8 B^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{g (c+d x)}{-d f + c g} \right] \operatorname{Log} \left[\frac{b (f+g x)}{b f - a g} \right] - 4 B^2 \operatorname{Log} \left[\frac{g (c+d x)}{-d f + c g} \right]^2 \operatorname{Log} \left[\frac{b (f+g x)}{b f - a g} \right] + \\
 & 8 B^2 \operatorname{Log} \left[\frac{g (c+d x)}{-d f + c g} \right] \operatorname{Log} \left[\frac{(b f - a g) (c+d x)}{(d f - c g) (a+b x)} \right] \operatorname{Log} \left[\frac{b (f+g x)}{b f - a g} \right] - \\
 & 4 B^2 \operatorname{Log} \left[\frac{(b f - a g) (c+d x)}{(d f - c g) (a+b x)} \right]^2 \operatorname{Log} \left[\frac{b (f+g x)}{b f - a g} \right] - 4 A B \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (f+g x)}{d f - c g} \right] + \\
 & 8 B^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (f+g x)}{d f - c g} \right] - 4 B^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \operatorname{Log} \left[\frac{d (f+g x)}{d f - c g} \right] - \\
 & 4 B^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \operatorname{Log} \left[\frac{d (f+g x)}{d f - c g} \right] - \\
 & 8 B^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{g (c+d x)}{-d f + c g} \right] \operatorname{Log} \left[\frac{d (f+g x)}{d f - c g} \right] + 4 B^2 \operatorname{Log} \left[\frac{g (c+d x)}{-d f + c g} \right]^2 \operatorname{Log} \left[\frac{d (f+g x)}{d f - c g} \right] - \\
 & 8 B^2 \operatorname{Log} \left[\frac{g (c+d x)}{-d f + c g} \right] \operatorname{Log} \left[\frac{(b f - a g) (c+d x)}{(d f - c g) (a+b x)} \right] \operatorname{Log} \left[\frac{d (f+g x)}{d f - c g} \right] +
 \end{aligned}$$

$$\begin{aligned}
 & 4 B^2 \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]^2 \operatorname{Log}\left[\frac{(-b c+a d)(f+g x)}{(d f-c g)(a+b x)}\right]+ \\
 & 4 B\left(A+B \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]+2 B \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]\right) \operatorname{PolyLog}\left[2, \frac{g(a+b x)}{-b f+a g}\right]- \\
 & 4 B\left(A+B \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]+2 B \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]\right) \operatorname{PolyLog}\left[2, \frac{g(c+d x)}{-d f+c g}\right]- \\
 & 8 B^2 \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]+ \\
 & 8 B^2 \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right] \operatorname{PolyLog}\left[2, \frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]+ \\
 & 8 B^2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{d(a+b x)}\right]-8 B^2 \operatorname{PolyLog}\left[3, \frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]
 \end{aligned}$$

Problem 277: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A+B \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]\right)^2}{(f+g x)^2} d x$$

Optimal (type 4, 200 leaves, 4 steps):

$$\frac{(a+b x)\left(A+B \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]\right)^2}{(b f-a g)(f+g x)}+\frac{4 B(b c-a d)\left(A+B \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]\right) \operatorname{Log}\left[1-\frac{(d f-c g)(a+b x)}{(b f-a g)(c+d x)}\right]}{(b f-a g)(d f-c g)}+ \\
 \frac{8 B^2(b c-a d) \operatorname{PolyLog}\left[2, \frac{(d f-c g)(a+b x)}{(b f-a g)(c+d x)}\right]}{(b f-a g)(d f-c g)}$$

Result (type 4, 3314 leaves):

$$\frac{1}{g(-b f+a g)(-d f+c g)(f+g x)} \\
 \left(-A^2 b d f^2+A^2 b c f g+a A^2 d f g-a A^2 c g^2+4 A b B d f^2 \operatorname{Log}\left[\frac{a}{b}+x\right]-4 A b B c f g \operatorname{Log}\left[\frac{a}{b}+x\right]+ \right. \\
 4 A b B d f g x \operatorname{Log}\left[\frac{a}{b}+x\right]-4 A b B c g^2 x \operatorname{Log}\left[\frac{a}{b}+x\right]-4 b B^2 d f^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2+ \\
 4 b B^2 c f g \operatorname{Log}\left[\frac{a}{b}+x\right]^2-4 b B^2 d f g x \operatorname{Log}\left[\frac{a}{b}+x\right]^2+4 b B^2 c g^2 x \operatorname{Log}\left[\frac{a}{b}+x\right]^2- \\
 4 A b B d f^2 \operatorname{Log}\left[\frac{c}{d}+x\right]+4 a A B d f g \operatorname{Log}\left[\frac{c}{d}+x\right]-4 A b B d f g x \operatorname{Log}\left[\frac{c}{d}+x\right]+ \\
 4 a A B d g^2 x \operatorname{Log}\left[\frac{c}{d}+x\right]+8 b B^2 d f^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right]-8 a B^2 d f g \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right]+ \\
 8 b B^2 d f g x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right]-8 a B^2 d g^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right]-4 b B^2 d f^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2+ \\
 \left. 4 a B^2 d f g \operatorname{Log}\left[\frac{c}{d}+x\right]^2-4 b B^2 d f g x \operatorname{Log}\left[\frac{c}{d}+x\right]^2+4 a B^2 d g^2 x \operatorname{Log}\left[\frac{c}{d}+x\right]^2\right)$$

$$\begin{aligned}
 & 2 A b B d f^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + 2 A b B c f g \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + 2 a A B d f g \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] - \\
 & 2 a A B c g^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + 4 b B^2 d f^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] - \\
 & 4 b B^2 c f g \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + 4 b B^2 d f g x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] - \\
 & 4 b B^2 c g^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] - 4 b B^2 d f^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + \\
 & 4 a B^2 d f g \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] - 4 b B^2 d f g x \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + \\
 & 4 a B^2 d g^2 x \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] - b B^2 d f^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]^2 + \\
 & b B^2 c f g \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]^2 + a B^2 d f g \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]^2 - a B^2 c g^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]^2 - \\
 & 8 b B^2 c f g \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] + 8 a B^2 d f g \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] - \\
 & 8 b B^2 c g^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] + 8 a B^2 d g^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] + \\
 & 4 b B^2 c f g \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right]^2 - 4 a B^2 d f g \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right]^2 + 4 b B^2 c g^2 x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right]^2 - \\
 & 4 a B^2 d g^2 x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right]^2 - 8 b B^2 c f g \operatorname{Log}\left[\frac{-b c+a d}{d(a+b x)}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right] + \\
 & 8 a B^2 d f g \operatorname{Log}\left[\frac{-b c+a d}{d(a+b x)}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right] - \\
 & 8 b B^2 c g^2 x \operatorname{Log}\left[\frac{-b c+a d}{d(a+b x)}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right] + \\
 & 8 a B^2 d g^2 x \operatorname{Log}\left[\frac{-b c+a d}{d(a+b x)}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right] - \\
 & 8 b B^2 c f g \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right] + \\
 & 8 a B^2 d f g \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right] - \\
 & 8 b B^2 c g^2 x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right] + \\
 & 8 a B^2 d g^2 x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right] + 4 b B^2 c f g \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]^2 -
 \end{aligned}$$

$$\begin{aligned}
 & 4 a B^2 d f g \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]^2+4 b B^2 c g^2 x \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]^2- \\
 & 4 a B^2 d g^2 x \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]^2-4 A b B d f^2 \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+ \\
 & 4 A b B c f g \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]-4 A b B d f g x \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+4 A b B c g^2 x \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+ \\
 & 8 b B^2 d f^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]-8 a B^2 d f g \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+ \\
 & 8 b B^2 d f g x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]-8 a B^2 d g^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]- \\
 & 4 b B^2 d f^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+4 b B^2 c f g \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]- \\
 & 4 b B^2 d f g x \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+4 b B^2 c g^2 x \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]- \\
 & 8 b B^2 d f^2 \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+8 b B^2 c f g \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]- \\
 & 8 b B^2 d f g x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+8 b B^2 c g^2 x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+ \\
 & 4 A b B d f^2 \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]-4 a A B d f g \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+4 A b B d f g x \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]- \\
 & 4 a A B d g^2 x \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]-8 b B^2 d f^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+ \\
 & 8 a B^2 d f g \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]-8 b B^2 d f g x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+ \\
 & 8 a B^2 d g^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+4 b B^2 d f^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]- \\
 & 4 a B^2 d f g \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+4 b B^2 d f g x \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]- \\
 & 4 a B^2 d g^2 x \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+8 b B^2 d f^2 \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]- \\
 & 8 b B^2 c f g \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+8 b B^2 d f g x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]- \\
 & 8 b B^2 c g^2 x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+8 B^2(b c-a d) g(f+g x) \\
 & \operatorname{PolyLog}\left[2, \frac{g(a+b x)}{-b f+a g}\right]-8 B^2(b c-a d) g(f+g x) \operatorname{PolyLog}\left[2, \frac{g(c+d x)}{-d f+c g}\right]- \\
 & 8 b B^2 c f g \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]+8 a B^2 d f g \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]-
 \end{aligned}$$

$$8 b B^2 c g^2 x \text{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right] + 8 a B^2 d g^2 x \text{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]$$

Problem 278: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \text{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]\right)^2}{(f+g x)^3} dx$$

Optimal (type 4, 381 leaves, 9 steps):

$$\begin{aligned} & \frac{2 B (b c - a d) g (a + b x) \left(A + B \text{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]\right)}{(b f - a g)^2 (d f - c g) (f + g x)} + \\ & \frac{b^2 \left(A + B \text{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]\right)^2}{2 g (b f - a g)^2} - \frac{\left(A + B \text{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]\right)^2}{2 g (f + g x)^2} + \frac{4 B^2 (b c - a d)^2 g \text{Log}\left[\frac{f+g x}{c+d x}\right]}{(b f - a g)^2 (d f - c g)^2} + \\ & \left(2 B (b c - a d) (2 b d f - b c g - a d g) \left(A + B \text{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]\right) \text{Log}\left[1 - \frac{(d f - c g)(a+b x)}{(b f - a g)(c+d x)}\right]\right) / \\ & \left((b f - a g)^2 (d f - c g)^2\right) + \frac{4 B^2 (b c - a d) (2 b d f - b c g - a d g) \text{PolyLog}\left[2, \frac{(d f - c g)(a+b x)}{(b f - a g)(c+d x)}\right]}{(b f - a g)^2 (d f - c g)^2} \end{aligned}$$

Result (type 4, 18290 leaves):

$$\begin{aligned} & -\frac{A^2}{2 g (f + g x)^2} + 2 A B \\ & \left(\frac{1}{g} \left(\frac{g \left(\frac{a}{b} + x\right)}{\left(-f + \frac{a g}{b}\right)^3 \left(1 - \frac{g \left(\frac{a}{b} + x\right)}{-f + \frac{a g}{b}}\right)} - \left(\frac{g^2 \left(\frac{a}{b} + x\right)^2}{\left(-f + \frac{a g}{b}\right)^4 \left(1 - \frac{g \left(\frac{a}{b} + x\right)}{-f + \frac{a g}{b}}\right)^2} + \frac{2 g \left(\frac{a}{b} + x\right)}{\left(-f + \frac{a g}{b}\right)^3 \left(1 - \frac{g \left(\frac{a}{b} + x\right)}{-f + \frac{a g}{b}}\right)} \right) \text{Log}\left[\frac{a}{b} + x\right] - \right. \\ & \left. \frac{\text{Log}\left[1 - \frac{g \left(\frac{a}{b} + x\right)}{-f + \frac{a g}{b}}\right]}{\left(-f + \frac{a g}{b}\right)^2} \right) - \frac{1}{g} \left(\frac{g \left(\frac{c}{d} + x\right)}{\left(-f + \frac{c g}{d}\right)^3 \left(1 - \frac{g \left(\frac{c}{d} + x\right)}{-f + \frac{c g}{d}}\right)} - \right. \\ & \left. \left(\frac{g^2 \left(\frac{c}{d} + x\right)^2}{\left(-f + \frac{c g}{d}\right)^4 \left(1 - \frac{g \left(\frac{c}{d} + x\right)}{-f + \frac{c g}{d}}\right)^2} + \frac{2 g \left(\frac{c}{d} + x\right)}{\left(-f + \frac{c g}{d}\right)^3 \left(1 - \frac{g \left(\frac{c}{d} + x\right)}{-f + \frac{c g}{d}}\right)} \right) \text{Log}\left[\frac{c}{d} + x\right] - \frac{\text{Log}\left[1 - \frac{g \left(\frac{c}{d} + x\right)}{-f + \frac{c g}{d}}\right]}{\left(-f + \frac{c g}{d}\right)^2} \right) - \\ & \left. \frac{-2 \text{Log}\left[\frac{a}{b} + x\right] + 2 \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a^2 e}{(c+d x)^2} + \frac{2 a b e x}{(c+d x)^2} + \frac{b^2 e x^2}{(c+d x)^2}\right]}{2 g (f + g x)^2} \right) + \end{aligned}$$

$$\begin{aligned}
 & B^2 \left(2 \left(\frac{1}{g} \left(\frac{g \left(\frac{a}{b} + x \right)}{\left(-f + \frac{ag}{b} \right)^3 \left(1 - \frac{g \left(\frac{a+x}{b} \right)}{-f + \frac{ag}{b}} \right)} - \left(\frac{g^2 \left(\frac{a}{b} + x \right)^2}{\left(-f + \frac{ag}{b} \right)^4 \left(1 - \frac{g \left(\frac{a+x}{b} \right)}{-f + \frac{ag}{b}} \right)^2} + \frac{2g \left(\frac{a}{b} + x \right)}{\left(-f + \frac{ag}{b} \right)^3 \left(1 - \frac{g \left(\frac{a+x}{b} \right)}{-f + \frac{ag}{b}} \right)} \right) \right. \\
 & \quad \left. \text{Log} \left[\frac{a}{b} + x \right] - \frac{\text{Log} \left[1 - \frac{g \left(\frac{a+x}{b} \right)}{-f + \frac{ag}{b}} \right]}{\left(-f + \frac{ag}{b} \right)^2} \right) - \frac{1}{g} \left(\frac{g \left(\frac{c}{d} + x \right)}{\left(-f + \frac{cg}{d} \right)^3 \left(1 - \frac{g \left(\frac{c+x}{d} \right)}{-f + \frac{cg}{d}} \right)} - \right. \\
 & \quad \left. \left(\frac{g^2 \left(\frac{c}{d} + x \right)^2}{\left(-f + \frac{cg}{d} \right)^4 \left(1 - \frac{g \left(\frac{c+x}{d} \right)}{-f + \frac{cg}{d}} \right)^2} + \frac{2g \left(\frac{c}{d} + x \right)}{\left(-f + \frac{cg}{d} \right)^3 \left(1 - \frac{g \left(\frac{c+x}{d} \right)}{-f + \frac{cg}{d}} \right)} \right) \text{Log} \left[\frac{c}{d} + x \right] - \frac{\text{Log} \left[1 - \frac{g \left(\frac{c+x}{d} \right)}{-f + \frac{cg}{d}} \right]}{\left(-f + \frac{cg}{d} \right)^2} \right) \right) \\
 & \quad \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + 2 \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a^2 e}{(c+dx)^2} + \frac{2abex}{(c+dx)^2} + \frac{b^2 ex^2}{(c+dx)^2} \right] \right) - \\
 & \quad \frac{\left(-2 \text{Log} \left[\frac{a}{b} + x \right] + 2 \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a^2 e}{(c+dx)^2} + \frac{2abex}{(c+dx)^2} + \frac{b^2 ex^2}{(c+dx)^2} \right] \right)^2}{2g(f+gx)^2} + \frac{1}{g} \\
 & \quad 4 \left(-\frac{1}{2} \left(\frac{g^2 \left(\frac{a}{b} + x \right)^2}{\left(-f + \frac{ag}{b} \right)^4 \left(1 - \frac{g \left(\frac{a+x}{b} \right)}{-f + \frac{ag}{b}} \right)^2} + \frac{2g \left(\frac{a}{b} + x \right)}{\left(-f + \frac{ag}{b} \right)^3 \left(1 - \frac{g \left(\frac{a+x}{b} \right)}{-f + \frac{ag}{b}} \right)} \right) \text{Log} \left[\frac{a}{b} + x \right]^2 + \frac{\text{Log} \left[1 - \frac{g \left(\frac{a+x}{b} \right)}{-f + \frac{ag}{b}} \right]}{\left(-f + \frac{ag}{b} \right)^2} + \right. \\
 & \quad \left. \text{Log} \left[\frac{a}{b} + x \right] \left(\frac{g \left(\frac{a}{b} + x \right)}{\left(-f + \frac{ag}{b} \right)^3 \left(1 - \frac{g \left(\frac{a+x}{b} \right)}{-f + \frac{ag}{b}} \right)} - \frac{\text{Log} \left[1 - \frac{g \left(\frac{a+x}{b} \right)}{-f + \frac{ag}{b}} \right]}{\left(-f + \frac{ag}{b} \right)^2} - \frac{\text{PolyLog} \left[2, \frac{g \left(\frac{a+x}{b} \right)}{-f + \frac{ag}{b}} \right]}{\left(-f + \frac{ag}{b} \right)^2} \right) + \frac{1}{g} \right. \\
 & \quad \left. 4 \left(-\frac{1}{2} \left(\frac{g^2 \left(\frac{c}{d} + x \right)^2}{\left(-f + \frac{cg}{d} \right)^4 \left(1 - \frac{g \left(\frac{c+x}{d} \right)}{-f + \frac{cg}{d}} \right)^2} + \frac{2g \left(\frac{c}{d} + x \right)}{\left(-f + \frac{cg}{d} \right)^3 \left(1 - \frac{g \left(\frac{c+x}{d} \right)}{-f + \frac{cg}{d}} \right)} \right) \text{Log} \left[\frac{c}{d} + x \right]^2 + \frac{\text{Log} \left[1 - \frac{g \left(\frac{c+x}{d} \right)}{-f + \frac{cg}{d}} \right]}{\left(-f + \frac{cg}{d} \right)^2} + \right. \\
 & \quad \left. \text{Log} \left[\frac{c}{d} + x \right] \left(\frac{g \left(\frac{c}{d} + x \right)}{\left(-f + \frac{cg}{d} \right)^3 \left(1 - \frac{g \left(\frac{c+x}{d} \right)}{-f + \frac{cg}{d}} \right)} - \frac{\text{Log} \left[1 - \frac{g \left(\frac{c+x}{d} \right)}{-f + \frac{cg}{d}} \right]}{\left(-f + \frac{cg}{d} \right)^2} - \frac{\text{PolyLog} \left[2, \frac{g \left(\frac{c+x}{d} \right)}{-f + \frac{cg}{d}} \right]}{\left(-f + \frac{cg}{d} \right)^2} \right) - \right. \\
 & \quad \left. \frac{1}{f^2} 4 \left(\frac{1}{g} 2 \left(\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] + \frac{1}{2} \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \right) \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{Log}\left[\frac{d g\left(\frac{c}{d}+x\right)}{-d f+c g}\right]\right)\left(\text{Log}\left[\frac{b(f+g x)}{b f-a g}\right]-\text{Log}\left[-\frac{d(f+g x)}{-d f+c g}\right]\right)+\text{Log}\left[\frac{d g\left(\frac{c}{d}+x\right)}{-d f+c g}\right] \\
 & \text{Log}\left[-\frac{d(b f-a g)\left(\frac{c}{d}+x\right)}{b(-d f+c g)\left(\frac{a}{b}+x\right)}\right]\left(-\text{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+\text{Log}\left[-\frac{d(f+g x)}{-d f+c g}\right]\right)+ \\
 & \frac{1}{2} \text{Log}\left[-\frac{d(b f-a g)\left(\frac{c}{d}+x\right)}{b(-d f+c g)\left(\frac{a}{b}+x\right)}\right]^2\left(\text{Log}\left[\frac{-b c+a d}{b d\left(\frac{a}{b}+x\right)}\right]+\text{Log}\left[\frac{b(f+g x)}{b f-a g}\right]-\text{Log}\left[\right. \right. \\
 & \left. \left. -\frac{(-b c+a d)(f+g x)}{b(-d f+c g)\left(\frac{a}{b}+x\right)}\right]\right)+\left(\text{Log}\left[\frac{c}{d}+x\right]-\text{Log}\left[-\frac{d(b f-a g)\left(\frac{c}{d}+x\right)}{b(-d f+c g)\left(\frac{a}{b}+x\right)}\right]\right) \\
 & \text{PolyLog}\left[2,-\frac{b g\left(\frac{a}{b}+x\right)}{b f-a g}\right]+\left(\text{Log}\left[\frac{a}{b}+x\right]+\text{Log}\left[-\frac{d(b f-a g)\left(\frac{c}{d}+x\right)}{b(-d f+c g)\left(\frac{a}{b}+x\right)}\right]\right) \\
 & \text{PolyLog}\left[2,\frac{d g\left(\frac{c}{d}+x\right)}{-d f+c g}\right]+\text{Log}\left[-\frac{d(b f-a g)\left(\frac{c}{d}+x\right)}{b(-d f+c g)\left(\frac{a}{b}+x\right)}\right]\left(\text{PolyLog}\left[2,\right. \right. \\
 & \left. \left.\frac{\frac{c}{d}+x}{\frac{a}{b}+x}\right]-\text{PolyLog}\left[2,-\frac{d(b f-a g)\left(\frac{c}{d}+x\right)}{b(-d f+c g)\left(\frac{a}{b}+x\right)}\right]\right)-\text{PolyLog}\left[3,-\frac{b g\left(\frac{a}{b}+x\right)}{b f-a g}\right]- \\
 & \text{PolyLog}\left[3,\frac{d g\left(\frac{c}{d}+x\right)}{-d f+c g}\right]-\text{PolyLog}\left[3,\frac{\frac{c}{d}+x}{\frac{a}{b}+x}\right]+\text{PolyLog}\left[3,-\frac{d(b f-a g)\left(\frac{c}{d}+x\right)}{b(-d f+c g)\left(\frac{a}{b}+x\right)}\right]\right)+ \\
 & g^2\left(\frac{1}{g}\left(\left(\frac{(b f-a g)\left(\frac{2 a b x}{(b f-a g)^2}+\frac{2 a^2 b(f+g x)}{(b f-a g)^3}\right)}{b(f+g x)}-\frac{(b f-a g) x\left(\frac{b x}{b f-a g}+\frac{a b(f+g x)}{(b f-a g)^2}\right)}{b(f+g x)^2}\right. \right. \right. \\
 & \left. \left. \frac{a\left(\frac{b x}{b f-a g}+\frac{a b(f+g x)}{(b f-a g)^2}\right)}{b(f+g x)}\right)\right)\text{Log}\left[\frac{a}{b}+x\right]\text{Log}\left[\frac{c}{d}+x\right]- \\
 & \left(2 b(-d f+c g)\left(\frac{a}{b}+x\right)\left(\frac{c d(b f-a g)\left(\frac{c}{d}+x\right)}{b(-d f+c g)^2\left(\frac{a}{b}+x\right)}+\frac{a d\left(\frac{c}{d}+x\right)}{b(-d f+c g)\left(\frac{a}{b}+x\right)}\right) \right. \\
 & \left(\frac{(b f-a g)\left(\frac{b x}{b f-a g}+\frac{a b(f+g x)}{(b f-a g)^2}\right)}{b(f+g x)}+\left(b(-d f+c g)\left(\frac{a}{b}+x\right)\right. \right. \\
 & \left. \left(-\frac{(-b c+a d) x}{b(-d f+c g)\left(\frac{a}{b}+x\right)}+\frac{c(-b c+a d)(f+g x)}{b(-d f+c g)^2\left(\frac{a}{b}+x\right)}\right)\right) /((-b c+a d)
 \end{aligned}$$

$$\begin{aligned}
& (f+gx) \Bigg) \log \left[-\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)} \right] \Bigg/ \left(d(bf-ag)\left(\frac{c}{d}+x\right) \right) + \\
& \left(-\frac{(bf-ag)\left(\frac{2abx}{(bf-ag)^2} + \frac{2a^2b(f+gx)}{(bf-ag)^3}\right)}{b(f+gx)} + \frac{(bf-ag)x\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)^2} + \right. \\
& \left. \frac{a\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)} - \frac{(-df+cg)\left(\frac{2cdx}{(-df+cg)^2} - \frac{2c^2d(f+gx)}{(-df+cg)^3}\right)}{d(f+gx)} + \right. \\
& \left. \frac{(-df+cg)x\left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2}\right)}{d(f+gx)^2} - \frac{c\left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2}\right)}{d(f+gx)} \right) \log \left[\frac{dg\left(\frac{c}{d}+x\right)}{-df+cg} \right] \\
& \log \left[-\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)} \right] + \frac{1}{2} \left(\frac{(bf-ag)\left(\frac{2abx}{(bf-ag)^2} + \frac{2a^2b(f+gx)}{(bf-ag)^3}\right)}{b(f+gx)} - \right. \\
& \left. \frac{(bf-ag)x\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)^2} - \frac{a\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)} + \right. \\
& \left(b(-df+cg)\left(\frac{a}{b}+x\right) \left(\frac{2c(-bc+ad)x}{b(-df+cg)^2\left(\frac{a}{b}+x\right)} - \frac{2c^2(-bc+ad)(f+gx)}{b(-df+cg)^3\left(\frac{a}{b}+x\right)} \right) \right) \Bigg/ \\
& \left((-bc+ad)(f+gx) \right) - \left(b(-df+cg)x\left(\frac{a}{b}+x\right) \left(-\frac{(-bc+ad)x}{b(-df+cg)\left(\frac{a}{b}+x\right)} + \right. \right. \\
& \left. \left. \frac{c(-bc+ad)(f+gx)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)} \right) \right) \Bigg/ \left((-bc+ad)(f+gx)^2 \right) + \\
& \left. \frac{bc\left(\frac{a}{b}+x\right) \left(-\frac{(-bc+ad)x}{b(-df+cg)\left(\frac{a}{b}+x\right)} + \frac{c(-bc+ad)(f+gx)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)} \right)}{(-bc+ad)(f+gx)} \right) \log \left[-\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)} \right]^2 + \\
& 2 \left(-\frac{(bf-ag)\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)} - \frac{(-df+cg)\left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2}\right)}{d(f+gx)} \right) \\
& \left(-\left(\left(b(-df+cg)\left(\frac{a}{b}+x\right) \left(\frac{cd(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)} + \frac{ad\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)} \right) \right) \right. \right. \\
& \left. \left. \log \left[\frac{dg\left(\frac{c}{d}+x\right)}{-df+cg} \right] \right) \Bigg/ \left(d(bf-ag)\left(\frac{c}{d}+x\right) \right) \right) + \frac{1}{dg\left(\frac{c}{d}+x\right)}
\end{aligned}$$

$$\begin{aligned}
 & (-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g} \right) \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] + \\
 & \frac{1}{d g \left(\frac{c}{d} + x\right)} (-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g} \right) \\
 & \left(\left(\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2}\right)}{b (f + g x)} + \frac{(-d f + c g) \left(-\frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2}\right)}{d (f + g x)} \right) \right. \\
 & \left. \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right] \right) + \frac{1}{d g \left(\frac{c}{d} + x\right)} (-d f + c g) \right. \\
 & \left. \left(-\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g} \right) \left(\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) \right) + \\
 & \frac{1}{2} \text{Log} \left[\frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right] \left(\frac{1}{d g \left(\frac{c}{d} + x\right)} 2 (-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g} \right) \right. \\
 & \left. \left(\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2}\right)}{b (f + g x)} + \frac{(-d f + c g) \left(-\frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2}\right)}{d (f + g x)} \right) \right) + \\
 & \left(\frac{(b f - a g) \left(\frac{2 a b x}{(b f - a g)^2} + \frac{2 a^2 b (f + g x)}{(b f - a g)^3}\right)}{b (f + g x)} - \frac{(b f - a g) x \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2}\right)}{b (f + g x)^2} - \right. \\
 & \frac{a \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2}\right)}{b (f + g x)} + \frac{(-d f + c g) \left(\frac{2 c d x}{(-d f + c g)^2} - \frac{2 c^2 d (f + g x)}{(-d f + c g)^3}\right)}{d (f + g x)} - \\
 & \left. \frac{(-d f + c g) x \left(-\frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2}\right)}{d (f + g x)^2} + \frac{c \left(-\frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2}\right)}{d (f + g x)} \right) \\
 & \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right] \right) + \left(\frac{(-d f + c g) \left(\frac{2 c^2 d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^3} - \frac{2 c d \left(\frac{c}{d} + x\right)}{(-d f + c g)^2}\right)}{d g \left(\frac{c}{d} + x\right)} \right) + \\
 & \left. \frac{c \left(-\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g}\right)}{d g \left(\frac{c}{d} + x\right)} - \frac{(-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g}\right)}{d g^2 \left(\frac{c}{d} + x\right)} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(\text{Log} \left[\frac{b(f+g x)}{b f - a g} \right] - \text{Log} \left[-\frac{d(f+g x)}{-d f + c g} \right] \right) + \\
 & \frac{1}{2} \left(\frac{(-d f + c g) \left(\frac{2 c^2 d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^3} - \frac{2 c d \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} \right)}{d g \left(\frac{c}{d} + x \right)} + \frac{c \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right)}{d g \left(\frac{c}{d} + x \right)} - \right. \\
 & \left. \frac{(-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right)}{d g^2 \left(\frac{c}{d} + x \right)} \right) \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \right. \\
 & \left. \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right) \left(\text{Log} \left[\frac{b(f+g x)}{b f - a g} \right] - \text{Log} \left[-\frac{d(f+g x)}{-d f + c g} \right] \right) + \\
 & \left(- \left(\left(2 b (-d f + c g)^2 \left(\frac{a}{b} + x \right) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \right. \right. \right. \\
 & \left. \left. \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right) / \left(d^2 g (b f - a g) \left(\frac{c}{d} + x \right)^2 \right) \right) + \\
 & \left(- \left(\left(b (-d f + c g) \left(\frac{a}{b} + x \right) \left(-\frac{2 c^2 d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^3 \left(\frac{a}{b} + x \right)} - \right. \right. \right. \right. \\
 & \left. \left. \frac{2 a c d \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right) \right) / \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) \right) - \\
 & \frac{b c \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right)}{d (b f - a g) \left(\frac{c}{d} + x \right)} - \left(a b (-d f + c g) \left(\frac{a}{b} + x \right) \right. \\
 & \left. \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right) / \left(d (b f - a g)^2 \right. \\
 & \left. \left(\frac{c}{d} + x \right) \right) \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] + \left(\frac{(-d f + c g) \left(\frac{2 c^2 d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^3} - \frac{2 c d \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} \right)}{d g \left(\frac{c}{d} + x \right)} + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{c \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right)}{d g \left(\frac{c}{d} + x \right)} - \frac{(-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right)}{d g^2 \left(\frac{c}{d} + x \right)} \right) \\
 & \left. \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) \left(-\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] + \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) + \\
 & \frac{1}{2} \left(\left(2 b^2 (-d f + c g)^2 \left(\frac{a}{b} + x \right)^2 \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right)^2 \right) / \right. \\
 & \left. \left(d^2 (b f - a g)^2 \left(\frac{c}{d} + x \right)^2 \right) - \right. \\
 & \left. \left(2 b (-d f + c g) \left(\frac{a}{b} + x \right) \left(-\frac{2 c^2 d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^3 \left(\frac{a}{b} + x \right)} - \frac{2 a c d \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right) \right) \right. \\
 & \left. \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) - \\
 & \left(2 b c \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right. \\
 & \left. \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) - \\
 & \left(2 a b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right. \\
 & \left. \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) / \left(d (b f - a g)^2 \left(\frac{c}{d} + x \right) \right) \right) \\
 & \left(\text{Log} \left[\frac{-b c + a d}{b d \left(\frac{a}{b} + x \right)} \right] + \text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \text{Log} \left[-\frac{(-b c + a d) (f + g x)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) + \\
 & \frac{(b f - a g)^2 \left(-\frac{a b g \left(\frac{a}{b} + x \right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x \right)}{b f - a g} \right)^2 \text{Log} \left[1 + \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right]}{b^2 g^2 \left(\frac{a}{b} + x \right)^2} + \frac{1}{d g \left(\frac{c}{d} + x \right)} 2 (-d f + c g) \\
 & \left(-\frac{a b g \left(\frac{a}{b} + x \right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x \right)}{b f - a g} \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \text{Log} [
 \end{aligned}$$

$$\begin{aligned}
 & \left. 1 + \frac{b g \left(\frac{a}{b} + x\right)}{b f - a g} \right] + \left(\text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[- \frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \right) \left((b f - a g) \right. \\
 & \left. \left(- \frac{a b g \left(\frac{a}{b} + x\right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x\right)}{b f - a g} \right) \left(\frac{a b g \left(\frac{a}{b} + x\right)}{(b f - a g)^2} + \frac{b \left(\frac{a}{b} + x\right)}{b f - a g} \right) \right) / \left(b g \left(\frac{a}{b} + x\right) \right. \\
 & \left. \left(1 + \frac{b g \left(\frac{a}{b} + x\right)}{b f - a g} \right) \right) + \frac{1}{b g \left(\frac{a}{b} + x\right)} (b f - a g) \left(- \frac{2 a^2 b g \left(\frac{a}{b} + x\right)}{(b f - a g)^3} - \frac{2 a b \left(\frac{a}{b} + x\right)}{(b f - a g)^2} \right) \\
 & \text{Log} \left[1 + \frac{b g \left(\frac{a}{b} + x\right)}{b f - a g} \right] - \frac{a \left(- \frac{a b g \left(\frac{a}{b} + x\right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x\right)}{b f - a g} \right) \text{Log} \left[1 + \frac{b g \left(\frac{a}{b} + x\right)}{b f - a g} \right]}{b g \left(\frac{a}{b} + x\right)} - \\
 & \left. \frac{(b f - a g) \left(- \frac{a b g \left(\frac{a}{b} + x\right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x\right)}{b f - a g} \right) \text{Log} \left[1 + \frac{b g \left(\frac{a}{b} + x\right)}{b f - a g} \right]}{b g^2 \left(\frac{a}{b} + x\right)} \right) + \\
 & \frac{(-d f + c g)^2 \left(- \frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g} \right)^2 \text{Log} \left[1 - \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right]}{d^2 g^2 \left(\frac{c}{d} + x\right)^2} + \\
 & \left(2 b (-d f + c g)^2 \left(\frac{a}{b} + x\right) \left(- \frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g} \right) \right. \\
 & \left. \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \text{Log} \left[1 - \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right] \right) / \\
 & \left(d^2 g (b f - a g) \left(\frac{c}{d} + x\right)^2 \right) + \left(\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[- \frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \right) \\
 & \left(- \left(\left((-d f + c g) \left(\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} - \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g} \right) \left(- \frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g} \right) \right) \right) / \\
 & \left(d g \left(\frac{c}{d} + x\right) \left(1 - \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right) \right) \right) - \frac{1}{d g \left(\frac{c}{d} + x\right)} \\
 & (-d f + c g) \left(\frac{2 c^2 d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^3} - \frac{2 c d \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} \right) \text{Log} \left[1 - \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right] -
 \end{aligned}$$

$$\begin{aligned}
 & \frac{c \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \text{Log} \left[1 - \frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right]}{d g \left(\frac{c}{d} + x \right)} + \\
 & \left. \frac{(-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \text{Log} \left[1 - \frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right]}{d g^2 \left(\frac{c}{d} + x \right)} \right\} + \\
 & \left(b^2 (-d f + c g)^2 \left(\frac{a}{b} + x \right)^2 \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right)^2 \right. \\
 & \left. \text{Log} \left[1 + \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) / \left(d^2 (b f - a g)^2 \right. \\
 & \left. \left(\frac{c}{d} + x \right)^2 \right) + \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \\
 & \left(-\left(\left(b (-d f + c g) \left(\frac{a}{b} + x \right) \left(-\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} - \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right. \right. \right. \\
 & \left. \left. \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right) \right) / \\
 & \left(d (b f - a g) \left(\frac{c}{d} + x \right) \left(1 + \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right) \right) - \\
 & \left(b (-d f + c g) \left(\frac{a}{b} + x \right) \left(-\frac{2 c^2 d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^3 \left(\frac{a}{b} + x \right)} - \frac{2 a c d \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right) \right. \\
 & \left. \text{Log} \left[1 + \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) - \\
 & \left(b c \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right. \\
 & \left. \text{Log} \left[1 + \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) - \\
 & \left(a b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left(\frac{\text{Log}\left[1 + \frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right]}{d(bf-ag)^2\left(\frac{c}{d}+x\right)} + \frac{1}{bg\left(\frac{a}{b}+x\right)} \right) \right) \\
 & (bf-ag) \left(-\frac{2a^2bg\left(\frac{a}{b}+x\right)}{(bf-ag)^3} - \frac{2ab\left(\frac{a}{b}+x\right)}{(bf-ag)^2} \right) \text{PolyLog}\left[2, -\frac{bg\left(\frac{a}{b}+x\right)}{bf-ag}\right] - \\
 & \frac{a \left(-\frac{abg\left(\frac{a}{b}+x\right)}{(bf-ag)^2} - \frac{b\left(\frac{a}{b}+x\right)}{bf-ag} \right) \text{PolyLog}\left[2, -\frac{bg\left(\frac{a}{b}+x\right)}{bf-ag}\right]}{bg\left(\frac{a}{b}+x\right)} - \frac{1}{bg^2\left(\frac{a}{b}+x\right)} \\
 & (bf-ag) \left(-\frac{abg\left(\frac{a}{b}+x\right)}{(bf-ag)^2} - \frac{b\left(\frac{a}{b}+x\right)}{bf-ag} \right) \text{PolyLog}\left[2, -\frac{bg\left(\frac{a}{b}+x\right)}{bf-ag}\right] + \\
 & \left(\left(b(-df+cg)\left(\frac{a}{b}+x\right) \left(-\frac{2c^2d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)^3\left(\frac{a}{b}+x\right)} - \frac{2acd\left(\frac{c}{d}+x\right)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)} \right) \right) \right) \\
 & \left(d(bf-ag)\left(\frac{c}{d}+x\right) + \frac{bc\left(\frac{a}{b}+x\right) \left(\frac{cd(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)} + \frac{ad\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)} \right)}{d(bf-ag)\left(\frac{c}{d}+x\right)} + \right. \\
 & \left. \left(ab(-df+cg)\left(\frac{a}{b}+x\right) \left(\frac{cd(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)} + \frac{ad\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)} \right) \right) \right) \\
 & \left(d(bf-ag)^2\left(\frac{c}{d}+x\right) \right) \text{PolyLog}\left[2, -\frac{bg\left(\frac{a}{b}+x\right)}{bf-ag}\right] - \frac{1}{dg\left(\frac{c}{d}+x\right)} \\
 & (-df+cg) \left(\frac{2c^2dg\left(\frac{c}{d}+x\right)}{(-df+cg)^3} - \frac{2cd\left(\frac{c}{d}+x\right)}{(-df+cg)^2} \right) \text{PolyLog}\left[2, \frac{dg\left(\frac{c}{d}+x\right)}{-df+cg}\right] - \\
 & \frac{c \left(-\frac{cdg\left(\frac{c}{d}+x\right)}{(-df+cg)^2} + \frac{d\left(\frac{c}{d}+x\right)}{-df+cg} \right) \text{PolyLog}\left[2, \frac{dg\left(\frac{c}{d}+x\right)}{-df+cg}\right]}{dg\left(\frac{c}{d}+x\right)} + \frac{1}{dg^2\left(\frac{c}{d}+x\right)} \\
 & (-df+cg) \left(-\frac{cdg\left(\frac{c}{d}+x\right)}{(-df+cg)^2} + \frac{d\left(\frac{c}{d}+x\right)}{-df+cg} \right) \text{PolyLog}\left[2, \frac{dg\left(\frac{c}{d}+x\right)}{-df+cg}\right] + \\
 & \left(-\left(\left(b(-df+cg)\left(\frac{a}{b}+x\right) \left(-\frac{2c^2d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)^3\left(\frac{a}{b}+x\right)} - \frac{2acd\left(\frac{c}{d}+x\right)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)} \right) \right) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) - \frac{b c \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right)}{d (b f - a g) \left(\frac{c}{d} + x \right)} - \\
 & \left(a b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right) / \\
 & \left(d (b f - a g)^2 \left(\frac{c}{d} + x \right) \right) \text{PolyLog}\left[2, \frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g}\right] + \\
 & \left(- \left(\left(b (-d f + c g) \left(\frac{a}{b} + x \right) \left(- \frac{2 c^2 d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^3 \left(\frac{a}{b} + x \right)} - \frac{2 a c d \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right) \right) \right) / \right. \\
 & \left. \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) - \frac{b c \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right)}{d (b f - a g) \left(\frac{c}{d} + x \right)} - \right. \\
 & \left. \left(a b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right) \right) / \\
 & \left(d (b f - a g)^2 \left(\frac{c}{d} + x \right) \right) \right) \\
 & \left(\text{PolyLog}\left[2, \frac{c}{b} + x\right] - \text{PolyLog}\left[2, - \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) - \\
 & \left(b (-d f + c g) \left(\frac{a}{b} + x \right) \left(- \frac{2 c^2 d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^3 \left(\frac{a}{b} + x \right)} - \frac{2 a c d \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right) \right. \\
 & \left. \text{PolyLog}\left[2, - \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) - \\
 & \left(b c \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right. \\
 & \left. \text{PolyLog}\left[2, - \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x \right) \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left(a b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right. \\
 & \quad \left. \text{PolyLog}\left[2, -\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)}\right] \right) / \left(d (b f - a g)^2 \left(\frac{c}{d} + x \right) \right) - \\
 & \frac{1}{g^2} 2 \left(\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right) \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right]}{b (f + g x)} + \frac{1}{2} \right. \\
 & \quad \left(\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right)}{b (f + g x)} + \frac{(-d f + c g) \left(-\frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2} \right)}{d (f + g x)} \right) \\
 & \quad \text{Log}\left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g}\right] \left(-2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g}\right] \right) + \\
 & \quad \left(-\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right)}{b (f + g x)} - \frac{(-d f + c g) \left(-\frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2} \right)}{d (f + g x)} \right) \text{Log}\left[\right. \\
 & \quad \left. \frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \text{Log}\left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] + \frac{1}{2} \left(\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right)}{b (f + g x)} + \right. \\
 & \quad \left. \left(b (-d f + c g) \left(\frac{a}{b} + x \right) \left(-\frac{(-b c + a d) x}{b (-d f + c g) \left(\frac{a}{b} + x \right)} + \frac{c (-b c + a d) (f + g x)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right) \right) / \right. \\
 & \quad \left. \left((-b c + a d) (f + g x) \right) \right) \text{Log}\left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right]^2 + \\
 & \quad \frac{1}{2 d g \left(\frac{c}{d} + x \right)} (-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \text{Log}\left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \\
 & \quad \left(\text{Log}\left[\frac{b (f + g x)}{b f - a g}\right] - \text{Log}\left[-\frac{d (f + g x)}{-d f + c g}\right] \right) + \frac{1}{2 d g \left(\frac{c}{d} + x \right)} (-d f + c g) \\
 & \quad \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \left(-2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g}\right] \right) \\
 & \quad \left(\text{Log}\left[\frac{b (f + g x)}{b f - a g}\right] - \text{Log}\left[-\frac{d (f + g x)}{-d f + c g}\right] \right) - \left(b (-d f + c g) \left(\frac{a}{b} + x \right) \right. \\
 & \quad \left. \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \text{Log}\left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(-\text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + \text{Log}\left[-\frac{d(f+gx)}{-df+cg}\right] \right) / \left(d(bf-ag) \left(\frac{c}{d}+x\right) \right) + \\
 & \frac{1}{dg\left(\frac{c}{d}+x\right)} (-df+cg) \left(-\frac{cdg\left(\frac{c}{d}+x\right)}{(-df+cg)^2} + \frac{d\left(\frac{c}{d}+x\right)}{-df+cg} \right) \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right] \\
 & \left(-\text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + \text{Log}\left[-\frac{d(f+gx)}{-df+cg}\right] \right) - \left(b(-df+cg) \left(\frac{a}{b}+x\right) \right. \\
 & \left. \left(\frac{cd(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)} + \frac{ad\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)} \right) \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right] \right. \\
 & \left. \left(\text{Log}\left[\frac{-bc+ad}{bd\left(\frac{a}{b}+x\right)}\right] + \text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - \text{Log}\left[-\frac{(-bc+ad)(f+gx)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right] \right) \right) / \\
 & \left(d(bf-ag) \left(\frac{c}{d}+x\right) \right) + \frac{1}{bg\left(\frac{a}{b}+x\right)} (bf-ag) \left(-\frac{abg\left(\frac{a}{b}+x\right)}{(bf-ag)^2} - \frac{b\left(\frac{a}{b}+x\right)}{bf-ag} \right) \\
 & \left(\text{Log}\left[\frac{c}{d}+x\right] - \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right] \right) \text{Log}\left[1 + \frac{bg\left(\frac{a}{b}+x\right)}{bf-ag}\right] - \\
 & \frac{1}{dg\left(\frac{c}{d}+x\right)} (-df+cg) \left(-\frac{cdg\left(\frac{c}{d}+x\right)}{(-df+cg)^2} + \frac{d\left(\frac{c}{d}+x\right)}{-df+cg} \right) \left(\text{Log}\left[\frac{a}{b}+x\right] + \right. \\
 & \left. \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right] \right) \text{Log}\left[1 - \frac{dg\left(\frac{c}{d}+x\right)}{-df+cg}\right] - \left(b(-df+cg) \left(\frac{a}{b}+x\right) \right. \\
 & \left. \left(\frac{cd(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)} + \frac{ad\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)} \right) \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right] \right. \\
 & \left. \text{Log}\left[1 + \frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right] \right) / \left(d(bf-ag) \left(\frac{c}{d}+x\right) \right) + \frac{1}{bg\left(\frac{a}{b}+x\right)} \\
 & (bf-ag) \left(-\frac{abg\left(\frac{a}{b}+x\right)}{(bf-ag)^2} - \frac{b\left(\frac{a}{b}+x\right)}{bf-ag} \right) \text{PolyLog}\left[2, -\frac{bg\left(\frac{a}{b}+x\right)}{bf-ag}\right] + \\
 & \left(b(-df+cg) \left(\frac{a}{b}+x\right) \left(\frac{cd(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)} + \frac{ad\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)} \right) \right. \\
 & \left. \text{PolyLog}\left[2, -\frac{bg\left(\frac{a}{b}+x\right)}{bf-ag}\right] \right) / \left(d(bf-ag) \left(\frac{c}{d}+x\right) \right) - \frac{1}{dg\left(\frac{c}{d}+x\right)}
 \end{aligned}$$

$$\begin{aligned}
 & (-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g} \right) \text{PolyLog}\left[2, \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g}\right] - \\
 & \left(b (-d f + c g) \left(\frac{a}{b} + x\right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \right. \\
 & \left. \text{PolyLog}\left[2, \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g}\right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x\right) \right) - \left(b (-d f + c g) \left(\frac{a}{b} + x\right) \right. \\
 & \left. \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \left(\text{PolyLog}\left[2, \frac{\frac{c}{d} + x}{\frac{a}{b} + x}\right] - \right. \right. \\
 & \left. \left. \text{PolyLog}\left[2, -\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \right) \right) / \left(d (b f - a g) \left(\frac{c}{d} + x\right) \right) - \\
 & \left(b (-d f + c g) \left(\frac{a}{b} + x\right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \right. \\
 & \left. \text{PolyLog}\left[2, -\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \right) / \left(d (b f - a g) \left(\frac{c}{d} + x\right) \right) \Bigg) + \\
 & \frac{1}{g^3} 2 \left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{b (f + g x)}{b f - a g}\right] + \frac{1}{2} \text{Log}\left[\frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g}\right] \right. \\
 & \left. \left(-2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g}\right] \right) \left(\text{Log}\left[\frac{b (f + g x)}{b f - a g}\right] - \text{Log}\left[-\frac{d (f + g x)}{-d f + c g}\right] \right) + \right. \\
 & \left. \text{Log}\left[\frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g}\right] \text{Log}\left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \right. \\
 & \left. \left(-\text{Log}\left[\frac{b (f + g x)}{b f - a g}\right] + \text{Log}\left[-\frac{d (f + g x)}{-d f + c g}\right] \right) + \frac{1}{2} \text{Log}\left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right]^2 \right. \\
 & \left. \left(\text{Log}\left[\frac{-b c + a d}{b d \left(\frac{a}{b} + x\right)}\right] + \text{Log}\left[\frac{b (f + g x)}{b f - a g}\right] - \text{Log}\left[-\frac{(-b c + a d) (f + g x)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \right) + \right. \\
 & \left. \left(\text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \right) \text{PolyLog}\left[2, -\frac{b g \left(\frac{a}{b} + x\right)}{b f - a g}\right] + \right. \\
 & \left. \left(\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \right) \text{PolyLog}\left[2, \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g}\right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \begin{aligned}
 & \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right] \left(\text{PolyLog}\left[2, \frac{\frac{c}{d}+x}{\frac{a}{b}+x}\right] - \right. \\
 & \left. \text{PolyLog}\left[2, -\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right] - \text{PolyLog}\left[3, -\frac{bg\left(\frac{a}{b}+x\right)}{bf-ag}\right] - \text{PolyLog}\left[3, \right. \right. \\
 & \left. \left. \frac{dg\left(\frac{c}{d}+x\right)}{-df+cg}\right] - \text{PolyLog}\left[3, \frac{\frac{c}{d}+x}{\frac{a}{b}+x}\right] + \text{PolyLog}\left[3, -\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right] \right) \right) + \\
 4g & \left(\frac{1}{g} \left(\frac{(bf-ag)\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right) \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{c}{d}+x\right]}{b(f+gx)} + \right. \right. \\
 & \left. \frac{1}{2} \left(\frac{(bf-ag)\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)} + \frac{(-df+cg)\left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2}\right)}{d(f+gx)} \right) \right) \\
 & \text{Log}\left[\frac{dg\left(\frac{c}{d}+x\right)}{-df+cg}\right] \left(-2 \text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{dg\left(\frac{c}{d}+x\right)}{-df+cg}\right] \right) + \\
 & \left(-\frac{(bf-ag)\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)} - \frac{(-df+cg)\left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2}\right)}{d(f+gx)} \right) \text{Log}\left[\right. \\
 & \left. \frac{dg\left(\frac{c}{d}+x\right)}{-df+cg}\right] \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right] + \frac{1}{2} \left(\frac{(bf-ag)\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)} + \right. \\
 & \left. \left(b(-df+cg)\left(\frac{a}{b}+x\right) \left(-\frac{(-bc+ad)x}{b(-df+cg)\left(\frac{a}{b}+x\right)} + \frac{c(-bc+ad)(f+gx)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)} \right) \right) \right) / \\
 & \left. \left((-bc+ad)(f+gx) \right) \right) \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right]^2 + \\
 & \frac{1}{2dg\left(\frac{c}{d}+x\right)} (-df+cg) \left(-\frac{cdg\left(\frac{c}{d}+x\right)}{(-df+cg)^2} + \frac{d\left(\frac{c}{d}+x\right)}{-df+cg} \right) \text{Log}\left[\frac{dg\left(\frac{c}{d}+x\right)}{-df+cg}\right] \\
 & \left(\text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - \text{Log}\left[-\frac{d(f+gx)}{-df+cg}\right] \right) + \frac{1}{2dg\left(\frac{c}{d}+x\right)} \\
 & (-df+cg) \left(-\frac{cdg\left(\frac{c}{d}+x\right)}{(-df+cg)^2} + \frac{d\left(\frac{c}{d}+x\right)}{-df+cg} \right) \left(-2 \text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{dg\left(\frac{c}{d}+x\right)}{-df+cg}\right] \right) \\
 & \left(\text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - \text{Log}\left[-\frac{d(f+gx)}{-df+cg}\right] \right) - \left(b(-df+cg)\left(\frac{a}{b}+x\right) \right)
 \end{aligned}
 \end{aligned}$$

$$\begin{aligned}
 & \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \text{Log} \left[\frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right] \\
 & \left(-\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] + \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) \Bigg/ \left(d (b f - a g) \left(\frac{c}{d} + x\right) \right) + \frac{1}{d g \left(\frac{c}{d} + x\right)} \\
 & (-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g} \right) \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \\
 & \left(-\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] + \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) - \left(b (-d f + c g) \left(\frac{a}{b} + x\right) \right) \\
 & \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \\
 & \left(\text{Log} \left[\frac{-b c + a d}{b d \left(\frac{a}{b} + x\right)} \right] + \text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \text{Log} \left[-\frac{(-b c + a d) (f + g x)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \right) \Bigg/ \\
 & \left(d (b f - a g) \left(\frac{c}{d} + x\right) \right) + \frac{1}{b g \left(\frac{a}{b} + x\right)} (b f - a g) \left(-\frac{a b g \left(\frac{a}{b} + x\right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x\right)}{b f - a g} \right) \\
 & \left(\text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \right) \text{Log} \left[1 + \frac{b g \left(\frac{a}{b} + x\right)}{b f - a g} \right] - \\
 & \frac{1}{d g \left(\frac{c}{d} + x\right)} (-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g} \right) \left(\text{Log} \left[\frac{a}{b} + x \right] + \right. \\
 & \left. \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \right) \text{Log} \left[1 - \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right] - \left(b (-d f + c g) \left(\frac{a}{b} + x\right) \right) \\
 & \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \\
 & \left. \text{Log} \left[1 + \frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \right) \Bigg/ \left(d (b f - a g) \left(\frac{c}{d} + x\right) \right) + \frac{1}{b g \left(\frac{a}{b} + x\right)} \\
 & (b f - a g) \left(-\frac{a b g \left(\frac{a}{b} + x\right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x\right)}{b f - a g} \right) \text{PolyLog} \left[2, -\frac{b g \left(\frac{a}{b} + x\right)}{b f - a g} \right] + \\
 & \left(b (-d f + c g) \left(\frac{a}{b} + x\right) \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{PolyLog}\left[2, -\frac{b g \left(\frac{a}{b} + x\right)}{b f - a g}\right] \Big/ \left(d (b f - a g) \left(\frac{c}{d} + x\right)\right) - \frac{1}{d g \left(\frac{c}{d} + x\right)} \\
 & (-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g}\right) \text{PolyLog}\left[2, \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g}\right] - \\
 & \left(b (-d f + c g) \left(\frac{a}{b} + x\right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right) \right. \\
 & \left. \text{PolyLog}\left[2, \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g}\right] \Big/ \left(d (b f - a g) \left(\frac{c}{d} + x\right)\right) - \left(b (-d f + c g) \left(\frac{a}{b} + x\right) \right. \right. \\
 & \left. \left. \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right) \right] \left(\text{PolyLog}\left[2, \frac{c}{\frac{a}{b} + x}\right] - \right. \right. \\
 & \left. \left. \text{PolyLog}\left[2, -\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \right) \Big/ \left(d (b f - a g) \left(\frac{c}{d} + x\right)\right) - \right. \\
 & \left. \left(b (-d f + c g) \left(\frac{a}{b} + x\right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right) \right) \right. \\
 & \left. \text{PolyLog}\left[2, -\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \Big/ \left(d (b f - a g) \left(\frac{c}{d} + x\right)\right) \right] - \\
 & \frac{1}{g^2} \left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{b (f + g x)}{b f - a g}\right] + \frac{1}{2} \text{Log}\left[\frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g}\right] \right. \\
 & \left. \left(-2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g}\right]\right) \left(\text{Log}\left[\frac{b (f + g x)}{b f - a g}\right] - \text{Log}\left[-\frac{d (f + g x)}{-d f + c g}\right]\right) + \right. \\
 & \left. \text{Log}\left[\frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g}\right] \text{Log}\left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \left(-\text{Log}\left[\frac{b (f + g x)}{b f - a g}\right] + \right. \right. \\
 & \left. \left. \text{Log}\left[-\frac{d (f + g x)}{-d f + c g}\right]\right) + \frac{1}{2} \text{Log}\left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right]^2 \right. \\
 & \left. \left(\text{Log}\left[\frac{-b c + a d}{b d \left(\frac{a}{b} + x\right)}\right] + \text{Log}\left[\frac{b (f + g x)}{b f - a g}\right] - \text{Log}\left[-\frac{(-b c + a d) (f + g x)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \right) + \right. \\
 & \left. \left(\text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right]\right) \text{PolyLog}\left[2, -\frac{b g \left(\frac{a}{b} + x\right)}{b f - a g}\right] + \right.
 \end{aligned}$$

$$\left(\left(\left(\left(\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[- \frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) \text{PolyLog} \left[2, \frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] + \right. \right. \right. \\
\left. \left. \text{Log} \left[- \frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \left(\text{PolyLog} \left[2, \frac{\frac{c}{d} + x}{\frac{a}{b} + x} \right] - \right. \right. \right. \\
\left. \left. \text{PolyLog} \left[2, - \frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) - \text{PolyLog} \left[3, - \frac{bg \left(\frac{a}{b} + x \right)}{bf-ag} \right] - \text{PolyLog} \left[3, \right. \right. \\
\left. \left. \frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] - \text{PolyLog} \left[3, \frac{\frac{c}{d} + x}{\frac{a}{b} + x} \right] + \text{PolyLog} \left[3, - \frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) \right) \right) \right) \right)$$

Problem 279: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \text{Log} \left[\frac{e(a+bx)^2}{(c+dx)^2} \right] \right)^2}{(f+gx)^4} dx$$

Optimal (type 4, 724 leaves, 12 steps):

$$\frac{4B^2(bc-ad)^2 g^2 (c+dx)}{3(bf-ag)^2(df-cg)^3(f+gx)^2} - \frac{2B(bc-ad)g^2(c+dx)^2(A+B \text{Log}[\frac{e(a+bx)^2}{(c+dx)^2}])}{3(bf-ag)(df-cg)^3(f+gx)^2} + \\
\frac{4B(bc-ad)g(3bdf-bcg-2adg)(a+bx)(A+B \text{Log}[\frac{e(a+bx)^2}{(c+dx)^2}])}{3(bf-ag)^3(df-cg)^2(f+gx)} + \\
\frac{b^3(A+B \text{Log}[\frac{e(a+bx)^2}{(c+dx)^2}])^2}{3g(bf-ag)^3} - \frac{(A+B \text{Log}[\frac{e(a+bx)^2}{(c+dx)^2}])^2}{3g(f+gx)^3} + \frac{4B^2(bc-ad)^3 g^2 \text{Log}[\frac{a+bx}{c+dx}]}{3(bf-ag)^3(df-cg)^3} - \\
\frac{4B^2(bc-ad)^3 g^2 \text{Log}[\frac{f+gx}{c+dx}]}{3(bf-ag)^3(df-cg)^3} + \frac{8B^2(bc-ad)^2 g(3bdf-bcg-2adg) \text{Log}[\frac{f+gx}{c+dx}]}{3(bf-ag)^3(df-cg)^3} + \\
\left(4B(bc-ad)(a^2 d^2 g^2 - abdg(3df-cg) + b^2(3d^2 f^2 - 3cdfg + c^2 g^2)) \right. \\
\left. \left(A + B \text{Log} \left[\frac{e(a+bx)^2}{(c+dx)^2} \right] \right) \text{Log} \left[1 - \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)} \right] \right) / (3(bf-ag)^3(df-cg)^3) + \\
\left(8B^2(bc-ad)(a^2 d^2 g^2 - abdg(3df-cg) + b^2(3d^2 f^2 - 3cdfg + c^2 g^2)) \right. \\
\left. \text{PolyLog} \left[2, \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)} \right] \right) / (3(bf-ag)^3(df-cg)^3)$$

Result (type 4, 55173 leaves): Display of huge result suppressed!

Problem 280: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right]\right)^2}{(f+gx)^5} dx$$

Optimal (type 4, 1154 leaves, 15 steps):

$$\begin{aligned} & -\frac{B^2 (bc-ad)^2 g^3 (c+dx)^2}{3 (bf-ag)^2 (df-cg)^4 (f+gx)^2} - \frac{2 B^2 (bc-ad)^3 g^3 (c+dx)}{3 (bf-ag)^3 (df-cg)^4 (f+gx)} + \\ & \frac{B^2 (bc-ad)^2 g^2 (4 b d f - b c g - 3 a d g) (c+dx)}{(bf-ag)^3 (df-cg)^4 (f+gx)} + \frac{B (bc-ad) g^3 (c+dx)^3 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right]\right)}{3 (bf-ag) (df-cg)^4 (f+gx)^3} - \\ & \left(B (bc-ad) g^2 (4 b d f - b c g - 3 a d g) (c+dx)^2 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right]\right) \right) / \\ & \left(2 (bf-ag)^2 (df-cg)^4 (f+gx)^2 \right) + \\ & \left(B (bc-ad) g (3 a^2 d^2 g^2 - 2 a b d g (4 d f - c g) + b^2 (6 d^2 f^2 - 4 c d f g + c^2 g^2)) \right. \\ & \left. (a+bx) \left(A + B \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right]\right) \right) / \left((bf-ag)^4 (df-cg)^3 (f+gx) \right) + \\ & \frac{b^4 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right]\right)^2}{4 g (bf-ag)^4} - \frac{\left(A + B \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right]\right)^2}{4 g (f+gx)^4} - \frac{2 B^2 (bc-ad)^4 g^3 \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]}{3 (bf-ag)^4 (df-cg)^4} + \\ & \frac{B^2 (bc-ad)^3 g^2 (4 b d f - b c g - 3 a d g) \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]}{(bf-ag)^4 (df-cg)^4} + \\ & \frac{2 B^2 (bc-ad)^4 g^3 \operatorname{Log}\left[\frac{f+gx}{c+dx}\right]}{3 (bf-ag)^4 (df-cg)^4} - \frac{B^2 (bc-ad)^3 g^2 (4 b d f - b c g - 3 a d g) \operatorname{Log}\left[\frac{f+gx}{c+dx}\right]}{(bf-ag)^4 (df-cg)^4} + \\ & \left(2 B^2 (bc-ad)^2 g (3 a^2 d^2 g^2 - 2 a b d g (4 d f - c g) + b^2 (6 d^2 f^2 - 4 c d f g + c^2 g^2)) \operatorname{Log}\left[\frac{f+gx}{c+dx}\right] \right) / \\ & \left((bf-ag)^4 (df-cg)^4 \right) - \\ & \left(B (bc-ad) (2 b d f - b c g - a d g) (2 a b d^2 f g - a^2 d^2 g^2 - b^2 (2 d^2 f^2 - 2 c d f g + c^2 g^2)) \right. \\ & \left. \left(A + B \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right]\right) \operatorname{Log}\left[1 - \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)}\right] \right) / \left((bf-ag)^4 (df-cg)^4 \right) - \\ & \left(2 B^2 (bc-ad) (2 b d f - b c g - a d g) (2 a b d^2 f g - a^2 d^2 g^2 - b^2 (2 d^2 f^2 - 2 c d f g + c^2 g^2)) \right. \\ & \left. \operatorname{PolyLog}\left[2, \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)}\right] \right) / \left((bf-ag)^4 (df-cg)^4 \right) \end{aligned}$$

Result (type 4, 142956 leaves): Display of huge result suppressed!

Problem 305: Result more than twice size of optimal antiderivative.

$$\int (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^2 dx$$

Optimal (type 4, 137 leaves, 6 steps):

$$\frac{2 B (b c - a d) n \text{Log}\left[\frac{b c - a d}{b (c + d x)}\right] (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])}{b d} + \frac{(a + b x) (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{b} + \frac{2 B^2 (b c - a d) n^2 \text{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]}{b d}$$

Result (type 4, 327 leaves):

$$-\frac{1}{b d} \left(2 a A B d n + 2 a B^2 d n^2 - A^2 b d x + a B^2 d n^2 \text{Log}[a + b x]^2 + 2 A b B c n \text{Log}[c + d x] + 2 a B^2 d n^2 \text{Log}[c + d x] + b B^2 c n^2 \text{Log}[c + d x]^2 + 2 a B^2 d n \text{Log}[e (a + b x)^n (c + d x)^{-n}] - 2 A b B d x \text{Log}[e (a + b x)^n (c + d x)^{-n}] + 2 b B^2 c n \text{Log}[c + d x] \text{Log}[e (a + b x)^n (c + d x)^{-n}] - b B^2 d x \text{Log}[e (a + b x)^n (c + d x)^{-n}]^2 - 2 B n \text{Log}[a + b x] \left(b B c n \text{Log}[c + d x] + B (-b c + a d) n \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) + a d (A + B n + B \text{Log}[e (a + b x)^n (c + d x)^{-n}]) \right) + 2 B^2 (b c - a d) n^2 \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right]$$

Problem 306: Result more than twice size of optimal antiderivative.

$$\int \frac{(A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{g + h x} dx$$

Optimal (type 4, 301 leaves, 10 steps):

$$-\frac{\text{Log}\left[\frac{b c - a d}{b (c + d x)}\right] (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{h} + \frac{(A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^2 \text{Log}\left[1 - \frac{(d g - c h) (a + b x)}{(b g - a h) (c + d x)}\right]}{h} - \frac{2 B n (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}]) \text{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]}{h} + \frac{2 B n (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}]) \text{PolyLog}\left[2, \frac{(d g - c h) (a + b x)}{(b g - a h) (c + d x)}\right]}{h} + \frac{2 B^2 n^2 \text{PolyLog}\left[3, \frac{d (a + b x)}{b (c + d x)}\right]}{h} - \frac{2 B^2 n^2 \text{PolyLog}\left[3, \frac{(d g - c h) (a + b x)}{(b g - a h) (c + d x)}\right]}{h}$$

Result (type 4, 1082 leaves):

$$\begin{aligned}
 & \frac{1}{h} \left((A+B(-n \operatorname{Log}[a+bx] + n \operatorname{Log}[c+dx] + \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}]])^2 \operatorname{Log}[g+hx] + \right. \\
 & 2Bn(A+B(-n \operatorname{Log}[a+bx] + n \operatorname{Log}[c+dx] + \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}]]) \\
 & \left. \left(\operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \operatorname{PolyLog}\left[2, \frac{h(a+bx)}{-bg+ah}\right] \right) - \right. \\
 & 2ABn \left(\operatorname{Log}[c+dx] \operatorname{Log}\left[\frac{d(g+hx)}{dg-ch}\right] + \operatorname{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right] \right) - \\
 & 2B^2n(-n \operatorname{Log}[a+bx] + n \operatorname{Log}[c+dx] + \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}]) \\
 & \left. \left(\operatorname{Log}[c+dx] \operatorname{Log}\left[\frac{d(g+hx)}{dg-ch}\right] + \operatorname{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right] \right) + \right. \\
 & B^2n^2 \left(\operatorname{Log}[a+bx]^2 \operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + 2 \operatorname{Log}[a+bx] \operatorname{PolyLog}\left[2, \frac{h(a+bx)}{-bg+ah}\right] - \right. \\
 & \left. 2 \operatorname{PolyLog}\left[3, \frac{h(a+bx)}{-bg+ah}\right] \right) + B^2n^2 \left(\operatorname{Log}[c+dx]^2 \operatorname{Log}\left[\frac{d(g+hx)}{dg-ch}\right] + \right. \\
 & \left. 2 \operatorname{Log}[c+dx] \operatorname{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right] - 2 \operatorname{PolyLog}\left[3, \frac{h(c+dx)}{-dg+ch}\right] \right) - \\
 & 2B^2n^2 \left(\operatorname{Log}[a+bx] \operatorname{Log}[c+dx] \operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \frac{1}{2} \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \right. \\
 & \left. \left(-2 \operatorname{Log}[a+bx] + \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \right) \left(\operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - \operatorname{Log}\left[\frac{d(g+hx)}{dg-ch}\right] \right) \right) + \\
 & \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \operatorname{Log}\left[\frac{(bg-ah)(c+dx)}{(dg-ch)(a+bx)}\right] \left(-\operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \operatorname{Log}\left[\frac{d(g+hx)}{dg-ch}\right] \right) \right) + \\
 & \frac{1}{2} \operatorname{Log}\left[\frac{(bg-ah)(c+dx)}{(dg-ch)(a+bx)}\right]^2 \\
 & \left(\operatorname{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] + \operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - \operatorname{Log}\left[\frac{(-bc+ad)(g+hx)}{(dg-ch)(a+bx)}\right] \right) + \\
 & \left(\operatorname{Log}[c+dx] - \operatorname{Log}\left[\frac{(bg-ah)(c+dx)}{(dg-ch)(a+bx)}\right] \right) \operatorname{PolyLog}\left[2, \frac{h(a+bx)}{-bg+ah}\right] + \\
 & \left(\operatorname{Log}[a+bx] + \operatorname{Log}\left[\frac{(bg-ah)(c+dx)}{(dg-ch)(a+bx)}\right] \right) \operatorname{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right] + \\
 & \operatorname{Log}\left[\frac{(bg-ah)(c+dx)}{(dg-ch)(a+bx)}\right] \left(\operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right] - \operatorname{PolyLog}\left[2, \frac{(bg-ah)(c+dx)}{(dg-ch)(a+bx)}\right] \right) - \\
 & \operatorname{PolyLog}\left[3, \frac{h(a+bx)}{-bg+ah}\right] - \operatorname{PolyLog}\left[3, \frac{h(c+dx)}{-dg+ch}\right] - \\
 & \left. \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right] + \operatorname{PolyLog}\left[3, \frac{(bg-ah)(c+dx)}{(dg-ch)(a+bx)}\right] \right) \right)
 \end{aligned}$$

Problem 307: Result more than twice size of optimal antiderivative.

$$\int \frac{(A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{(g + h x)^2} dx$$

Optimal (type 4, 208 leaves, 5 steps):

$$\frac{(a + b x) (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{(b g - a h) (g + h x)} + \left(2 B (b c - a d) n (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}]) \text{Log}\left[1 - \frac{(d g - c h) (a + b x)}{(b g - a h) (c + d x)}\right] \right) / \left((b g - a h) (d g - c h) \right) + \frac{2 B^2 (b c - a d) n^2 \text{PolyLog}\left[2, \frac{(d g - c h) (a + b x)}{(b g - a h) (c + d x)}\right]}{(b g - a h) (d g - c h)}$$

Result (type 4, 3460 leaves):

$$\frac{1}{h (-b g + a h) (-d g + c h) (g + h x)} \left(-A^2 b d g^2 + A^2 b c g h + a A^2 d g h - a A^2 c h^2 + 2 A b B d g^2 n \text{Log}[a + b x] - 2 A b B c g h n \text{Log}[a + b x] + 2 A b B d g h n x \text{Log}[a + b x] - 2 A b B c h^2 n x \text{Log}[a + b x] - b B^2 d g^2 n^2 \text{Log}[a + b x]^2 + b B^2 c g h n^2 \text{Log}[a + b x]^2 - b B^2 d g h n^2 x \text{Log}[a + b x]^2 + b B^2 c h^2 n^2 x \text{Log}[a + b x]^2 - 2 A b B d g^2 n \text{Log}[c + d x] + 2 a A B d g h n \text{Log}[c + d x] - 2 A b B d g h n x \text{Log}[c + d x] + 2 a A B d h^2 n x \text{Log}[c + d x] + 2 b B^2 d g^2 n^2 \text{Log}[a + b x] \text{Log}[c + d x] - 2 a B^2 d g h n^2 \text{Log}[a + b x] \text{Log}[c + d x] + 2 b B^2 d g h n^2 x \text{Log}[a + b x] \text{Log}[c + d x] - 2 a B^2 d h^2 n^2 x \text{Log}[a + b x] \text{Log}[c + d x] - b B^2 d g^2 n^2 \text{Log}[c + d x]^2 + a B^2 d g h n^2 \text{Log}[c + d x]^2 - b B^2 d g h n^2 x \text{Log}[c + d x]^2 + a B^2 d h^2 n^2 x \text{Log}[c + d x]^2 - 2 b B^2 c g h n^2 \text{Log}[a + b x] \text{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] + 2 a B^2 d g h n^2 \text{Log}[a + b x] \text{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] - 2 b B^2 c h^2 n^2 x \text{Log}[a + b x] \text{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] + 2 a B^2 d h^2 n^2 x \text{Log}[a + b x] \text{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] + b B^2 c g h n^2 \text{Log}\left[\frac{h (c + d x)}{-d g + c h}\right]^2 - a B^2 d g h n^2 \text{Log}\left[\frac{h (c + d x)}{-d g + c h}\right]^2 + b B^2 c h^2 n^2 x \text{Log}\left[\frac{h (c + d x)}{-d g + c h}\right]^2 - a B^2 d h^2 n^2 x \text{Log}\left[\frac{h (c + d x)}{-d g + c h}\right]^2 - 2 b B^2 c g h n^2 \text{Log}\left[\frac{-b c + a d}{d (a + b x)}\right] \text{Log}\left[\frac{(b g - a h) (c + d x)}{(d g - c h) (a + b x)}\right] + 2 a B^2 d g h n^2 \text{Log}\left[\frac{-b c + a d}{d (a + b x)}\right] \text{Log}\left[\frac{(b g - a h) (c + d x)}{(d g - c h) (a + b x)}\right] - 2 b B^2 c h^2 n^2 x \text{Log}\left[\frac{-b c + a d}{d (a + b x)}\right] \text{Log}\left[\frac{(b g - a h) (c + d x)}{(d g - c h) (a + b x)}\right] + 2 a B^2 d h^2 n^2 x \text{Log}\left[\frac{-b c + a d}{d (a + b x)}\right] \text{Log}\left[\frac{(b g - a h) (c + d x)}{(d g - c h) (a + b x)}\right] - 2 b B^2 c g h n^2 \text{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] \text{Log}\left[\frac{(b g - a h) (c + d x)}{(d g - c h) (a + b x)}\right] +$$

$$\begin{aligned}
 & 2 a B^2 d g h n^2 \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{(b g-a h)(c+d x)}{(d g-c h)(a+b x)}\right] - \\
 & 2 b B^2 c h^2 n^2 x \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{(b g-a h)(c+d x)}{(d g-c h)(a+b x)}\right] + \\
 & 2 a B^2 d h^2 n^2 x \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{(b g-a h)(c+d x)}{(d g-c h)(a+b x)}\right] + \\
 & b B^2 c g h n^2 \operatorname{Log}\left[\frac{(b g-a h)(c+d x)}{(d g-c h)(a+b x)}\right]^2 - a B^2 d g h n^2 \operatorname{Log}\left[\frac{(b g-a h)(c+d x)}{(d g-c h)(a+b x)}\right]^2 + \\
 & b B^2 c h^2 n^2 x \operatorname{Log}\left[\frac{(b g-a h)(c+d x)}{(d g-c h)(a+b x)}\right]^2 - a B^2 d h^2 n^2 x \operatorname{Log}\left[\frac{(b g-a h)(c+d x)}{(d g-c h)(a+b x)}\right]^2 - \\
 & 2 A b B d g^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + 2 A b B c g h \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 2 a A B d g h \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - 2 a A B c h^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 2 b B^2 d g^2 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
 & 2 b B^2 c g h n \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 2 b B^2 d g h n x \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
 & 2 b B^2 c h^2 n x \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
 & 2 b B^2 d g^2 n \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 2 a B^2 d g h n \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - \\
 & 2 b B^2 d g h n x \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & 2 a B^2 d h^2 n x \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] - b B^2 d g^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2 + \\
 & b B^2 c g h \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2 + a B^2 d g h \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2 - \\
 & a B^2 c h^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2 - 2 A b B d g^2 n \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] + \\
 & 2 A b B c g h n \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] - 2 A b B d g h n x \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] + 2 A b B c h^2 n x \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] + \\
 & 2 b B^2 d g^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] - 2 a B^2 d g h n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] + \\
 & 2 b B^2 d g h n^2 x \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] - 2 a B^2 d h^2 n^2 x \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] - \\
 & 2 b B^2 d g^2 n^2 \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] + 2 b B^2 c g h n^2 \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] - \\
 & 2 b B^2 d g h n^2 x \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] + \\
 & 2 b B^2 c h^2 n^2 x \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] - 2 b B^2 d g^2 n \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] \\
 & \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] + 2 b B^2 c g h n \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] - \\
 & 2 b B^2 d g h n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] + \\
 & 2 b B^2 c h^2 n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] + 2 A b B d g^2 n \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right] -
 \end{aligned}$$

$$\begin{aligned}
 & 2 a A B d g h n \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]+2 A b B d g h n x \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]-2 a A B d h^2 n x \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]- \\
 & 2 b B^2 d g^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]+2 a B^2 d g h n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]- \\
 & 2 b B^2 d g h n^2 x \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]+2 a B^2 d h^2 n^2 x \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]+ \\
 & 2 b B^2 d g^2 n^2 \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]-2 b B^2 c g h n^2 \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]+ \\
 & 2 b B^2 d g h n^2 x \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]- \\
 & 2 b B^2 c h^2 n^2 x \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]+2 b B^2 d g^2 n \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] \\
 & \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]-2 a B^2 d g h n \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]+ \\
 & 2 b B^2 d g h n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]- \\
 & 2 a B^2 d h^2 n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]+ \\
 & 2 B^2(b c-a d) h n^2(g+h x) \operatorname{PolyLog}\left[2, \frac{h(a+b x)}{-b g+a h}\right]- \\
 & 2 B^2(b c-a d) h n^2(g+h x) \operatorname{PolyLog}\left[2, \frac{h(c+d x)}{-d g+c h}\right]- \\
 & 2 b B^2 c g h n^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]+2 a B^2 d g h n^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]- \\
 & 2 b B^2 c h^2 n^2 x \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]+2 a B^2 d h^2 n^2 x \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]
 \end{aligned}$$

Problem 308: Result more than twice size of optimal antiderivative.

$$\int \frac{(A+B \operatorname{Log}[e(a+b x)^n(c+d x)^{-n}])^2}{(g+h x)^3} d x$$

Optimal (type 4, 393 leaves, 10 steps):

$$\begin{aligned}
 & \frac{B (b c - a d) h n (a + b x) (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])}{(b g - a h)^2 (d g - c h) (g + h x)} + \\
 & \frac{b^2 (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{2 h (b g - a h)^2} - \\
 & \frac{(A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{2 h (g + h x)^2} + \frac{B^2 (b c - a d)^2 h n^2 \text{Log}\left[\frac{g+h x}{c+d x}\right]}{(b g - a h)^2 (d g - c h)^2} + \\
 & \left(B (b c - a d) (2 b d g - b c h - a d h) n (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}]) \right. \\
 & \quad \left. \text{Log}\left[1 - \frac{(d g - c h) (a + b x)}{(b g - a h) (c + d x)}\right] \right) / \left((b g - a h)^2 (d g - c h)^2 \right) + \\
 & \frac{B^2 (b c - a d) (2 b d g - b c h - a d h) n^2 \text{PolyLog}\left[2, \frac{(d g - c h) (a + b x)}{(b g - a h) (c + d x)}\right]}{(b g - a h)^2 (d g - c h)^2}
 \end{aligned}$$

Result (type 4, 15422 leaves):

$$\begin{aligned}
 & -\frac{1}{2 h (g + h x)^2} (A + B (-n \text{Log}[a + b x] + n \text{Log}[c + d x] + \text{Log}[e (a + b x)^n (c + d x)^{-n}]))^2 + \\
 & \frac{1}{h} B n (A + B (-n \text{Log}[a + b x] + n \text{Log}[c + d x] + \text{Log}[e (a + b x)^n (c + d x)^{-n}])) \\
 & \left(\frac{b^2 h (a + b x)}{(-b g + a h)^3 \left(1 - \frac{h(a+b x)}{-b g + a h}\right)} - \left(\frac{b^2 h^2 (a + b x)^2}{(-b g + a h)^4 \left(1 - \frac{h(a+b x)}{-b g + a h}\right)^2} + \frac{2 b^2 h (a + b x)}{(-b g + a h)^3 \left(1 - \frac{h(a+b x)}{-b g + a h}\right)} \right) \right. \\
 & \quad \left. \text{Log}[a + b x] - \frac{b^2 \text{Log}\left[1 - \frac{h(a+b x)}{-b g + a h}\right]}{(-b g + a h)^2} \right) - \frac{1}{h} A B n \left(\frac{d^2 h (c + d x)}{(-d g + c h)^3 \left(1 - \frac{h(c+d x)}{-d g + c h}\right)} - \right. \\
 & \quad \left. \left(\frac{d^2 h^2 (c + d x)^2}{(-d g + c h)^4 \left(1 - \frac{h(c+d x)}{-d g + c h}\right)^2} + \frac{2 d^2 h (c + d x)}{(-d g + c h)^3 \left(1 - \frac{h(c+d x)}{-d g + c h}\right)} \right) \text{Log}[c + d x] - \frac{d^2 \text{Log}\left[1 - \frac{h(c+d x)}{-d g + c h}\right]}{(-d g + c h)^2} \right) - \\
 & \frac{1}{h} B^2 n (-n \text{Log}[a + b x] + n \text{Log}[c + d x] + \text{Log}[e (a + b x)^n (c + d x)^{-n}]) \left(\frac{d^2 h (c + d x)}{(-d g + c h)^3 \left(1 - \frac{h(c+d x)}{-d g + c h}\right)} - \right. \\
 & \quad \left. \left(\frac{d^2 h^2 (c + d x)^2}{(-d g + c h)^4 \left(1 - \frac{h(c+d x)}{-d g + c h}\right)^2} + \frac{2 d^2 h (c + d x)}{(-d g + c h)^3 \left(1 - \frac{h(c+d x)}{-d g + c h}\right)} \right) \text{Log}[c + d x] - \frac{d^2 \text{Log}\left[1 - \frac{h(c+d x)}{-d g + c h}\right]}{(-d g + c h)^2} \right) + \\
 & \frac{1}{h} B^2 n^2 \left(-\frac{1}{2} \left(\frac{b^2 h^2 (a + b x)^2}{(-b g + a h)^4 \left(1 - \frac{h(a+b x)}{-b g + a h}\right)^2} + \frac{2 b^2 h (a + b x)}{(-b g + a h)^3 \left(1 - \frac{h(a+b x)}{-b g + a h}\right)} \right) \text{Log}[a + b x]^2 + \right. \\
 & \quad \left. \frac{b^2 \text{Log}\left[1 - \frac{h(a+b x)}{-b g + a h}\right]}{(-b g + a h)^2} + \text{Log}[a + b x] \left(\frac{b^2 h (a + b x)}{(-b g + a h)^3 \left(1 - \frac{h(a+b x)}{-b g + a h}\right)} - \frac{b^2 \text{Log}\left[1 - \frac{h(a+b x)}{-b g + a h}\right]}{(-b g + a h)^2} \right) - \right.
 \end{aligned}$$

$$\frac{b^2 \operatorname{PolyLog}\left[2, \frac{h(a+b x)}{-b g+a h}\right]}{(-b g+a h)^2} + \frac{1}{h}$$

$$B^2 n^2 \left(-\frac{1}{2} \left(\frac{d^2 h^2 (c+d x)^2}{(-d g+c h)^4 \left(1-\frac{h(c+d x)}{-d g+c h}\right)^2} + \frac{2 d^2 h (c+d x)}{(-d g+c h)^3 \left(1-\frac{h(c+d x)}{-d g+c h}\right)} \right) \operatorname{Log}[c+d x]^2 + \right.$$

$$\frac{d^2 \operatorname{Log}\left[1-\frac{h(c+d x)}{-d g+c h}\right]}{(-d g+c h)^2} + \operatorname{Log}[c+d x] \left(\frac{d^2 h (c+d x)}{(-d g+c h)^3 \left(1-\frac{h(c+d x)}{-d g+c h}\right)} - \frac{d^2 \operatorname{Log}\left[1-\frac{h(c+d x)}{-d g+c h}\right]}{(-d g+c h)^2} \right) -$$

$$\left. \frac{d^2 \operatorname{PolyLog}\left[2, \frac{h(c+d x)}{-d g+c h}\right]}{(-d g+c h)^2} \right) -$$

$$\frac{1}{g^2} B^2 n^2 \left(\frac{1}{h} 2 \left(\operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] + \frac{1}{2} \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \right) \right.$$

$$\left(-2 \operatorname{Log}[a+b x] + \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \right) \left(\operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] - \operatorname{Log}\left[-\frac{d(g+h x)}{-d g+c h}\right] \right) +$$

$$\operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[-\frac{(b g-a h)(c+d x)}{(-d g+c h)(a+b x)}\right] \left(-\operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] + \operatorname{Log}\left[-\frac{d(g+h x)}{-d g+c h}\right] \right) +$$

$$\frac{1}{2} \operatorname{Log}\left[-\frac{(b g-a h)(c+d x)}{(-d g+c h)(a+b x)}\right]^2 \left(\operatorname{Log}\left[\frac{-b c+a d}{d(a+b x)}\right] + \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] - \right.$$

$$\left. \operatorname{Log}\left[-\frac{(-b c+a d)(g+h x)}{(-d g+c h)(a+b x)}\right] \right) + \left(\operatorname{Log}[c+d x] - \operatorname{Log}\left[-\frac{(b g-a h)(c+d x)}{(-d g+c h)(a+b x)}\right] \right)$$

$$\operatorname{PolyLog}\left[2, -\frac{h(a+b x)}{b g-a h}\right] + \left(\operatorname{Log}[a+b x] + \operatorname{Log}\left[-\frac{(b g-a h)(c+d x)}{(-d g+c h)(a+b x)}\right] \right)$$

$$\operatorname{PolyLog}\left[2, \frac{h(c+d x)}{-d g+c h}\right] + \operatorname{Log}\left[-\frac{(b g-a h)(c+d x)}{(-d g+c h)(a+b x)}\right] \left(\operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right] - \right.$$

$$\left. \operatorname{PolyLog}\left[2, -\frac{(b g-a h)(c+d x)}{(-d g+c h)(a+b x)}\right] \right) - \operatorname{PolyLog}\left[3, -\frac{h(a+b x)}{b g-a h}\right] - \operatorname{PolyLog}\left[3, \right.$$

$$\left. \frac{h(c+d x)}{-d g+c h}\right] - \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{d(a+b x)}\right] + \operatorname{PolyLog}\left[3, -\frac{(b g-a h)(c+d x)}{(-d g+c h)(a+b x)}\right] \right) +$$

$$h^2 \left(\frac{1}{h} \left(\left(\frac{(b g-a h) \left(\frac{2 a b x}{(b g-a h)^2} + \frac{2 a^2 b (g+h x)}{(b g-a h)^3} \right)}{b(g+h x)} - \frac{(b g-a h) x \left(\frac{b x}{b g-a h} + \frac{a b (g+h x)}{(b g-a h)^2} \right)}{b(g+h x)^2} - \right. \right.$$

$$\left. \frac{a \left(\frac{b x}{b g-a h} + \frac{a b (g+h x)}{(b g-a h)^2} \right)}{b(g+h x)} \right) \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] - \left(2(-d g+c h)(a+b x) \right.$$

$$\begin{aligned}
 & \left(\frac{c (b g - a h) (c + d x)}{(-d g + c h)^2 (a + b x)} + \frac{a (c + d x)}{(-d g + c h) (a + b x)} \right) \left(\frac{(b g - a h) \left(\frac{b x}{b g - a h} + \frac{a b (g + h x)}{(b g - a h)^2} \right)}{b (g + h x)} \right. \\
 & \left. \left((-d g + c h) (a + b x) \left(-\frac{(-b c + a d) x}{(-d g + c h) (a + b x)} + \frac{c (-b c + a d) (g + h x)}{(-d g + c h)^2 (a + b x)} \right) \right) \right) / \\
 & \left((-b c + a d) (g + h x) \right) \left. \right) \text{Log} \left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)} \right] / \left((b g - a h) (c + d x) \right) + \\
 & \left(-\frac{(b g - a h) \left(\frac{2 a b x}{(b g - a h)^2} + \frac{2 a^2 b (g + h x)}{(b g - a h)^3} \right)}{b (g + h x)} + \frac{(b g - a h) x \left(\frac{b x}{b g - a h} + \frac{a b (g + h x)}{(b g - a h)^2} \right)}{b (g + h x)^2} \right. \\
 & \left. \frac{a \left(\frac{b x}{b g - a h} + \frac{a b (g + h x)}{(b g - a h)^2} \right)}{b (g + h x)} - \frac{(-d g + c h) \left(\frac{2 c d x}{(-d g + c h)^2} - \frac{2 c^2 d (g + h x)}{(-d g + c h)^3} \right)}{d (g + h x)} + \right. \\
 & \left. \frac{(-d g + c h) x \left(-\frac{d x}{-d g + c h} + \frac{c d (g + h x)}{(-d g + c h)^2} \right)}{d (g + h x)^2} - \frac{c \left(-\frac{d x}{-d g + c h} + \frac{c d (g + h x)}{(-d g + c h)^2} \right)}{d (g + h x)} \right) \text{Log} \left[\frac{h (c + d x)}{-d g + c h} \right] \\
 & \text{Log} \left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)} \right] + \frac{1}{2} \left(\frac{(b g - a h) \left(\frac{2 a b x}{(b g - a h)^2} + \frac{2 a^2 b (g + h x)}{(b g - a h)^3} \right)}{b (g + h x)} - \right. \\
 & \left. \frac{(b g - a h) x \left(\frac{b x}{b g - a h} + \frac{a b (g + h x)}{(b g - a h)^2} \right)}{b (g + h x)^2} - \frac{a \left(\frac{b x}{b g - a h} + \frac{a b (g + h x)}{(b g - a h)^2} \right)}{b (g + h x)} \right. \\
 & \left. \left((-d g + c h) (a + b x) \left(\frac{2 c (-b c + a d) x}{(-d g + c h)^2 (a + b x)} - \frac{2 c^2 (-b c + a d) (g + h x)}{(-d g + c h)^3 (a + b x)} \right) \right) \right) / \\
 & \left((-b c + a d) (g + h x) \right) - \left((-d g + c h) x (a + b x) \right. \\
 & \left. \left(-\frac{(-b c + a d) x}{(-d g + c h) (a + b x)} + \frac{c (-b c + a d) (g + h x)}{(-d g + c h)^2 (a + b x)} \right) \right) / \left((-b c + a d) (g + h x)^2 \right) + \\
 & \left. \frac{c (a + b x) \left(-\frac{(-b c + a d) x}{(-d g + c h) (a + b x)} + \frac{c (-b c + a d) (g + h x)}{(-d g + c h)^2 (a + b x)} \right)}{(-b c + a d) (g + h x)} \right) \text{Log} \left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)} \right]^2 + \\
 & 2 \left(-\frac{(b g - a h) \left(\frac{b x}{b g - a h} + \frac{a b (g + h x)}{(b g - a h)^2} \right)}{b (g + h x)} - \frac{(-d g + c h) \left(-\frac{d x}{-d g + c h} + \frac{c d (g + h x)}{(-d g + c h)^2} \right)}{d (g + h x)} \right) \\
 & \left(-\left(\left((-d g + c h) (a + b x) \left(\frac{c (b g - a h) (c + d x)}{(-d g + c h)^2 (a + b x)} + \frac{a (c + d x)}{(-d g + c h) (a + b x)} \right) \right) \right. \right. \\
 & \left. \left. \text{Log} \left[\frac{h (c + d x)}{-d g + c h} \right] \right) / \left((b g - a h) (c + d x) \right) \right) + \frac{1}{h (c + d x)}
 \end{aligned}$$

$$\begin{aligned}
 & (-d g + c h) \left(-\frac{c h (c + d x)}{(-d g + c h)^2} + \frac{c + d x}{-d g + c h} \right) \text{Log} \left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)} \right] + \\
 & \frac{1}{h (c + d x)} (-d g + c h) \left(-\frac{c h (c + d x)}{(-d g + c h)^2} + \frac{c + d x}{-d g + c h} \right) \\
 & \left(\left(\frac{(b g - a h) \left(\frac{b x}{b g - a h} + \frac{a b (g + h x)}{(b g - a h)^2} \right)}{b (g + h x)} + \frac{(-d g + c h) \left(-\frac{d x}{-d g + c h} + \frac{c d (g + h x)}{(-d g + c h)^2} \right)}{d (g + h x)} \right) \right. \\
 & \left. \left(-2 \text{Log}[a + b x] + \text{Log} \left[\frac{h (c + d x)}{-d g + c h} \right] \right) + \frac{1}{h (c + d x)} \right. \\
 & \left. (-d g + c h) \left(-\frac{c h (c + d x)}{(-d g + c h)^2} + \frac{c + d x}{-d g + c h} \right) \left(\text{Log} \left[\frac{b (g + h x)}{b g - a h} \right] - \text{Log} \left[-\frac{d (g + h x)}{-d g + c h} \right] \right) \right) + \\
 & \frac{1}{2} \text{Log} \left[\frac{h (c + d x)}{-d g + c h} \right] \left(\frac{1}{h (c + d x)} 2 (-d g + c h) \left(-\frac{c h (c + d x)}{(-d g + c h)^2} + \frac{c + d x}{-d g + c h} \right) \right. \\
 & \left. \left(\frac{(b g - a h) \left(\frac{b x}{b g - a h} + \frac{a b (g + h x)}{(b g - a h)^2} \right)}{b (g + h x)} + \frac{(-d g + c h) \left(-\frac{d x}{-d g + c h} + \frac{c d (g + h x)}{(-d g + c h)^2} \right)}{d (g + h x)} \right) + \right. \\
 & \left. \left(\frac{(b g - a h) \left(\frac{2 a b x}{(b g - a h)^2} + \frac{2 a^2 b (g + h x)}{(b g - a h)^3} \right)}{b (g + h x)} - \frac{(b g - a h) x \left(\frac{b x}{b g - a h} + \frac{a b (g + h x)}{(b g - a h)^2} \right)}{b (g + h x)^2} - \right. \right. \\
 & \left. \frac{a \left(\frac{b x}{b g - a h} + \frac{a b (g + h x)}{(b g - a h)^2} \right)}{b (g + h x)} + \frac{(-d g + c h) \left(\frac{2 c d x}{(-d g + c h)^2} - \frac{2 c^2 d (g + h x)}{(-d g + c h)^3} \right)}{d (g + h x)} - \right. \\
 & \left. \frac{(-d g + c h) x \left(-\frac{d x}{-d g + c h} + \frac{c d (g + h x)}{(-d g + c h)^2} \right)}{d (g + h x)^2} + \frac{c \left(-\frac{d x}{-d g + c h} + \frac{c d (g + h x)}{(-d g + c h)^2} \right)}{d (g + h x)} \right) \\
 & \left. \left(-2 \text{Log}[a + b x] + \text{Log} \left[\frac{h (c + d x)}{-d g + c h} \right] \right) + \left(\frac{(-d g + c h) \left(\frac{2 c^2 h (c + d x)}{(-d g + c h)^3} - \frac{2 c (c + d x)}{(-d g + c h)^2} \right)}{h (c + d x)} + \right. \right. \\
 & \left. \frac{c \left(-\frac{c h (c + d x)}{(-d g + c h)^2} + \frac{c + d x}{-d g + c h} \right)}{h (c + d x)} - \frac{(-d g + c h) \left(-\frac{c h (c + d x)}{(-d g + c h)^2} + \frac{c + d x}{-d g + c h} \right)}{h^2 (c + d x)} \right) \left(\text{Log} \left[\right. \right. \\
 & \left. \frac{b (g + h x)}{b g - a h} \right] - \text{Log} \left[-\frac{d (g + h x)}{-d g + c h} \right] \right) \left. \right) + \frac{1}{2} \left(\frac{(-d g + c h) \left(\frac{2 c^2 h (c + d x)}{(-d g + c h)^3} - \frac{2 c (c + d x)}{(-d g + c h)^2} \right)}{h (c + d x)} + \right. \\
 & \left. \frac{c \left(-\frac{c h (c + d x)}{(-d g + c h)^2} + \frac{c + d x}{-d g + c h} \right)}{h (c + d x)} - \frac{(-d g + c h) \left(-\frac{c h (c + d x)}{(-d g + c h)^2} + \frac{c + d x}{-d g + c h} \right)}{h^2 (c + d x)} \right) \\
 & \left. \left(-2 \text{Log}[a + b x] + \text{Log} \left[\frac{h (c + d x)}{-d g + c h} \right] \right) \left(\text{Log} \left[\frac{b (g + h x)}{b g - a h} \right] - \text{Log} \left[-\frac{d (g + h x)}{-d g + c h} \right] \right) + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(- \left(\left(2 (-d g + c h)^2 (a + b x) \left(-\frac{c h (c + d x)}{(-d g + c h)^2} + \frac{c + d x}{-d g + c h} \right) \left(\frac{c (b g - a h) (c + d x)}{(-d g + c h)^2 (a + b x)} + \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{a (c + d x)}{(-d g + c h) (a + b x)} \right) \right) \right) / \left(h (b g - a h) (c + d x)^2 \right) \Bigg) + \\
 & \left(- \left(\left((-d g + c h) (a + b x) \left(-\frac{2 c^2 (b g - a h) (c + d x)}{(-d g + c h)^3 (a + b x)} - \frac{2 a c (c + d x)}{(-d g + c h)^2 (a + b x)} \right) \right) \right) / \right. \\
 & \quad \left. \left((b g - a h) (c + d x) \right) \right) - \frac{c (a + b x) \left(\frac{c (b g - a h) (c + d x)}{(-d g + c h)^2 (a + b x)} + \frac{a (c + d x)}{(-d g + c h) (a + b x)} \right)}{(b g - a h) (c + d x)} - \\
 & \left(a (-d g + c h) (a + b x) \left(\frac{c (b g - a h) (c + d x)}{(-d g + c h)^2 (a + b x)} + \frac{a (c + d x)}{(-d g + c h) (a + b x)} \right) \right) / \\
 & \quad \left((b g - a h)^2 (c + d x) \right) \Bigg) \text{Log} \left[\frac{h (c + d x)}{-d g + c h} \right] + \\
 & \left(\frac{(-d g + c h) \left(\frac{2 c^2 h (c + d x)}{(-d g + c h)^3} - \frac{2 c (c + d x)}{(-d g + c h)^2} \right)}{h (c + d x)} + \frac{c \left(-\frac{c h (c + d x)}{(-d g + c h)^2} + \frac{c + d x}{-d g + c h} \right)}{h (c + d x)} - \right. \\
 & \quad \left. \frac{(-d g + c h) \left(-\frac{c h (c + d x)}{(-d g + c h)^2} + \frac{c + d x}{-d g + c h} \right)}{h^2 (c + d x)} \right) \text{Log} \left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)} \right] \Bigg) \\
 & \left(-\text{Log} \left[\frac{b (g + h x)}{b g - a h} \right] + \text{Log} \left[-\frac{d (g + h x)}{-d g + c h} \right] \right) + \frac{1}{2} \left(\left(2 (-d g + c h)^2 (a + b x)^2 \right. \right. \\
 & \quad \left. \left. \left(\frac{c (b g - a h) (c + d x)}{(-d g + c h)^2 (a + b x)} + \frac{a (c + d x)}{(-d g + c h) (a + b x)} \right)^2 \right) / \left((b g - a h)^2 (c + d x)^2 \right) - \right. \\
 & \quad \left(2 (-d g + c h) (a + b x) \left(-\frac{2 c^2 (b g - a h) (c + d x)}{(-d g + c h)^3 (a + b x)} - \frac{2 a c (c + d x)}{(-d g + c h)^2 (a + b x)} \right) \right. \\
 & \quad \left. \text{Log} \left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)} \right] \right) / \left((b g - a h) (c + d x) \right) - \\
 & \quad \left(2 c (a + b x) \left(\frac{c (b g - a h) (c + d x)}{(-d g + c h)^2 (a + b x)} + \frac{a (c + d x)}{(-d g + c h) (a + b x)} \right) \right. \\
 & \quad \left. \text{Log} \left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)} \right] \right) / \left((b g - a h) (c + d x) \right) - \\
 & \quad \left(2 a (-d g + c h) (a + b x) \left(\frac{c (b g - a h) (c + d x)}{(-d g + c h)^2 (a + b x)} + \frac{a (c + d x)}{(-d g + c h) (a + b x)} \right) \right. \\
 & \quad \left. \text{Log} \left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)} \right] \right) / \left((b g - a h)^2 (c + d x) \right) \Bigg)
 \end{aligned}$$

$$\begin{aligned}
& \left(\text{Log} \left[\frac{-b c + a d}{d (a + b x)} \right] + \text{Log} \left[\frac{b (g + h x)}{b g - a h} \right] - \text{Log} \left[-\frac{(-b c + a d) (g + h x)}{(-d g + c h) (a + b x)} \right] \right) + \\
& \frac{(b g - a h)^2 \left(-\frac{a h (a + b x)}{(b g - a h)^2} - \frac{a + b x}{b g - a h} \right)^2 \text{Log} \left[1 + \frac{h (a + b x)}{b g - a h} \right]}{h^2 (a + b x)^2} + \frac{1}{h (c + d x)^2} (-d g + c h) \\
& \left(-\frac{a h (a + b x)}{(b g - a h)^2} - \frac{a + b x}{b g - a h} \right) \left(\frac{c (b g - a h) (c + d x)}{(-d g + c h)^2 (a + b x)} + \frac{a (c + d x)}{(-d g + c h) (a + b x)} \right) \\
& \text{Log} \left[1 + \frac{h (a + b x)}{b g - a h} \right] + \left(\text{Log} [c + d x] - \text{Log} \left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)} \right] \right) \\
& \left(\frac{(b g - a h) \left(-\frac{a h (a + b x)}{(b g - a h)^2} - \frac{a + b x}{b g - a h} \right) \left(\frac{a h (a + b x)}{(b g - a h)^2} + \frac{a + b x}{b g - a h} \right)}{h (a + b x) \left(1 + \frac{h (a + b x)}{b g - a h} \right)} + \right. \\
& \left. \frac{(b g - a h) \left(-\frac{2 a^2 h (a + b x)}{(b g - a h)^3} - \frac{2 a (a + b x)}{(b g - a h)^2} \right) \text{Log} \left[1 + \frac{h (a + b x)}{b g - a h} \right]}{h (a + b x)} - \right. \\
& \left. \frac{a \left(-\frac{a h (a + b x)}{(b g - a h)^2} - \frac{a + b x}{b g - a h} \right) \text{Log} \left[1 + \frac{h (a + b x)}{b g - a h} \right]}{h (a + b x)} - \right. \\
& \left. \frac{(b g - a h) \left(-\frac{a h (a + b x)}{(b g - a h)^2} - \frac{a + b x}{b g - a h} \right) \text{Log} \left[1 + \frac{h (a + b x)}{b g - a h} \right]}{h^2 (a + b x)} \right) + \\
& \frac{(-d g + c h)^2 \left(-\frac{c h (c + d x)}{(-d g + c h)^2} + \frac{c + d x}{-d g + c h} \right)^2 \text{Log} \left[1 - \frac{h (c + d x)}{-d g + c h} \right]}{h^2 (c + d x)^2} + \\
& \left(2 (-d g + c h)^2 (a + b x) \left(-\frac{c h (c + d x)}{(-d g + c h)^2} + \frac{c + d x}{-d g + c h} \right) \right. \\
& \left. \left(\frac{c (b g - a h) (c + d x)}{(-d g + c h)^2 (a + b x)} + \frac{a (c + d x)}{(-d g + c h) (a + b x)} \right) \text{Log} \left[1 - \frac{h (c + d x)}{-d g + c h} \right] \right) / \\
& \left(h (b g - a h) (c + d x)^2 \right) + \left(\text{Log} [a + b x] + \text{Log} \left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)} \right] \right) \\
& \left(-\left(\left((-d g + c h) \left(\frac{c h (c + d x)}{(-d g + c h)^2} - \frac{c + d x}{-d g + c h} \right) \left(-\frac{c h (c + d x)}{(-d g + c h)^2} + \frac{c + d x}{-d g + c h} \right) \right) \right) / \right. \\
& \left. \left(h (c + d x) \left(1 - \frac{h (c + d x)}{-d g + c h} \right) \right) \right) - \\
& \frac{(-d g + c h) \left(\frac{2 c^2 h (c + d x)}{(-d g + c h)^3} - \frac{2 c (c + d x)}{(-d g + c h)^2} \right) \text{Log} \left[1 - \frac{h (c + d x)}{-d g + c h} \right]}{h (c + d x)} - \\
& \frac{c \left(-\frac{c h (c + d x)}{(-d g + c h)^2} + \frac{c + d x}{-d g + c h} \right) \text{Log} \left[1 - \frac{h (c + d x)}{-d g + c h} \right]}{h (c + d x)} +
\end{aligned}$$

$$\begin{aligned}
 & \left. \frac{(-d g + c h) \left(-\frac{c h (c+d x)}{(-d g + c h)^2} + \frac{c+d x}{-d g + c h} \right) \text{Log}\left[1 - \frac{h (c+d x)}{-d g + c h}\right]}{h^2 (c+d x)} \right) + \\
 & \left((-d g + c h)^2 (a+b x)^2 \left(\frac{c (b g - a h) (c+d x)}{(-d g + c h)^2 (a+b x)} + \frac{a (c+d x)}{(-d g + c h) (a+b x)} \right) \right)^2 \\
 & \text{Log}\left[1 + \frac{(b g - a h) (c+d x)}{(-d g + c h) (a+b x)}\right] \Big/ \left((b g - a h)^2 (c+d x)^2 \right) + \\
 & \text{Log}\left[-\frac{(b g - a h) (c+d x)}{(-d g + c h) (a+b x)}\right] \left(-\left(\left((-d g + c h) (a+b x) \left(-\frac{c (b g - a h) (c+d x)}{(-d g + c h)^2 (a+b x)} - \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{a (c+d x)}{(-d g + c h) (a+b x)} \right) \left(\frac{c (b g - a h) (c+d x)}{(-d g + c h)^2 (a+b x)} + \frac{a (c+d x)}{(-d g + c h) (a+b x)} \right) \right) \right) \Big/ \\
 & \quad \left((b g - a h) (c+d x) \left(1 + \frac{(b g - a h) (c+d x)}{(-d g + c h) (a+b x)} \right) \right) \Big) - \\
 & \left((-d g + c h) (a+b x) \left(-\frac{2 c^2 (b g - a h) (c+d x)}{(-d g + c h)^3 (a+b x)} - \frac{2 a c (c+d x)}{(-d g + c h)^2 (a+b x)} \right) \right) \\
 & \text{Log}\left[1 + \frac{(b g - a h) (c+d x)}{(-d g + c h) (a+b x)}\right] \Big/ \left((b g - a h) (c+d x) \right) - \\
 & \left(c (a+b x) \left(\frac{c (b g - a h) (c+d x)}{(-d g + c h)^2 (a+b x)} + \frac{a (c+d x)}{(-d g + c h) (a+b x)} \right) \right) \\
 & \text{Log}\left[1 + \frac{(b g - a h) (c+d x)}{(-d g + c h) (a+b x)}\right] \Big/ \left((b g - a h) (c+d x) \right) - \\
 & \left(a (-d g + c h) (a+b x) \left(\frac{c (b g - a h) (c+d x)}{(-d g + c h)^2 (a+b x)} + \frac{a (c+d x)}{(-d g + c h) (a+b x)} \right) \right) \\
 & \text{Log}\left[1 + \frac{(b g - a h) (c+d x)}{(-d g + c h) (a+b x)}\right] \Big/ \left((b g - a h)^2 (c+d x) \right) \Big) + \\
 & \frac{(b g - a h) \left(-\frac{2 a^2 h (a+b x)}{(b g - a h)^3} - \frac{2 a (a+b x)}{(b g - a h)^2} \right) \text{PolyLog}\left[2, -\frac{h (a+b x)}{b g - a h}\right]}{h (a+b x)} - \\
 & \frac{a \left(-\frac{a h (a+b x)}{(b g - a h)^2} - \frac{a+b x}{b g - a h} \right) \text{PolyLog}\left[2, -\frac{h (a+b x)}{b g - a h}\right]}{h (a+b x)} - \\
 & \frac{(b g - a h) \left(-\frac{a h (a+b x)}{(b g - a h)^2} - \frac{a+b x}{b g - a h} \right) \text{PolyLog}\left[2, -\frac{h (a+b x)}{b g - a h}\right]}{h^2 (a+b x)} + \\
 & \left(\left((-d g + c h) (a+b x) \left(-\frac{2 c^2 (b g - a h) (c+d x)}{(-d g + c h)^3 (a+b x)} - \frac{2 a c (c+d x)}{(-d g + c h)^2 (a+b x)} \right) \right) \right) \Big/ \\
 & \quad \left((b g - a h) (c+d x) \right) + \frac{c (a+b x) \left(\frac{c (b g - a h) (c+d x)}{(-d g + c h)^2 (a+b x)} + \frac{a (c+d x)}{(-d g + c h) (a+b x)} \right)}{(b g - a h) (c+d x)} +
 \end{aligned}$$

$$\begin{aligned}
 & \left(a (-d g + c h) (a + b x) \left(\frac{c (b g - a h) (c + d x)}{(-d g + c h)^2 (a + b x)} + \frac{a (c + d x)}{(-d g + c h) (a + b x)} \right) \right) / \\
 & \left((b g - a h)^2 (c + d x) \right) \text{PolyLog}\left[2, -\frac{h (a + b x)}{b g - a h}\right] - \\
 & \frac{(-d g + c h) \left(\frac{2 c^2 h (c + d x)}{(-d g + c h)^3} - \frac{2 c (c + d x)}{(-d g + c h)^2} \right) \text{PolyLog}\left[2, \frac{h (c + d x)}{-d g + c h}\right]}{h (c + d x)} - \\
 & \frac{c \left(-\frac{c h (c + d x)}{(-d g + c h)^2} + \frac{c + d x}{-d g + c h} \right) \text{PolyLog}\left[2, \frac{h (c + d x)}{-d g + c h}\right]}{h (c + d x)} + \\
 & \frac{(-d g + c h) \left(-\frac{c h (c + d x)}{(-d g + c h)^2} + \frac{c + d x}{-d g + c h} \right) \text{PolyLog}\left[2, \frac{h (c + d x)}{-d g + c h}\right]}{h^2 (c + d x)} + \\
 & \left(- \left(\left((-d g + c h) (a + b x) \left(-\frac{2 c^2 (b g - a h) (c + d x)}{(-d g + c h)^3 (a + b x)} - \frac{2 a c (c + d x)}{(-d g + c h)^2 (a + b x)} \right) \right) / \right. \right. \\
 & \left. \left. (b g - a h) (c + d x) \right) - \frac{c (a + b x) \left(\frac{c (b g - a h) (c + d x)}{(-d g + c h)^2 (a + b x)} + \frac{a (c + d x)}{(-d g + c h) (a + b x)} \right)}{(b g - a h) (c + d x)} - \right. \\
 & \left. \left(a (-d g + c h) (a + b x) \left(\frac{c (b g - a h) (c + d x)}{(-d g + c h)^2 (a + b x)} + \frac{a (c + d x)}{(-d g + c h) (a + b x)} \right) \right) / \right. \\
 & \left. \left((b g - a h)^2 (c + d x) \right) \text{PolyLog}\left[2, \frac{h (c + d x)}{-d g + c h}\right] + \right. \\
 & \left(- \left(\left((-d g + c h) (a + b x) \left(-\frac{2 c^2 (b g - a h) (c + d x)}{(-d g + c h)^3 (a + b x)} - \frac{2 a c (c + d x)}{(-d g + c h)^2 (a + b x)} \right) \right) / \right. \right. \\
 & \left. \left. (b g - a h) (c + d x) \right) - \frac{c (a + b x) \left(\frac{c (b g - a h) (c + d x)}{(-d g + c h)^2 (a + b x)} + \frac{a (c + d x)}{(-d g + c h) (a + b x)} \right)}{(b g - a h) (c + d x)} - \right. \\
 & \left. \left(a (-d g + c h) (a + b x) \left(\frac{c (b g - a h) (c + d x)}{(-d g + c h)^2 (a + b x)} + \frac{a (c + d x)}{(-d g + c h) (a + b x)} \right) \right) / \right. \\
 & \left. \left((b g - a h)^2 (c + d x) \right) \right) \\
 & \left(\text{PolyLog}\left[2, \frac{b (c + d x)}{d (a + b x)}\right] - \text{PolyLog}\left[2, -\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)}\right] \right) - \\
 & \left((-d g + c h) (a + b x) \left(-\frac{2 c^2 (b g - a h) (c + d x)}{(-d g + c h)^3 (a + b x)} - \frac{2 a c (c + d x)}{(-d g + c h)^2 (a + b x)} \right) \right. \\
 & \left. \text{PolyLog}\left[2, -\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)}\right] \right) / ((b g - a h) (c + d x)) -
 \end{aligned}$$

$$\begin{aligned}
 & \left(c (a+b x) \left(\frac{c (b g-a h) (c+d x)}{(-d g+c h)^2 (a+b x)} + \frac{a (c+d x)}{(-d g+c h) (a+b x)} \right) \right. \\
 & \quad \left. \text{PolyLog}\left[2, -\frac{(b g-a h) (c+d x)}{(-d g+c h) (a+b x)}\right] \right) / \left((b g-a h) (c+d x) - \right. \\
 & \quad \left. \left(a (-d g+c h) (a+b x) \left(\frac{c (b g-a h) (c+d x)}{(-d g+c h)^2 (a+b x)} + \frac{a (c+d x)}{(-d g+c h) (a+b x)} \right) \right) \right. \\
 & \quad \left. \text{PolyLog}\left[2, -\frac{(b g-a h) (c+d x)}{(-d g+c h) (a+b x)}\right] \right) / \left((b g-a h)^2 (c+d x) \right) \Bigg) - \\
 & \frac{1}{h^2} 2 \left(\frac{(b g-a h) \left(\frac{b x}{b g-a h} + \frac{a b (g+h x)}{(b g-a h)^2} \right) \text{Log}[a+b x] \text{Log}[c+d x]}{b (g+h x)} + \right. \\
 & \quad \frac{1}{2} \left(\frac{(b g-a h) \left(\frac{b x}{b g-a h} + \frac{a b (g+h x)}{(b g-a h)^2} \right)}{b (g+h x)} + \frac{(-d g+c h) \left(-\frac{d x}{-d g+c h} + \frac{c d (g+h x)}{(-d g+c h)^2} \right)}{d (g+h x)} \right) \\
 & \quad \text{Log}\left[\frac{h (c+d x)}{-d g+c h}\right] \left(-2 \text{Log}[a+b x] + \text{Log}\left[\frac{h (c+d x)}{-d g+c h}\right] \right) + \\
 & \quad \left(-\frac{(b g-a h) \left(\frac{b x}{b g-a h} + \frac{a b (g+h x)}{(b g-a h)^2} \right)}{b (g+h x)} - \frac{(-d g+c h) \left(-\frac{d x}{-d g+c h} + \frac{c d (g+h x)}{(-d g+c h)^2} \right)}{d (g+h x)} \right) \\
 & \quad \text{Log}\left[\frac{h (c+d x)}{-d g+c h}\right] \text{Log}\left[-\frac{(b g-a h) (c+d x)}{(-d g+c h) (a+b x)}\right] + \frac{1}{2} \left(\frac{(b g-a h) \left(\frac{b x}{b g-a h} + \frac{a b (g+h x)}{(b g-a h)^2} \right)}{b (g+h x)} + \right. \\
 & \quad \left. \left((-d g+c h) (a+b x) \left(-\frac{(-b c+a d) x}{(-d g+c h) (a+b x)} + \frac{c (-b c+a d) (g+h x)}{(-d g+c h)^2 (a+b x)} \right) \right) / \right. \\
 & \quad \left. \left((-b c+a d) (g+h x) \right) \right) \text{Log}\left[-\frac{(b g-a h) (c+d x)}{(-d g+c h) (a+b x)}\right]^2 + \\
 & \quad \frac{1}{2 h (c+d x)} (-d g+c h) \left(-\frac{c h (c+d x)}{(-d g+c h)^2} + \frac{c+d x}{-d g+c h} \right) \text{Log}\left[\frac{h (c+d x)}{-d g+c h}\right] \\
 & \quad \left(\text{Log}\left[\frac{b (g+h x)}{b g-a h}\right] - \text{Log}\left[-\frac{d (g+h x)}{-d g+c h}\right] \right) + \frac{1}{2 h (c+d x)} \\
 & \quad (-d g+c h) \left(-\frac{c h (c+d x)}{(-d g+c h)^2} + \frac{c+d x}{-d g+c h} \right) \left(-2 \text{Log}[a+b x] + \text{Log}\left[\frac{h (c+d x)}{-d g+c h}\right] \right) \\
 & \quad \left(\text{Log}\left[\frac{b (g+h x)}{b g-a h}\right] - \text{Log}\left[-\frac{d (g+h x)}{-d g+c h}\right] \right) - \\
 & \quad \left((-d g+c h) (a+b x) \left(\frac{c (b g-a h) (c+d x)}{(-d g+c h)^2 (a+b x)} + \frac{a (c+d x)}{(-d g+c h) (a+b x)} \right) \right) \text{Log}\left[\right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{h(c+dx)}{-dg+ch} \left(-\text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \text{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right] \right) \Big/ ((bg-ah)(c+dx)) + \\
 & \frac{1}{h(c+dx)} (-dg+ch) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \\
 & \left(-\text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \text{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right] \right) - \\
 & \left((-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \text{Log}\left[\right. \right. \\
 & \quad \left. \left. -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right] \left(\text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] + \text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - \right. \right. \\
 & \quad \left. \left. \text{Log}\left[-\frac{(-bc+ad)(g+hx)}{(-dg+ch)(a+bx)}\right] \right) \right) \Big/ ((bg-ah)(c+dx)) + \frac{1}{h(a+bx)} \\
 & (bg-ah) \left(-\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah} \right) \left(\text{Log}[c+dx] - \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) \\
 & \text{Log}\left[1 + \frac{h(a+bx)}{bg-ah}\right] - \frac{1}{h(c+dx)} (-dg+ch) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \\
 & \left(\text{Log}[a+bx] + \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) \text{Log}\left[1 - \frac{h(c+dx)}{-dg+ch}\right] - \\
 & \left((-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \text{Log}\left[\right. \right. \\
 & \quad \left. \left. -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right] \text{Log}\left[1 + \frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) \Big/ ((bg-ah)(c+dx)) + \\
 & \frac{(bg-ah) \left(-\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah} \right) \text{PolyLog}\left[2, -\frac{h(a+bx)}{bg-ah}\right]}{h(a+bx)} + \left((-dg+ch)(a+bx) \right. \\
 & \quad \left. \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \text{PolyLog}\left[2, -\frac{h(a+bx)}{bg-ah}\right] \right) \Big/ \\
 & ((bg-ah)(c+dx)) - \frac{(-dg+ch) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \text{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right]}{h(c+dx)} - \\
 & \left((-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \right. \\
 & \quad \left. \text{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right] \right) \Big/ ((bg-ah)(c+dx)) - \\
 & \left((-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \left(\text{PolyLog}\left[2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b(c+dx)}{d(a+bx)} \right] - \text{PolyLog}\left[2, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) \Big/ ((bg-ah)(c+dx)) -
 \end{aligned}$$

$$\begin{aligned}
 & \left((-d g + c h) (a + b x) \left(\frac{c (b g - a h) (c + d x)}{(-d g + c h)^2 (a + b x)} + \frac{a (c + d x)}{(-d g + c h) (a + b x)} \right) \right. \\
 & \quad \left. \text{PolyLog}\left[2, -\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)}\right] \right) / ((b g - a h) (c + d x)) + \\
 & \frac{1}{h^3} 2 \left(\text{Log}[a + b x] \text{Log}[c + d x] \text{Log}\left[\frac{b (g + h x)}{b g - a h}\right] + \frac{1}{2} \text{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] \right. \\
 & \quad \left(-2 \text{Log}[a + b x] + \text{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] \right) \left(\text{Log}\left[\frac{b (g + h x)}{b g - a h}\right] - \text{Log}\left[-\frac{d (g + h x)}{-d g + c h}\right] \right) + \\
 & \quad \text{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] \text{Log}\left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)}\right] \\
 & \quad \left(-\text{Log}\left[\frac{b (g + h x)}{b g - a h}\right] + \text{Log}\left[-\frac{d (g + h x)}{-d g + c h}\right] \right) + \frac{1}{2} \text{Log}\left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)}\right]^2 \\
 & \quad \left(\text{Log}\left[\frac{-b c + a d}{d (a + b x)}\right] + \text{Log}\left[\frac{b (g + h x)}{b g - a h}\right] - \text{Log}\left[-\frac{(-b c + a d) (g + h x)}{(-d g + c h) (a + b x)}\right] \right) + \\
 & \quad \left(\text{Log}[c + d x] - \text{Log}\left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)}\right] \right) \text{PolyLog}\left[2, -\frac{h (a + b x)}{b g - a h}\right] + \\
 & \quad \left(\text{Log}[a + b x] + \text{Log}\left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)}\right] \right) \text{PolyLog}\left[2, \frac{h (c + d x)}{-d g + c h}\right] + \\
 & \quad \text{Log}\left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)}\right] \left(\text{PolyLog}\left[2, \frac{b (c + d x)}{d (a + b x)}\right] - \text{PolyLog}\left[2, \right. \right. \\
 & \quad \left. \left. -\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)}\right] - \text{PolyLog}\left[3, -\frac{h (a + b x)}{b g - a h}\right] - \text{PolyLog}\left[3, \frac{h (c + d x)}{-d g + c h}\right] - \right. \\
 & \quad \left. \text{PolyLog}\left[3, \frac{b (c + d x)}{d (a + b x)}\right] + \text{PolyLog}\left[3, -\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)}\right] \right) \left. \right) + \\
 & 4 h \left(\frac{1}{h} \left(\frac{(b g - a h) \left(\frac{b x}{b g - a h} + \frac{a b (g + h x)}{(b g - a h)^2} \right) \text{Log}[a + b x] \text{Log}[c + d x]}{b (g + h x)} + \right. \right. \\
 & \quad \left. \frac{1}{2} \left(\frac{(b g - a h) \left(\frac{b x}{b g - a h} + \frac{a b (g + h x)}{(b g - a h)^2} \right)}{b (g + h x)} + \frac{(-d g + c h) \left(-\frac{d x}{-d g + c h} + \frac{c d (g + h x)}{(-d g + c h)^2} \right)}{d (g + h x)} \right) \right. \\
 & \quad \left. \text{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] \left(-2 \text{Log}[a + b x] + \text{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] \right) + \right. \\
 & \quad \left(-\frac{(b g - a h) \left(\frac{b x}{b g - a h} + \frac{a b (g + h x)}{(b g - a h)^2} \right)}{b (g + h x)} - \frac{(-d g + c h) \left(-\frac{d x}{-d g + c h} + \frac{c d (g + h x)}{(-d g + c h)^2} \right)}{d (g + h x)} \right) \\
 & \quad \left. \text{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] \text{Log}\left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)}\right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{2} \left(\frac{(b g - a h) \left(\frac{b x}{b g - a h} + \frac{a b (g + h x)}{(b g - a h)^2} \right)}{b (g + h x)} + \left((-d g + c h) (a + b x) \right. \right. \\
 & \quad \left. \left. \left(-\frac{(-b c + a d) x}{(-d g + c h) (a + b x)} + \frac{c (-b c + a d) (g + h x)}{(-d g + c h)^2 (a + b x)} \right) \right) / \left((-b c + a d) (g + h x) \right) \right) \\
 & \text{Log} \left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)} \right]^2 + \frac{1}{2 h (c + d x)} (-d g + c h) \left(-\frac{c h (c + d x)}{(-d g + c h)^2} + \frac{c + d x}{-d g + c h} \right) \\
 & \text{Log} \left[\frac{h (c + d x)}{-d g + c h} \right] \left(\text{Log} \left[\frac{b (g + h x)}{b g - a h} \right] - \text{Log} \left[-\frac{d (g + h x)}{-d g + c h} \right] \right) + \\
 & \frac{1}{2 h (c + d x)} (-d g + c h) \left(-\frac{c h (c + d x)}{(-d g + c h)^2} + \frac{c + d x}{-d g + c h} \right) \\
 & \left(-2 \text{Log} [a + b x] + \text{Log} \left[\frac{h (c + d x)}{-d g + c h} \right] \right) \left(\text{Log} \left[\frac{b (g + h x)}{b g - a h} \right] - \text{Log} \left[-\frac{d (g + h x)}{-d g + c h} \right] \right) - \\
 & \left((-d g + c h) (a + b x) \left(\frac{c (b g - a h) (c + d x)}{(-d g + c h)^2 (a + b x)} + \frac{a (c + d x)}{(-d g + c h) (a + b x)} \right) \text{Log} \left[\frac{h (c + d x)}{-d g + c h} \right] \right. \\
 & \quad \left. \left(-\text{Log} \left[\frac{b (g + h x)}{b g - a h} \right] + \text{Log} \left[-\frac{d (g + h x)}{-d g + c h} \right] \right) \right) / \left((b g - a h) (c + d x) \right) + \frac{1}{h (c + d x)} \\
 & (-d g + c h) \left(-\frac{c h (c + d x)}{(-d g + c h)^2} + \frac{c + d x}{-d g + c h} \right) \text{Log} \left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)} \right] \\
 & \left(-\text{Log} \left[\frac{b (g + h x)}{b g - a h} \right] + \text{Log} \left[-\frac{d (g + h x)}{-d g + c h} \right] \right) - \left((-d g + c h) (a + b x) \right. \\
 & \quad \left. \left(\frac{c (b g - a h) (c + d x)}{(-d g + c h)^2 (a + b x)} + \frac{a (c + d x)}{(-d g + c h) (a + b x)} \right) \text{Log} \left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)} \right] \right. \\
 & \quad \left. \left(\text{Log} \left[\frac{-b c + a d}{d (a + b x)} \right] + \text{Log} \left[\frac{b (g + h x)}{b g - a h} \right] - \text{Log} \left[-\frac{(-b c + a d) (g + h x)}{(-d g + c h) (a + b x)} \right] \right) \right) / \\
 & \left((b g - a h) (c + d x) \right) + \frac{1}{h (a + b x)} (b g - a h) \left(-\frac{a h (a + b x)}{(b g - a h)^2} - \frac{a + b x}{b g - a h} \right) \\
 & \left(\text{Log} [c + d x] - \text{Log} \left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)} \right] \right) \text{Log} \left[1 + \frac{h (a + b x)}{b g - a h} \right] - \\
 & \frac{1}{h (c + d x)} (-d g + c h) \left(-\frac{c h (c + d x)}{(-d g + c h)^2} + \frac{c + d x}{-d g + c h} \right) \\
 & \left(\text{Log} [a + b x] + \text{Log} \left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)} \right] \right) \text{Log} \left[1 - \frac{h (c + d x)}{-d g + c h} \right] - \\
 & \left((-d g + c h) (a + b x) \left(\frac{c (b g - a h) (c + d x)}{(-d g + c h)^2 (a + b x)} + \frac{a (c + d x)}{(-d g + c h) (a + b x)} \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{Log}\left[-\frac{(b g-a h)(c+d x)}{(-d g+c h)(a+b x)}\right] \text{Log}\left[1+\frac{(b g-a h)(c+d x)}{(-d g+c h)(a+b x)}\right]\right\} / \\
 & \left((b g-a h)(c+d x) + \frac{(b g-a h)\left(-\frac{a h(a+b x)}{(b g-a h)^2}-\frac{a+b x}{b g-a h}\right) \text{PolyLog}\left[2,-\frac{h(a+b x)}{b g-a h}\right]}{h(a+b x)} + \right. \\
 & \left. \left((-d g+c h)(a+b x) \left(\frac{c(b g-a h)(c+d x)}{(-d g+c h)^2(a+b x)} + \frac{a(c+d x)}{(-d g+c h)(a+b x)} \right) \right. \right. \\
 & \left. \left. \text{PolyLog}\left[2,-\frac{h(a+b x)}{b g-a h}\right]\right)\right\} / \left((b g-a h)(c+d x) - \right. \\
 & \left. \frac{(-d g+c h)\left(-\frac{c h(c+d x)}{(-d g+c h)^2}+\frac{c+d x}{-d g+c h}\right) \text{PolyLog}\left[2,\frac{h(c+d x)}{-d g+c h}\right]}{h(c+d x)} - \right. \\
 & \left. \left((-d g+c h)(a+b x) \left(\frac{c(b g-a h)(c+d x)}{(-d g+c h)^2(a+b x)} + \frac{a(c+d x)}{(-d g+c h)(a+b x)} \right) \right. \right. \\
 & \left. \left. \text{PolyLog}\left[2,\frac{h(c+d x)}{-d g+c h}\right]\right)\right\} / \left((b g-a h)(c+d x) - \right. \\
 & \left. \left((-d g+c h)(a+b x) \left(\frac{c(b g-a h)(c+d x)}{(-d g+c h)^2(a+b x)} + \frac{a(c+d x)}{(-d g+c h)(a+b x)} \right) \right) \left(\text{PolyLog}\left[2,\right. \right. \right. \\
 & \left. \left. \left. \frac{b(c+d x)}{d(a+b x)}\right] - \text{PolyLog}\left[2,-\frac{(b g-a h)(c+d x)}{(-d g+c h)(a+b x)}\right]\right)\right\} / \left((b g-a h)(c+d x) - \right. \\
 & \left. \left((-d g+c h)(a+b x) \left(\frac{c(b g-a h)(c+d x)}{(-d g+c h)^2(a+b x)} + \frac{a(c+d x)}{(-d g+c h)(a+b x)} \right) \right. \right. \\
 & \left. \left. \text{PolyLog}\left[2,-\frac{(b g-a h)(c+d x)}{(-d g+c h)(a+b x)}\right]\right)\right\} / \left((b g-a h)(c+d x) \right) - \\
 & \frac{1}{h^2} \left(\text{Log}[a+b x] \text{Log}[c+d x] \text{Log}\left[\frac{b(g+h x)}{b g-a h}\right] + \frac{1}{2} \text{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \right. \\
 & \left. \left(-2 \text{Log}[a+b x] + \text{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \right) \left(\text{Log}\left[\frac{b(g+h x)}{b g-a h}\right] - \text{Log}\left[-\frac{d(g+h x)}{-d g+c h}\right] \right) + \right. \\
 & \left. \text{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \text{Log}\left[-\frac{(b g-a h)(c+d x)}{(-d g+c h)(a+b x)}\right] \right. \\
 & \left. \left(-\text{Log}\left[\frac{b(g+h x)}{b g-a h}\right] + \text{Log}\left[-\frac{d(g+h x)}{-d g+c h}\right] \right) + \frac{1}{2} \text{Log}\left[-\frac{(b g-a h)(c+d x)}{(-d g+c h)(a+b x)}\right]^2 \right. \\
 & \left. \left(\text{Log}\left[\frac{-b c+a d}{d(a+b x)}\right] + \text{Log}\left[\frac{b(g+h x)}{b g-a h}\right] - \text{Log}\left[-\frac{(-b c+a d)(g+h x)}{(-d g+c h)(a+b x)}\right] \right) + \right. \\
 & \left. \left(\text{Log}[c+d x] - \text{Log}\left[-\frac{(b g-a h)(c+d x)}{(-d g+c h)(a+b x)}\right] \right) \text{PolyLog}\left[2,-\frac{h(a+b x)}{b g-a h}\right] + \right. \\
 & \left. \left(\text{Log}[a+b x] + \text{Log}\left[-\frac{(b g-a h)(c+d x)}{(-d g+c h)(a+b x)}\right] \right) \text{PolyLog}\left[2,\frac{h(c+d x)}{-d g+c h}\right] + \right.
 \end{aligned}$$

$$\begin{aligned} & \text{Log}\left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)}\right] \\ & \left(\text{PolyLog}\left[2, \frac{b (c + d x)}{d (a + b x)}\right] - \text{PolyLog}\left[2, -\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)}\right] \right) - \\ & \text{PolyLog}\left[3, -\frac{h (a + b x)}{b g - a h}\right] - \text{PolyLog}\left[3, \frac{h (c + d x)}{-d g + c h}\right] - \\ & \left. \text{PolyLog}\left[3, \frac{b (c + d x)}{d (a + b x)}\right] + \text{PolyLog}\left[3, -\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)}\right] \right) \end{aligned}$$

Problem 309: Result more than twice size of optimal antiderivative.

$$\int (g + h x)^2 (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^3 dx$$

Optimal (type 4, 875 leaves, 19 steps):

$$\begin{aligned}
 & - \frac{B^3 (b c - a d)^3 h^2 n^3 \text{Log}[c + d x]}{b^3 d^3} + \\
 & \frac{B^2 (b c - a d)^2 h^2 n^2 (a + b x) (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])}{b^3 d^2} - \frac{1}{b^3 d^3} \\
 & 2 B^2 (b c - a d)^2 h (3 b d g - 2 b c h - a d h) n^2 \text{Log}\left[\frac{b c - a d}{b (c + d x)}\right] (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}]) - \\
 & \frac{1}{b^3 d^2} B (b c - a d) h (3 b d g - 2 b c h - a d h) n (a + b x) (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^2 - \\
 & \frac{B (b c - a d) h^2 n (c + d x)^2 (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{2 b d^3} + \frac{1}{b^3 d^3} \\
 & B (b c - a d) (a^2 d^2 h^2 - a b d h (3 d g - c h) + b^2 (3 d^2 g^2 - 3 c d g h + c^2 h^2)) \\
 & n \text{Log}\left[\frac{b c - a d}{b (c + d x)}\right] (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^2 - \\
 & \frac{(b g - a h)^3 (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^3}{3 b^3 h} + \frac{(g + h x)^3 (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^3}{3 h} - \\
 & \frac{1}{b^3 d^3} B^2 (b c - a d)^3 h^2 n^2 (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}]) \text{Log}\left[1 - \frac{b (c + d x)}{d (a + b x)}\right] - \\
 & \frac{2 B^3 (b c - a d)^2 h (3 b d g - 2 b c h - a d h) n^3 \text{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]}{b^3 d^3} + \frac{1}{b^3 d^3} \\
 & 2 B^2 (b c - a d) (a^2 d^2 h^2 - a b d h (3 d g - c h) + b^2 (3 d^2 g^2 - 3 c d g h + c^2 h^2)) \\
 & n^2 (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}]) \text{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right] + \\
 & \frac{B^3 (b c - a d)^3 h^2 n^3 \text{PolyLog}\left[2, \frac{b (c + d x)}{d (a + b x)}\right]}{b^3 d^3} - \frac{1}{b^3 d^3} 2 B^3 (b c - a d) \\
 & (a^2 d^2 h^2 - a b d h (3 d g - c h) + b^2 (3 d^2 g^2 - 3 c d g h + c^2 h^2)) n^3 \text{PolyLog}\left[3, \frac{d (a + b x)}{b (c + d x)}\right]
 \end{aligned}$$

Result (type 4, 7328 leaves):

$$\begin{aligned}
 & - \frac{6 a A B^2 g^2 n^2}{b} - \frac{6 A B^2 c g^2 n^2}{d} + \frac{12 a A B^2 c g h n^2}{b d} - \frac{2 a A B^2 c^2 h^2 n^2}{b d^2} - \frac{2 a^2 A B^2 c h^2 n^2}{b^2 d} + \\
 & \frac{6 a B^3 g^2 n^3}{b} - \frac{6 a^2 B^3 g h n^3}{b^2} - \frac{6 B^3 c^2 g h n^3}{d^2} + \frac{6 a B^3 c g h n^3}{b d} + \frac{2 a^3 B^3 h^2 n^3}{b^3} + \frac{2 B^3 c^3 h^2 n^3}{d^3} - \\
 & \frac{a B^3 c^2 h^2 n^3}{b d^2} - \frac{a^2 B^3 c h^2 n^3}{b^2 d} + A^3 g^2 x + \frac{3 a A^2 B g h n x}{b} - \frac{3 A^2 B c g h n x}{d} - \frac{a^2 A^2 B h^2 n x}{b^2} + \\
 & \frac{A^2 B c^2 h^2 n x}{d^2} + \frac{a^2 A B^2 h^2 n^2 x}{b^2} + \frac{A B^2 c^2 h^2 n^2 x}{d^2} - \frac{2 a A B^2 c h^2 n^2 x}{b d} + A^3 g h x^2 + \frac{a A^2 B h^2 n x^2}{2 b} - \\
 & \frac{A^2 B c h^2 n x^2}{2 d} + \frac{1}{3} A^3 h^2 x^3 + \frac{3 a A^2 B g^2 n \text{Log}[a + b x]}{b} - \frac{3 a^2 A^2 B g h n \text{Log}[a + b x]}{b^2} + \\
 & \frac{a^3 A^2 B h^2 n \text{Log}[a + b x]}{b^3} + \frac{6 a^2 A B^2 g h n^2 \text{Log}[a + b x]}{b^2} - \frac{6 a A B^2 c g h n^2 \text{Log}[a + b x]}{b d} - \\
 & \frac{3 a^3 A B^2 h^2 n^2 \text{Log}[a + b x]}{b^3} + \frac{2 a A B^2 c^2 h^2 n^2 \text{Log}[a + b x]}{b d^2} + \frac{a^2 A B^2 c h^2 n^2 \text{Log}[a + b x]}{b^2 d} +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{6 a B^3 g^2 n^3 \operatorname{Log}[a+b x]}{b} + \frac{6 B^3 c g^2 n^3 \operatorname{Log}[a+b x]}{d} - \frac{12 a B^3 c g h n^3 \operatorname{Log}[a+b x]}{b d} + \\
 & \frac{a^3 B^3 h^2 n^3 \operatorname{Log}[a+b x]}{b^3} + \frac{3 a B^3 c^2 h^2 n^3 \operatorname{Log}[a+b x]}{b d^2} - \frac{3 a A B^2 g^2 n^2 \operatorname{Log}[a+b x]^2}{b} + \\
 & \frac{3 a^2 A B^2 g h n^2 \operatorname{Log}[a+b x]^2}{b^2} - \frac{a^3 A B^2 h^2 n^2 \operatorname{Log}[a+b x]^2}{b^3} - \frac{3 a^2 B^3 g h n^3 \operatorname{Log}[a+b x]^2}{b^2} + \\
 & \frac{3 a B^3 c g h n^3 \operatorname{Log}[a+b x]^2}{b d} + \frac{3 a^3 B^3 h^2 n^3 \operatorname{Log}[a+b x]^2}{2 b^3} - \frac{a B^3 c^2 h^2 n^3 \operatorname{Log}[a+b x]^2}{b d^2} - \\
 & \frac{a^2 B^3 c h^2 n^3 \operatorname{Log}[a+b x]^2}{2 b^2 d} + \frac{a B^3 g^2 n^3 \operatorname{Log}[a+b x]^3}{b} - \frac{a^2 B^3 g h n^3 \operatorname{Log}[a+b x]^3}{b^2} + \\
 & \frac{a^3 B^3 h^2 n^3 \operatorname{Log}[a+b x]^3}{3 b^3} - \frac{3 A^2 B c g^2 n \operatorname{Log}[c+d x]}{d} + \frac{3 A^2 B c^2 g h n \operatorname{Log}[c+d x]}{d^2} - \\
 & \frac{A^2 B c^3 h^2 n \operatorname{Log}[c+d x]}{d^3} + \frac{6 A B^2 c^2 g h n^2 \operatorname{Log}[c+d x]}{d^2} - \frac{6 a A B^2 c g h n^2 \operatorname{Log}[c+d x]}{b d} - \\
 & \frac{3 A B^2 c^3 h^2 n^2 \operatorname{Log}[c+d x]}{d^3} + \frac{a A B^2 c^2 h^2 n^2 \operatorname{Log}[c+d x]}{b d^2} + \frac{2 a^2 A B^2 c h^2 n^2 \operatorname{Log}[c+d x]}{b^2 d} - \\
 & \frac{6 a B^3 g^2 n^3 \operatorname{Log}[c+d x]}{b} - \frac{6 B^3 c g^2 n^3 \operatorname{Log}[c+d x]}{d} + \frac{12 a B^3 c g h n^3 \operatorname{Log}[c+d x]}{b d} - \\
 & \frac{B^3 c^3 h^2 n^3 \operatorname{Log}[c+d x]}{d^3} - \frac{3 a^2 B^3 c h^2 n^3 \operatorname{Log}[c+d x]}{b^2 d} + \frac{6 a A B^2 g^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]}{b} + \\
 & \frac{6 A B^2 c g^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]}{d} - \frac{6 a^2 A B^2 g h n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]}{b^2} - \\
 & \frac{6 A B^2 c^2 g h n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]}{d^2} + \frac{2 a^3 A B^2 h^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]}{b^3} + \\
 & \frac{2 A B^2 c^3 h^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]}{d^3} - \frac{6 B^3 c^2 g h n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]}{d^2} + \\
 & \frac{6 a B^3 c g h n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]}{b d} + \frac{3 B^3 c^3 h^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]}{d^3} - \\
 & \frac{a B^3 c^2 h^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]}{b d^2} - \frac{2 a^2 B^3 c h^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]}{b^2 d} - \\
 & \frac{6 a B^3 g^2 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x]}{b} - \frac{3 B^3 c g^2 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x]}{d} + \\
 & \frac{6 a^2 B^3 g h n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x]}{b^2} + \frac{3 B^3 c^2 g h n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x]}{d^2} - \\
 & \frac{2 a^3 B^3 h^2 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x]}{b^3} - \frac{B^3 c^3 h^2 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x]}{d^3} - \\
 & \frac{6 a A B^2 g^2 n^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]}{b} + \frac{6 a^2 A B^2 g h n^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]}{b^2} - \\
 & \frac{2 a^3 A B^2 h^2 n^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]}{b^3} + \frac{6 a B^3 g^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]}{b} - \\
 & \frac{6 a^2 B^3 g h n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]}{b^2} +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{2 a^3 B^3 h^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]}{b^3} - \frac{3 A B^2 c g^2 n^2 \operatorname{Log}[c+d x]^2}{d} + \\
 & \frac{3 A B^2 c^2 g h n^2 \operatorname{Log}[c+d x]^2}{d^2} - \frac{A B^2 c^3 h^2 n^2 \operatorname{Log}[c+d x]^2}{d^3} + \frac{3 B^3 c^2 g h n^3 \operatorname{Log}[c+d x]^2}{d^2} - \\
 & \frac{3 a B^3 c g h n^3 \operatorname{Log}[c+d x]^2}{b d} - \frac{3 B^3 c^3 h^2 n^3 \operatorname{Log}[c+d x]^2}{2 d^3} + \frac{a B^3 c^2 h^2 n^3 \operatorname{Log}[c+d x]^2}{2 b d^2} + \\
 & \frac{a^2 B^3 c h^2 n^3 \operatorname{Log}[c+d x]^2}{b^2 d} + \frac{3 a B^3 g^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2}{b} + \\
 & \frac{6 B^3 c g^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2}{d} - \frac{3 a^2 B^3 g h n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2}{b^2} - \\
 & \frac{6 B^3 c^2 g h n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2}{d^2} + \frac{a^3 B^3 h^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2}{b^3} + \\
 & \frac{2 B^3 c^3 h^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2}{d^3} - \frac{3 a B^3 g^2 n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2}{b} - \\
 & \frac{3 B^3 c g^2 n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2}{d} + \frac{3 a^2 B^3 g h n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2}{b^2} + \\
 & \frac{3 B^3 c^2 g h n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2}{d^2} - \frac{a^3 B^3 h^2 n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2}{b^3} - \\
 & \frac{B^3 c^3 h^2 n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2}{d^3} - \frac{B^3 c g^2 n^3 \operatorname{Log}[c+d x]^3}{d} + \frac{B^3 c^2 g h n^3 \operatorname{Log}[c+d x]^3}{d^2} - \\
 & \frac{B^3 c^3 h^2 n^3 \operatorname{Log}[c+d x]^3}{3 d^3} - \frac{6 A B^2 c g^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d} + \\
 & \frac{6 A B^2 c^2 g h n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^2} - \frac{2 A B^2 c^3 h^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^3} + \\
 & \frac{6 a^2 B^3 g h n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{b^2} + \frac{6 B^3 c^2 g h n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^2} - \\
 & \frac{12 a B^3 c g h n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{b d} - \frac{3 a^3 B^3 h^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{b^3} - \\
 & \frac{3 B^3 c^3 h^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^3} + \frac{3 a B^3 c^2 h^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{b d^2} + \\
 & \frac{3 a^2 B^3 c h^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{b^2 d} + \frac{3 a B^3 g^2 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{b} + \\
 & \frac{3 B^3 c g^2 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d} - \frac{3 a^2 B^3 g h n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{b^2} - \\
 & \frac{3 B^3 c^2 g h n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^2} + \frac{a^3 B^3 h^2 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{b^3} + \\
 & \frac{B^3 c^3 h^2 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^3} - \frac{6 B^3 c g^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d} +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{6 B^3 c^2 g h n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^2} - \\
 & \frac{2 B^3 c^3 h^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^3} - \frac{6 a B^3 g^2 n^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b} - \\
 & \frac{6 B^3 c g^2 n^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d} + \frac{12 a B^3 c g h n^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b d} - \\
 & \frac{2 a B^3 c^2 h^2 n^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b d^2} - \frac{2 a^2 B^3 c h^2 n^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b^2 d} + \\
 & 3 A^2 B g^2 x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \frac{6 a A B^2 g h n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b} - \\
 & \frac{6 A B^2 c g h n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d} - \frac{2 a^2 A B^2 h^2 n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b^2} + \\
 & \frac{2 A B^2 c^2 h^2 n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^2} + \frac{a^2 B^3 h^2 n^2 x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b^2} + \\
 & \frac{B^3 c^2 h^2 n^2 x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^2} - \frac{2 a B^3 c h^2 n^2 x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b d} + \\
 & 3 A^2 B g h x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \frac{a A B^2 h^2 n x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b} - \\
 & \frac{A B^2 c h^2 n x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d} + A^2 B h^2 x^3 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
 & \frac{6 a A B^2 g^2 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b} - \\
 & \frac{6 a^2 A B^2 g h n \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b^2} + \\
 & \frac{2 a^3 A B^2 h^2 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b^3} + \\
 & \frac{6 a^2 B^3 g h n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b^2} - \\
 & \frac{6 a B^3 c g h n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b d} - \\
 & \frac{3 a^3 B^3 h^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b^3} + \\
 & \frac{2 a B^3 c^2 h^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b d^2} + \\
 & \frac{a^2 B^3 c h^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b^2 d} - \\
 & \frac{3 a B^3 g^2 n^2 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b} + \\
 & \frac{3 a^2 B^3 g h n^2 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b^2} -
 \end{aligned}$$

$$\begin{aligned}
 & \frac{a^3 B^3 h^2 n^2 \text{Log}[a + b x]^2 \text{Log}[e (a + b x)^n (c + d x)^{-n}]}{b^3} - \\
 & \frac{6 A B^2 c g^2 n \text{Log}[c + d x] \text{Log}[e (a + b x)^n (c + d x)^{-n}]}{d} + \\
 & \frac{6 A B^2 c^2 g h n \text{Log}[c + d x] \text{Log}[e (a + b x)^n (c + d x)^{-n}]}{d^2} - \\
 & \frac{2 A B^2 c^3 h^2 n \text{Log}[c + d x] \text{Log}[e (a + b x)^n (c + d x)^{-n}]}{d^3} + \\
 & \frac{6 B^3 c^2 g h n^2 \text{Log}[c + d x] \text{Log}[e (a + b x)^n (c + d x)^{-n}]}{d^2} - \\
 & \frac{6 a B^3 c g h n^2 \text{Log}[c + d x] \text{Log}[e (a + b x)^n (c + d x)^{-n}]}{b d} - \\
 & \frac{3 B^3 c^3 h^2 n^2 \text{Log}[c + d x] \text{Log}[e (a + b x)^n (c + d x)^{-n}]}{d^3} + \\
 & \frac{a B^3 c^2 h^2 n^2 \text{Log}[c + d x] \text{Log}[e (a + b x)^n (c + d x)^{-n}]}{b d^2} + \\
 & \frac{2 a^2 B^3 c h^2 n^2 \text{Log}[c + d x] \text{Log}[e (a + b x)^n (c + d x)^{-n}]}{b^2 d} + \\
 & \frac{6 a B^3 g^2 n^2 \text{Log}[a + b x] \text{Log}[c + d x] \text{Log}[e (a + b x)^n (c + d x)^{-n}]}{b} + \\
 & \frac{6 B^3 c g^2 n^2 \text{Log}[a + b x] \text{Log}[c + d x] \text{Log}[e (a + b x)^n (c + d x)^{-n}]}{d} - \\
 & \frac{6 a^2 B^3 g h n^2 \text{Log}[a + b x] \text{Log}[c + d x] \text{Log}[e (a + b x)^n (c + d x)^{-n}]}{b^2} - \\
 & \frac{6 B^3 c^2 g h n^2 \text{Log}[a + b x] \text{Log}[c + d x] \text{Log}[e (a + b x)^n (c + d x)^{-n}]}{d^2} + \\
 & \frac{2 a^3 B^3 h^2 n^2 \text{Log}[a + b x] \text{Log}[c + d x] \text{Log}[e (a + b x)^n (c + d x)^{-n}]}{b^3} + \\
 & \frac{2 B^3 c^3 h^2 n^2 \text{Log}[a + b x] \text{Log}[c + d x] \text{Log}[e (a + b x)^n (c + d x)^{-n}]}{d^3} - \\
 & \frac{6 a B^3 g^2 n^2 \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \text{Log}[c + d x] \text{Log}[e (a + b x)^n (c + d x)^{-n}]}{b} + \\
 & \frac{6 a^2 B^3 g h n^2 \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \text{Log}[c + d x] \text{Log}[e (a + b x)^n (c + d x)^{-n}]}{b^2} - \\
 & \frac{2 a^3 B^3 h^2 n^2 \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \text{Log}[c + d x] \text{Log}[e (a + b x)^n (c + d x)^{-n}]}{b^3} - \\
 & \frac{3 B^3 c g^2 n^2 \text{Log}[c + d x]^2 \text{Log}[e (a + b x)^n (c + d x)^{-n}]}{d} + \\
 & \frac{3 B^3 c^2 g h n^2 \text{Log}[c + d x]^2 \text{Log}[e (a + b x)^n (c + d x)^{-n}]}{d^2} -
 \end{aligned}$$

$$\begin{aligned}
 & \frac{B^3 c^3 h^2 n^2 \text{Log}[c+d x]^2 \text{Log}[e(a+b x)^n (c+d x)^{-n}]}{d^3} - \\
 & \frac{6 B^3 c g^2 n^2 \text{Log}[a+b x] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \text{Log}[e(a+b x)^n (c+d x)^{-n}]}{d} + \\
 & \frac{6 B^3 c^2 g h n^2 \text{Log}[a+b x] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \text{Log}[e(a+b x)^n (c+d x)^{-n}]}{d^2} - \\
 & \frac{2 B^3 c^3 h^2 n^2 \text{Log}[a+b x] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \text{Log}[e(a+b x)^n (c+d x)^{-n}]}{d^3} + \\
 & 3 A B^2 g^2 x \text{Log}[e(a+b x)^n (c+d x)^{-n}]^2 + \frac{3 a B^3 g h n x \text{Log}[e(a+b x)^n (c+d x)^{-n}]^2}{b} - \\
 & \frac{3 B^3 c g h n x \text{Log}[e(a+b x)^n (c+d x)^{-n}]^2}{d} - \frac{a^2 B^3 h^2 n x \text{Log}[e(a+b x)^n (c+d x)^{-n}]^2}{b^2} + \\
 & \frac{B^3 c^2 h^2 n x \text{Log}[e(a+b x)^n (c+d x)^{-n}]^2}{d^2} + 3 A B^2 g h x^2 \text{Log}[e(a+b x)^n (c+d x)^{-n}]^2 + \\
 & \frac{a B^3 h^2 n x^2 \text{Log}[e(a+b x)^n (c+d x)^{-n}]^2}{2 b} - \frac{B^3 c h^2 n x^2 \text{Log}[e(a+b x)^n (c+d x)^{-n}]^2}{2 d} + \\
 & A B^2 h^2 x^3 \text{Log}[e(a+b x)^n (c+d x)^{-n}]^2 + \frac{3 a B^3 g^2 n \text{Log}[a+b x] \text{Log}[e(a+b x)^n (c+d x)^{-n}]^2}{b} - \\
 & \frac{3 a^2 B^3 g h n \text{Log}[a+b x] \text{Log}[e(a+b x)^n (c+d x)^{-n}]^2}{b^2} + \\
 & \frac{a^3 B^3 h^2 n \text{Log}[a+b x] \text{Log}[e(a+b x)^n (c+d x)^{-n}]^2}{b^3} - \\
 & \frac{3 B^3 c g^2 n \text{Log}[c+d x] \text{Log}[e(a+b x)^n (c+d x)^{-n}]^2}{d} + \\
 & \frac{3 B^3 c^2 g h n \text{Log}[c+d x] \text{Log}[e(a+b x)^n (c+d x)^{-n}]^2}{d^2} - \\
 & \frac{B^3 c^3 h^2 n \text{Log}[c+d x] \text{Log}[e(a+b x)^n (c+d x)^{-n}]^2}{d^3} + B^3 g^2 x \text{Log}[e(a+b x)^n (c+d x)^{-n}]^3 + \\
 & B^3 g h x^2 \text{Log}[e(a+b x)^n (c+d x)^{-n}]^3 + \frac{1}{3} B^3 h^2 x^3 \text{Log}[e(a+b x)^n (c+d x)^{-n}]^3 - \\
 & \frac{1}{b^3 d^3} B^2 n^2 (6 A b^3 c d^2 g^2 - 6 A b^3 c^2 d g h + 2 A b^3 c^3 h^2 - 6 b^3 B c^2 d g h n + 12 a b^2 B c d^2 g h n - \\
 & 6 a^2 b B d^3 g h n + 3 b^3 B c^3 h^2 n - 3 a b^2 B c^2 d h^2 n - 3 a^2 b B c d^2 h^2 n + 3 a^3 B d^3 h^2 n - 2 a B d^3 \\
 & (3 b^2 g^2 - 3 a b g h + a^2 h^2) n \text{Log}[a+b x] + 2 b^3 B c (3 d^2 g^2 - 3 c d g h + c^2 h^2) n \text{Log}[c+d x] + \\
 & 6 b^3 B c d^2 g^2 \text{Log}[e(a+b x)^n (c+d x)^{-n}] - 6 b^3 B c^2 d g h \text{Log}[e(a+b x)^n (c+d x)^{-n}] + \\
 & 2 b^3 B c^3 h^2 \text{Log}[e(a+b x)^n (c+d x)^{-n}]) \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] - \frac{1}{b^3 d^3} 2 B^2 n^2 \\
 & (-a B d^3 (3 b^2 g^2 - 3 a b g h + a^2 h^2) n \text{Log}[a+b x] + b^3 B c (3 d^2 g^2 - 3 c d g h + c^2 h^2) n \text{Log}[c+d x] + \\
 & a d^3 (3 b^2 g^2 - 3 a b g h + a^2 h^2) (A+B \text{Log}[e(a+b x)^n (c+d x)^{-n}])) \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] -
 \end{aligned}$$

$$\begin{aligned}
 & \frac{6 a B^3 g^2 n^3 \text{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]}{b} + \frac{6 B^3 c g^2 n^3 \text{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]}{d} + \\
 & \frac{6 a^2 B^3 g h n^3 \text{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]}{b^2} - \frac{6 B^3 c^2 g h n^3 \text{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]}{d^2} - \\
 & \frac{2 a^3 B^3 h^2 n^3 \text{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]}{b^3} + \frac{2 B^3 c^3 h^2 n^3 \text{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]}{d^3} - \\
 & \frac{6 a B^3 g^2 n^3 \text{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]}{b} + \frac{6 B^3 c g^2 n^3 \text{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]}{d} + \\
 & \frac{6 a^2 B^3 g h n^3 \text{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]}{b^2} - \frac{6 B^3 c^2 g h n^3 \text{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]}{d^2} - \\
 & \frac{2 a^3 B^3 h^2 n^3 \text{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]}{b^3} + \frac{2 B^3 c^3 h^2 n^3 \text{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]}{d^3}
 \end{aligned}$$

Problem 310: Result more than twice size of optimal antiderivative.

$$\int (g+h x) (A+B \text{Log}[e (a+b x)^n (c+d x)^{-n}])^3 dx$$

Optimal (type 4, 466 leaves, 13 steps):

$$\begin{aligned}
 & -\frac{1}{b^2 d^2} 3 B^2 (b c-a d)^2 h n^2 \text{Log}\left[\frac{b c-a d}{b(c+d x)}\right] (A+B \text{Log}[e (a+b x)^n (c+d x)^{-n}]) - \\
 & \frac{3 B (b c-a d) h n (a+b x) (A+B \text{Log}[e (a+b x)^n (c+d x)^{-n}])^2}{2 b^2 d} + \frac{1}{2 b^2 d^2} \\
 & 3 B (b c-a d) (2 b d g-b c h-a d h) n \text{Log}\left[\frac{b c-a d}{b(c+d x)}\right] (A+B \text{Log}[e (a+b x)^n (c+d x)^{-n}])^2 - \\
 & \frac{(b g-a h)^2 (A+B \text{Log}[e (a+b x)^n (c+d x)^{-n}])^3}{2 b^2 h} + \\
 & \frac{(g+h x)^2 (A+B \text{Log}[e (a+b x)^n (c+d x)^{-n}])^3}{2 h} - \frac{3 B^3 (b c-a d)^2 h n^3 \text{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{b^2 d^2} + \frac{1}{b^2 d^2} \\
 & 3 B^2 (b c-a d) (2 b d g-b c h-a d h) n^2 (A+B \text{Log}[e (a+b x)^n (c+d x)^{-n}]) \text{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right] - \\
 & \frac{3 B^3 (b c-a d) (2 b d g-b c h-a d h) n^3 \text{PolyLog}\left[3, \frac{d(a+b x)}{b(c+d x)}\right]}{b^2 d^2}
 \end{aligned}$$

Result (type 4, 3919 leaves):

$$\begin{aligned}
 & \frac{1}{2 b^2 d^2} \left(-12 A b^2 B^2 c d g n^2 - 12 a A b B^2 d^2 g n^2 + 12 a A b B^2 c d h n^2 + 12 a b B^3 d^2 g n^3 - \right. \\
 & 6 b^2 B^3 c^2 h n^3 + 6 a b B^3 c d h n^3 - 6 a^2 B^3 d^2 h n^3 + 2 A^3 b^2 d^2 g x - 3 A^2 b^2 B c d h n x + \\
 & 3 a A^2 b B d^2 h n x + A^3 b^2 d^2 h x^2 + 6 a A^2 b B d^2 g n \text{Log}[a+b x] - 3 a^2 A^2 B d^2 h n \text{Log}[a+b x] - \\
 & 6 a A b B^2 c d h n^2 \text{Log}[a+b x] + 6 a^2 A B^2 d^2 h n^2 \text{Log}[a+b x] + 12 b^2 B^3 c d g n^3 \text{Log}[a+b x] + \\
 & 12 a b B^3 d^2 g n^3 \text{Log}[a+b x] - 12 a b B^3 c d h n^3 \text{Log}[a+b x] - 6 a A b B^2 d^2 g n^2 \text{Log}[a+b x]^2 + \\
 & \left. 3 a^2 A B^2 d^2 h n^2 \text{Log}[a+b x]^2 + 3 a b B^3 c d h n^3 \text{Log}[a+b x]^2 - 3 a^2 B^3 d^2 h n^3 \text{Log}[a+b x]^2 + \right)
 \end{aligned}$$

$$\begin{aligned}
 & 2 a b B^3 d^2 g n^3 \operatorname{Log}[a+b x]^3 - a^2 B^3 d^2 h n^3 \operatorname{Log}[a+b x]^3 - 6 A^2 b^2 B c d g n \operatorname{Log}[c+d x] + \\
 & 3 A^2 b^2 B c^2 h n \operatorname{Log}[c+d x] + 6 A b^2 B^2 c^2 h n^2 \operatorname{Log}[c+d x] - 6 a A b B^2 c d h n^2 \operatorname{Log}[c+d x] - \\
 & 12 b^2 B^3 c d g n^3 \operatorname{Log}[c+d x] - 12 a b B^3 d^2 g n^3 \operatorname{Log}[c+d x] + 12 a b B^3 c d h n^3 \operatorname{Log}[c+d x] + \\
 & 12 A b^2 B^2 c d g n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] + 12 a A b B^2 d^2 g n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] - \\
 & 6 A b^2 B^2 c^2 h n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] - 6 a^2 A B^2 d^2 h n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] - \\
 & 6 b^2 B^3 c^2 h n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] + 6 a b B^3 c d h n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] - \\
 & 6 b^2 B^3 c d g n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x] - 12 a b B^3 d^2 g n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x] + \\
 & 3 b^2 B^3 c^2 h n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x] + 6 a^2 B^3 d^2 h n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x] - \\
 & 12 a A b B^2 d^2 g n^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x] + 6 a^2 A B^2 d^2 h n^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x] + \\
 & 12 a b B^3 d^2 g n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x] - \\
 & 6 a^2 B^3 d^2 h n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x] - 6 A b^2 B^2 c d g n^2 \operatorname{Log}[c+d x]^2 + \\
 & 3 A b^2 B^2 c^2 h n^2 \operatorname{Log}[c+d x]^2 + 3 b^2 B^3 c^2 h n^3 \operatorname{Log}[c+d x]^2 - \\
 & 3 a b B^3 c d h n^3 \operatorname{Log}[c+d x]^2 + 12 b^2 B^3 c d g n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2 + \\
 & 6 a b B^3 d^2 g n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2 - 6 b^2 B^3 c^2 h n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2 - \\
 & 3 a^2 B^3 d^2 h n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2 - 6 b^2 B^3 c d g n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2 - \\
 & 6 a b B^3 d^2 g n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2 + 3 b^2 B^3 c^2 h n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2 + \\
 & 3 a^2 B^3 d^2 h n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2 - 2 b^2 B^3 c d g n^3 \operatorname{Log}[c+d x]^3 + \\
 & b^2 B^3 c^2 h n^3 \operatorname{Log}[c+d x]^3 - 12 A b^2 B^2 c d g n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 & 6 A b^2 B^2 c^2 h n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 6 b^2 B^3 c^2 h n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
 & 12 a b B^3 c d h n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 6 a^2 B^3 d^2 h n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 & 6 b^2 B^3 c d g n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 6 a b B^3 d^2 g n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
 & 3 b^2 B^3 c^2 h n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 3 a^2 B^3 d^2 h n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
 & 12 b^2 B^3 c d g n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 6 b^2 B^3 c^2 h n^3 \operatorname{Log}[a+b x] \\
 & \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 12 b^2 B^3 c d g n^2 \operatorname{Log}[e(a+b x)^n(c+d x)^{-n}] - \\
 & 12 a b B^3 d^2 g n^2 \operatorname{Log}[e(a+b x)^n(c+d x)^{-n}] + 12 a b B^3 c d h n^2 \operatorname{Log}[e(a+b x)^n(c+d x)^{-n}] + \\
 & 6 A^2 b^2 B d^2 g x \operatorname{Log}[e(a+b x)^n(c+d x)^{-n}] - 6 A b^2 B^2 c d h n x \operatorname{Log}[e(a+b x)^n(c+d x)^{-n}] + \\
 & 6 a A b B^2 d^2 h n x \operatorname{Log}[e(a+b x)^n(c+d x)^{-n}] + 3 A^2 b^2 B d^2 h x^2 \operatorname{Log}[e(a+b x)^n(c+d x)^{-n}] + \\
 & 12 a A b B^2 d^2 g n \operatorname{Log}[a+b x] \operatorname{Log}[e(a+b x)^n(c+d x)^{-n}] - \\
 & 6 a^2 A B^2 d^2 h n \operatorname{Log}[a+b x] \operatorname{Log}[e(a+b x)^n(c+d x)^{-n}] - 6 a b B^3 c d h n^2 \operatorname{Log}[a+b x] \\
 & \operatorname{Log}[e(a+b x)^n(c+d x)^{-n}] + 6 a^2 B^3 d^2 h n^2 \operatorname{Log}[a+b x] \operatorname{Log}[e(a+b x)^n(c+d x)^{-n}] - \\
 & 6 a b B^3 d^2 g n^2 \operatorname{Log}[a+b x]^2 \operatorname{Log}[e(a+b x)^n(c+d x)^{-n}] + 3 a^2 B^3 d^2 h n^2 \operatorname{Log}[a+b x]^2 \\
 & \operatorname{Log}[e(a+b x)^n(c+d x)^{-n}] - 12 A b^2 B^2 c d g n \operatorname{Log}[c+d x] \operatorname{Log}[e(a+b x)^n(c+d x)^{-n}] +
 \end{aligned}$$

$$\begin{aligned}
 & 6 A b^2 B^2 c^2 h n \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]+6 b^2 B^3 c^2 h n^2 \operatorname{Log}[c+d x] \\
 & \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]-6 a b B^3 c d h n^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]+ \\
 & 12 b^2 B^3 c d g n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]+ \\
 & 12 a b B^3 d^2 g n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]- \\
 & 6 b^2 B^3 c^2 h n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]- \\
 & 6 a^2 B^3 d^2 h n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]- \\
 & 12 a b B^3 d^2 g n^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]+ \\
 & 6 a^2 B^3 d^2 h n^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]- \\
 & 6 b^2 B^3 c d g n^2 \operatorname{Log}[c+d x]^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]+ \\
 & 3 b^2 B^3 c^2 h n^2 \operatorname{Log}[c+d x]^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]- \\
 & 12 b^2 B^3 c d g n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]+ \\
 & 6 b^2 B^3 c^2 h n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]+ \\
 & 6 A b^2 B^2 d^2 g x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2-3 b^2 B^3 c d h n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2+ \\
 & 3 a b B^3 d^2 h n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2+3 A b^2 B^2 d^2 h x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2+ \\
 & 6 a b B^3 d^2 g n \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2- \\
 & 3 a^2 B^3 d^2 h n \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2- \\
 & 6 b^2 B^3 c d g n \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2+ \\
 & 3 b^2 B^3 c^2 h n \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2+ \\
 & 2 b^2 B^3 d^2 g x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^3+b^2 B^3 d^2 h x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^3+6 B^2 n^2 \\
 & (-2 A b^2 c d g+A b^2 c^2 h+b^2 B c^2 h n-2 a b B c d h n+a^2 B d^2 h n+a B d^2(2 b g-a h) n \operatorname{Log}[a+b x]+ \\
 & b^2 B c(-2 d g+c h) n \operatorname{Log}[c+d x]-2 b^2 B c d g \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]+ \\
 & b^2 B c^2 h \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]+ \\
 & 6 B^2 n^2(a B d^2(2 b g-a h) n \operatorname{Log}[a+b x]+b^2 B c(-2 d g+c h) n \operatorname{Log}[c+d x]+ \\
 & a d^2(-2 b g+a h)(A+B \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right])) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]+ \\
 & 12 b^2 B^3 c d g n^3 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]-12 a b B^3 d^2 g n^3 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]- \\
 & 6 b^2 B^3 c^2 h n^3 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]+6 a^2 B^3 d^2 h n^3 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]+ \\
 & 12 b^2 B^3 c d g n^3 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]-12 a b B^3 d^2 g n^3 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]- \\
 & 6 b^2 B^3 c^2 h n^3 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]+6 a^2 B^3 d^2 h n^3 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]
 \end{aligned}$$

Problem 311: Result more than twice size of optimal antiderivative.

$$\int (A+B \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right])^3 dx$$

Optimal (type 4, 203 leaves, 6 steps):

$$\frac{3 B (b c - a d) n \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)}\right] (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{b d} + \frac{(a + b x) (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^3}{b} + \frac{1}{b d}$$

$$6 B^2 (b c - a d) n^2 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]) \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right] - \frac{6 B^3 (b c - a d) n^3 \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{b (c + d x)}\right]}{b d}$$

Result (type 4, 1465 leaves):

$$\begin{aligned}
 & -\frac{1}{b d} \left(6 A b B^2 c n^2 + 6 a A B^2 d n^2 - 6 a B^3 d n^3 - A^3 b d x - 3 a A^2 B d n \log [a + b x] - 6 b B^3 c n^3 \log [a + b x] - \right. \\
 & 6 a B^3 d n^3 \log [a + b x] + 3 a A B^2 d n^2 \log [a + b x]^2 - a B^3 d n^3 \log [a + b x]^3 + \\
 & 3 A^2 b B c n \log [c + d x] + 6 b B^3 c n^3 \log [c + d x] + 6 a B^3 d n^3 \log [c + d x] - \\
 & 6 A b B^2 c n^2 \log [a + b x] \log [c + d x] - 6 a A B^2 d n^2 \log [a + b x] \log [c + d x] + \\
 & 3 b B^3 c n^3 \log [a + b x]^2 \log [c + d x] + 6 a B^3 d n^3 \log [a + b x]^2 \log [c + d x] + \\
 & 6 a A B^2 d n^2 \log \left[\frac{d (a + b x)}{-b c + a d} \right] \log [c + d x] - 6 a B^3 d n^3 \log [a + b x] \log \left[\frac{d (a + b x)}{-b c + a d} \right] \log [c + d x] + \\
 & 3 A b B^2 c n^2 \log [c + d x]^2 - 6 b B^3 c n^3 \log [a + b x] \log [c + d x]^2 - \\
 & 3 a B^3 d n^3 \log [a + b x] \log [c + d x]^2 + 3 b B^3 c n^3 \log \left[\frac{d (a + b x)}{-b c + a d} \right] \log [c + d x]^2 + \\
 & 3 a B^3 d n^3 \log \left[\frac{d (a + b x)}{-b c + a d} \right] \log [c + d x]^2 + b B^3 c n^3 \log [c + d x]^3 + \\
 & 6 A b B^2 c n^2 \log [a + b x] \log \left[\frac{b (c + d x)}{b c - a d} \right] - 3 b B^3 c n^3 \log [a + b x]^2 \log \left[\frac{b (c + d x)}{b c - a d} \right] - \\
 & 3 a B^3 d n^3 \log [a + b x]^2 \log \left[\frac{b (c + d x)}{b c - a d} \right] + 6 b B^3 c n^3 \log [a + b x] \log [c + d x] \log \left[\frac{b (c + d x)}{b c - a d} \right] + \\
 & 6 b B^3 c n^2 \log [e (a + b x)^n (c + d x)^{-n}] + 6 a B^3 d n^2 \log [e (a + b x)^n (c + d x)^{-n}] - \\
 & 3 A^2 b B d x \log [e (a + b x)^n (c + d x)^{-n}] - 6 a A B^2 d n \log [a + b x] \log [e (a + b x)^n (c + d x)^{-n}] + \\
 & 3 a B^3 d n^2 \log [a + b x]^2 \log [e (a + b x)^n (c + d x)^{-n}] + \\
 & 6 A b B^2 c n \log [c + d x] \log [e (a + b x)^n (c + d x)^{-n}] - \\
 & 6 b B^3 c n^2 \log [a + b x] \log [c + d x] \log [e (a + b x)^n (c + d x)^{-n}] - \\
 & 6 a B^3 d n^2 \log [a + b x] \log [c + d x] \log [e (a + b x)^n (c + d x)^{-n}] + \\
 & 6 a B^3 d n^2 \log \left[\frac{d (a + b x)}{-b c + a d} \right] \log [c + d x] \log [e (a + b x)^n (c + d x)^{-n}] + \\
 & 3 b B^3 c n^2 \log [c + d x]^2 \log [e (a + b x)^n (c + d x)^{-n}] + \\
 & 6 b B^3 c n^2 \log [a + b x] \log \left[\frac{b (c + d x)}{b c - a d} \right] \log [e (a + b x)^n (c + d x)^{-n}] - \\
 & 3 A b B^2 d x \log [e (a + b x)^n (c + d x)^{-n}]^2 - 3 a B^3 d n \log [a + b x] \log [e (a + b x)^n (c + d x)^{-n}]^2 + \\
 & 3 b B^3 c n \log [c + d x] \log [e (a + b x)^n (c + d x)^{-n}]^2 - b B^3 d x \log [e (a + b x)^n (c + d x)^{-n}]^3 + \\
 & 6 B^2 n^2 (-a B d n \log [a + b x] + b c (A + B n \log [c + d x] + B \log [e (a + b x)^n (c + d x)^{-n}])) \\
 & \text{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] + 6 B^2 n^2 (-a B d n \log [a + b x] + b B c n \log [c + d x] + \\
 & a d (A + B \log [e (a + b x)^n (c + d x)^{-n}])) \text{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] - \\
 & 6 b B^3 c n^3 \text{PolyLog} \left[3, \frac{d (a + b x)}{-b c + a d} \right] + 6 a B^3 d n^3 \text{PolyLog} \left[3, \frac{d (a + b x)}{-b c + a d} \right] - \\
 & 6 b B^3 c n^3 \text{PolyLog} \left[3, \frac{b (c + d x)}{b c - a d} \right] + 6 a B^3 d n^3 \text{PolyLog} \left[3, \frac{b (c + d x)}{b c - a d} \right] \Big)
 \end{aligned}$$

Problem 312: Unable to integrate problem.

$$\int \frac{(A + B \log [e (a + b x)^n (c + d x)^{-n}])^3}{g + h x} dx$$

Optimal (type 4, 425 leaves, 12 steps):

$$\begin{aligned}
 & - \frac{\text{Log}\left[\frac{bc-ad}{b(c+dx)}\right] (A+B \text{Log}[e(a+bx)^n(c+dx)^{-n}])^3}{h} + \\
 & \frac{(A+B \text{Log}[e(a+bx)^n(c+dx)^{-n}])^3 \text{Log}\left[1 - \frac{(dg-ch)(a+bx)}{(bg-ah)(c+dx)}\right]}{h} - \\
 & \frac{3Bn(A+B \text{Log}[e(a+bx)^n(c+dx)^{-n}])^2 \text{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{h} + \\
 & \frac{3Bn(A+B \text{Log}[e(a+bx)^n(c+dx)^{-n}])^2 \text{PolyLog}\left[2, \frac{(dg-ch)(a+bx)}{(bg-ah)(c+dx)}\right]}{h} + \\
 & \frac{6B^2n^2(A+B \text{Log}[e(a+bx)^n(c+dx)^{-n}]) \text{PolyLog}\left[3, \frac{d(a+bx)}{b(c+dx)}\right]}{h} - \\
 & \frac{6B^2n^2(A+B \text{Log}[e(a+bx)^n(c+dx)^{-n}]) \text{PolyLog}\left[3, \frac{(dg-ch)(a+bx)}{(bg-ah)(c+dx)}\right]}{h} - \\
 & \frac{6B^3n^3 \text{PolyLog}\left[4, \frac{d(a+bx)}{b(c+dx)}\right]}{h} + \frac{6B^3n^3 \text{PolyLog}\left[4, \frac{(dg-ch)(a+bx)}{(bg-ah)(c+dx)}\right]}{h}
 \end{aligned}$$

Result (type 8, 35 leaves):

$$\int \frac{(A+B \text{Log}[e(a+bx)^n(c+dx)^{-n}])^3}{g+hx} dx$$

Problem 313: Unable to integrate problem.

$$\int \frac{(A+B \text{Log}[e(a+bx)^n(c+dx)^{-n}])^3}{(g+hx)^2} dx$$

Optimal (type 4, 302 leaves, 6 steps):

$$\begin{aligned}
 & \frac{(a+bx)(A+B \text{Log}[e(a+bx)^n(c+dx)^{-n}])^3}{(bg-ah)(g+hx)} + \\
 & \left(\frac{3B(bc-ad)n(A+B \text{Log}[e(a+bx)^n(c+dx)^{-n}])^2 \text{Log}\left[1 - \frac{(dg-ch)(a+bx)}{(bg-ah)(c+dx)}\right]}{(bg-ah)(dg-ch)} + \right. \\
 & \left. \frac{6B^2(bc-ad)n^2(A+B \text{Log}[e(a+bx)^n(c+dx)^{-n}]) \text{PolyLog}\left[2, \frac{(dg-ch)(a+bx)}{(bg-ah)(c+dx)}\right]}{(bg-ah)(c+dx)} \right) / \\
 & \left((bg-ah)(dg-ch) - \frac{6B^3(bc-ad)n^3 \text{PolyLog}\left[3, \frac{(dg-ch)(a+bx)}{(bg-ah)(c+dx)}\right]}{(bg-ah)(dg-ch)} \right)
 \end{aligned}$$

Result (type 8, 35 leaves):

$$\int \frac{(A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^3}{(g + h x)^2} dx$$

Problem 314: Unable to integrate problem.

$$\int \frac{(A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^3}{(g + h x)^3} dx$$

Optimal (type 4, 629 leaves, 13 steps):

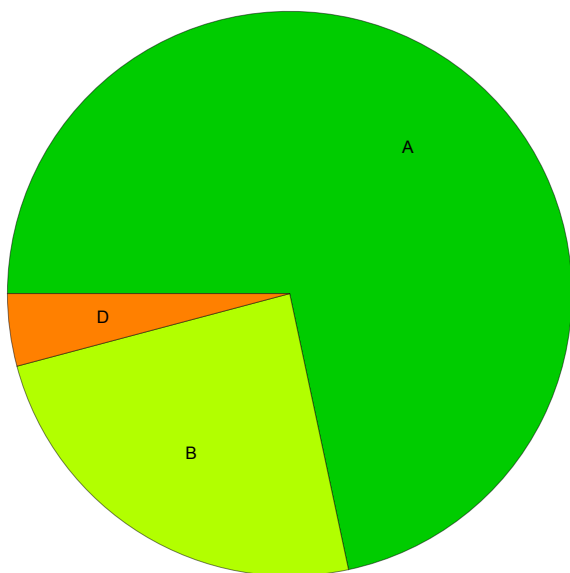
$$\begin{aligned} & \frac{3 B (b c - a d) h n (a + b x) (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{2 (b g - a h)^2 (d g - c h) (g + h x)} + \\ & \frac{b^2 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^3}{2 h (b g - a h)^2} - \frac{(A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^3}{2 h (g + h x)^2} + \\ & \frac{3 B^2 (b c - a d)^2 h n^2 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]) \operatorname{Log}\left[1 - \frac{(d g - c h) (a + b x)}{(b g - a h) (c + d x)}\right]}{(b g - a h)^2 (d g - c h)^2} + \\ & \frac{3 B (b c - a d) (2 b d g - b c h - a d h) n (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^2 \operatorname{Log}\left[1 - \frac{(d g - c h) (a + b x)}{(b g - a h) (c + d x)}\right]}{2 (b g - a h)^2 (d g - c h)^2} + \\ & \frac{3 B^3 (b c - a d)^2 h n^3 \operatorname{PolyLog}\left[2, \frac{(d g - c h) (a + b x)}{(b g - a h) (c + d x)}\right]}{(b g - a h)^2 (d g - c h)^2} + \frac{1}{(b g - a h)^2 (d g - c h)^2} 3 B^2 (b c - a d) \\ & (2 b d g - b c h - a d h) n^2 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]) \operatorname{PolyLog}\left[2, \frac{(d g - c h) (a + b x)}{(b g - a h) (c + d x)}\right] - \\ & \frac{3 B^3 (b c - a d) (2 b d g - b c h - a d h) n^3 \operatorname{PolyLog}\left[3, \frac{(d g - c h) (a + b x)}{(b g - a h) (c + d x)}\right]}{(b g - a h)^2 (d g - c h)^2} \end{aligned}$$

Result (type 8, 35 leaves):

$$\int \frac{(A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^3}{(g + h x)^3} dx$$

Summary of Integration Test Results

314 integration problems



- A - 225 optimal antiderivatives
- B - 76 more than twice size of optimal antiderivatives
- C - 0 unnecessarily complex antiderivatives
- D - 13 unable to integrate problems
- E - 0 integration timeouts